

Rents and Intangible Capital: A Q+ Framework

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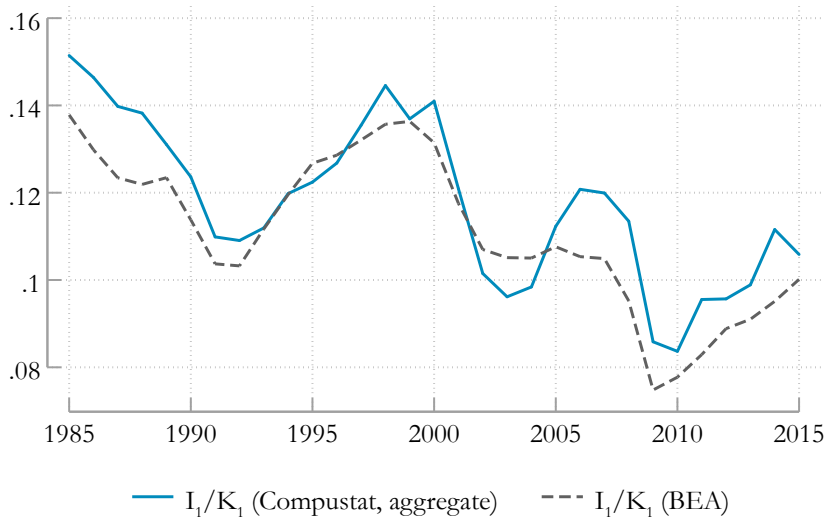
Question

Why is PPE investment weak ?

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PPE investment is weak

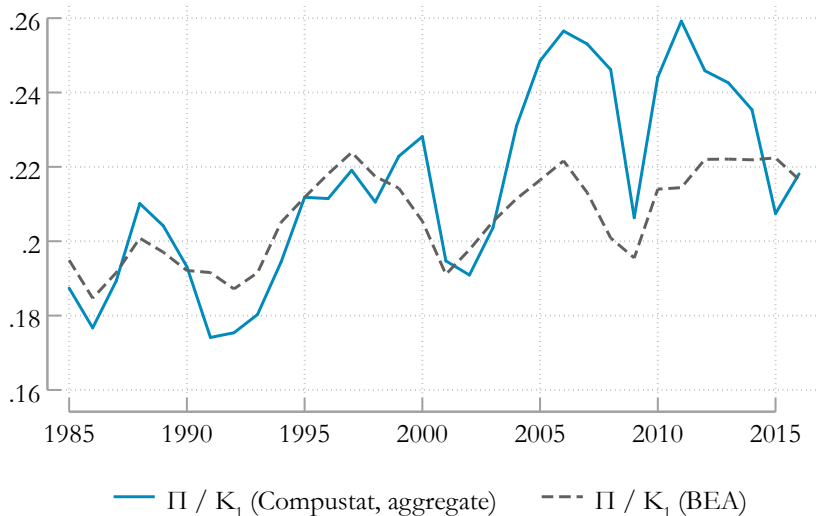


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Why is PPE investment weak ?

- ... *despite* high returns ?

PPE investment is weak despite high returns



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Explanation 1: **economic rents**

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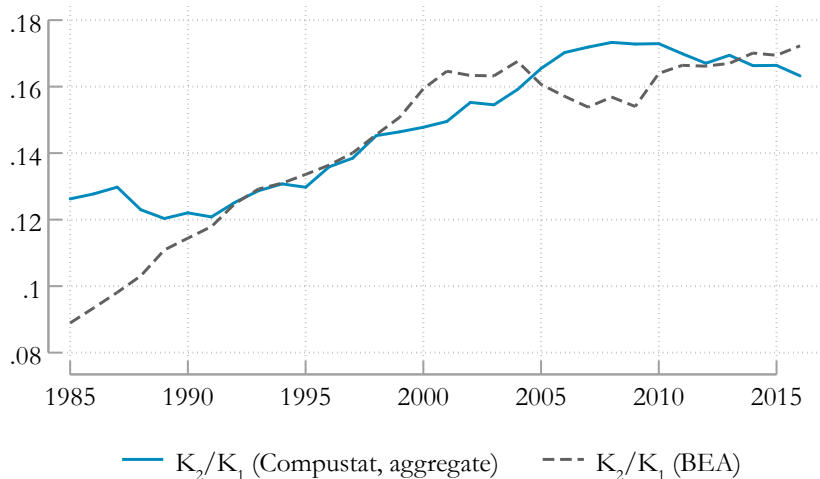
(Gutierrez and Philippon, 2018; Barkai, 2020)

- rents reduce the incentive to increase scale at the margin

Explanation 2: **intangibles**

(Crouzet and Eberly, 2018, 2019)

The growing importance of intangible capital



K_1 = PPE and K_2 = R&D capital.

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This paper

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What we do:

- Neo-classical investment model with rents + intangibles
 - "Q+": Lindenberg and Ross (1981) + Hayashi and Inoue (1991)
- Quantify in aggregate and sectoral data

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What we find:

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+ Omitted capital effect
+ **(Rents $\rightarrow$ intangibles) $\times$ (Omitted capital effect)**

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2. **Aggregate data:** $\text{intan} = 1/3$ to $2/3$ of gap
3. **Sectoral data:** no common trends; intan is $> 2/3$ of gap in high-growth sectors

1. Theory

A (fairly) general Q -theory model

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$$\begin{aligned} V_t^c(\mathbf{K}_t) = & \max_{\mathbf{K}_{t+1}} \Pi_t(K_t) - \tilde{\Phi}_t(\mathbf{K}_t, \mathbf{K}_{t+1}) + \mathbb{E}_t \left[M_{t,t+1} V_{t+1}^c(\mathbf{K}_{t+1}) \right] \\ \text{s.t.} \quad & K_t = F_t(\mathbf{K}_t), \quad \mathbf{K}_t = \left\{ K_{n,t} \right\}_{n=1}^2 \end{aligned}$$

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The value of the firm

Lemma

$$V_t^e = q_{1,t}K_{1,t+1} + q_{2,t}K_{2,t+1} + \sum_{n=1}^2 \sum_{k \geq 1} \mathbb{E}_t [M_{t,t+k} (\mu - 1) \Pi_{n,t+k} K_{n,t+k}]$$

$$V_t^e = \mathbb{E}_t [M_{t,t+1} V_{t+1}^c], \quad q_{n,t} \equiv \frac{\partial V_t^e}{\partial K_{n,t+1}}, \quad \Pi_{n,t} \equiv \frac{\partial \Pi_t}{\partial K_t} \frac{\partial K_t}{\partial K_{n,t}}.$$

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- $\mu > 1$: $V_t^e = q_{1,t}K_{1,t+1} + q_{2,t}K_{2,t+1} + \text{rents}$ (Lindenberg and Ross, 1981)

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$$(\mu - 1) \Pi_{n,t} = \underbrace{\left(\frac{\Pi_t}{K_t} - \frac{\partial \Pi_t}{\partial K_t} \right)}_{\text{gap btw. average and marginal product}} \times \frac{\partial K_t}{\partial K_{n,t}}$$

gap btw. average and marginal product

The investment gap

$$Q_{1,t} - q_{1,t}$$

The investment gap

$$Q_{1,t} - q_{1,t} = 0$$

No intan + no rents ($\mu = 1$): no investment gap, $Q_{1,t} = q_{1,t}$ (Hayashi, 1982)

The investment gap

$$Q_{1,t} - q_{1,t} = \sum_{k \geq 1} \mathbb{E}_t [M_{t,t+k} (\mu - 1) \Pi_{1,t+k} (1 + g_{1,t+k})]$$

No intan + rents ($\mu > 1$): $Q_{1,t} > q_{1,t}$ due to **rents**

(Lindenberg and Ross, 1981)

The investment gap

$$Q_{1,t} - q_{1,t} =$$

$$q_{2,t} \frac{K_{2,t+1}}{K_{1,t+1}}$$

Intan + no rents ($\mu = 1$): $Q_{1,t} > q_{1,t}$ due to **omitted intangibles** (Hayashi and Inoue, 1991)

The investment gap

$$\begin{aligned} Q_{1,t} - q_{1,t} &= \sum_{k \geq 1} \mathbb{E}_t [M_{t,t+k} (\mu - 1) \Pi_{1,t+k} (1 + g_{1,t+k})] \\ &+ q_{2,t} \frac{K_{2,t+1}}{K_{1,t+1}} \end{aligned}$$

Intan + rents ($\mu > 1$):

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Intan + rents ($\mu > 1$): additional term: **omitted intangibles** $\times$ **rents**

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Balanced growth: productivity grows at rate g ; constant discount rate r

The investment gap

$$\begin{aligned} Q_1 - q_1 &= \frac{(\mu - 1)R_1}{r - g} && \text{(rents} \rightarrow \text{physical capital)} \\ &+ q_2 \frac{K_{2,t+1}}{K_{1,t+1}} && \text{(intangibles)} \\ &+ \frac{(\mu - 1)R_2}{r - g} \times \frac{K_{2,t+1}}{K_{1,t+1}} && \text{(rents} \rightarrow \text{intangibles)} \end{aligned}$$

Balanced growth: $R_n \equiv r + \delta_n + \gamma_n g r, \quad n = 1, 2$

2. Measurement: aggregate data

Constructing the investment gap

$$Q_1 - q_1 = \frac{(\mu - 1)R_1}{r - g} + q_2 S + \frac{(\mu - 1)R_2}{r - g} \times S$$

Scope: non-financial corporate business (NFCB) sector, 1947-2017

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5 data moments needed to construct the investment gap:

$S = \frac{K_{2,t+1}}{K_{1,t+1}}$ ratio of intangible to physical capital BEA; $K_{2,t+1}$ = only R&D capital

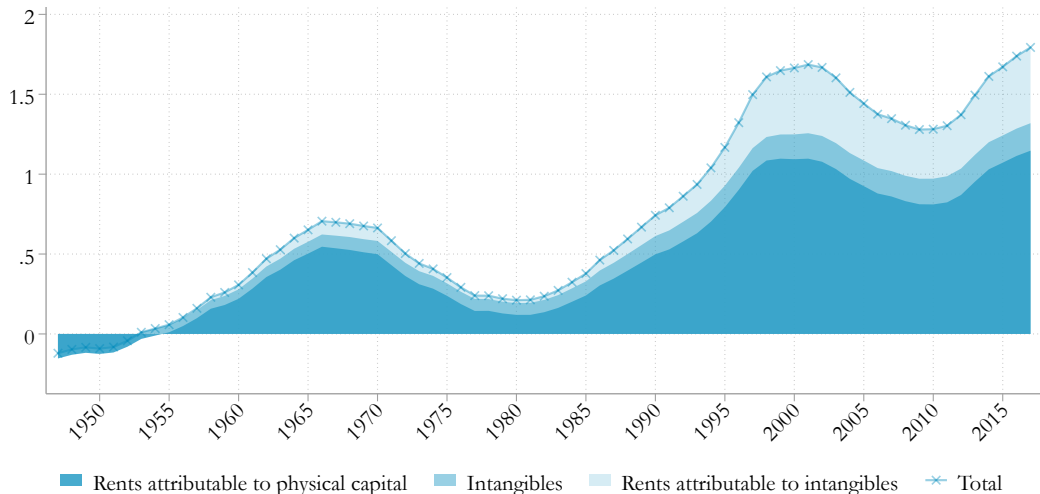
$ROA_1 = \frac{\Pi_t}{K_{1,t}}$ return to physical capital BEA; Π_t = operating surplus

ι_1, ι_2 gross investment rates BEA

$Q_1 = \frac{V_t}{K_{1,t+1}}$ average Q of physical capital Flow of Funds; V_t = m.v. of debt + equity

The investment gap in the non-financial sector

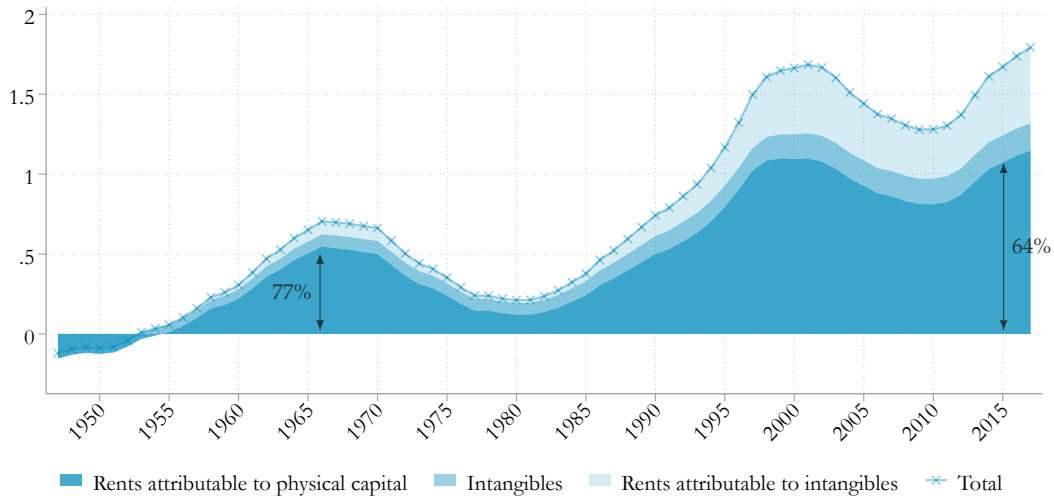
(adj. costs = 0)



Adjustment costs

The investment gap in the non-financial sector

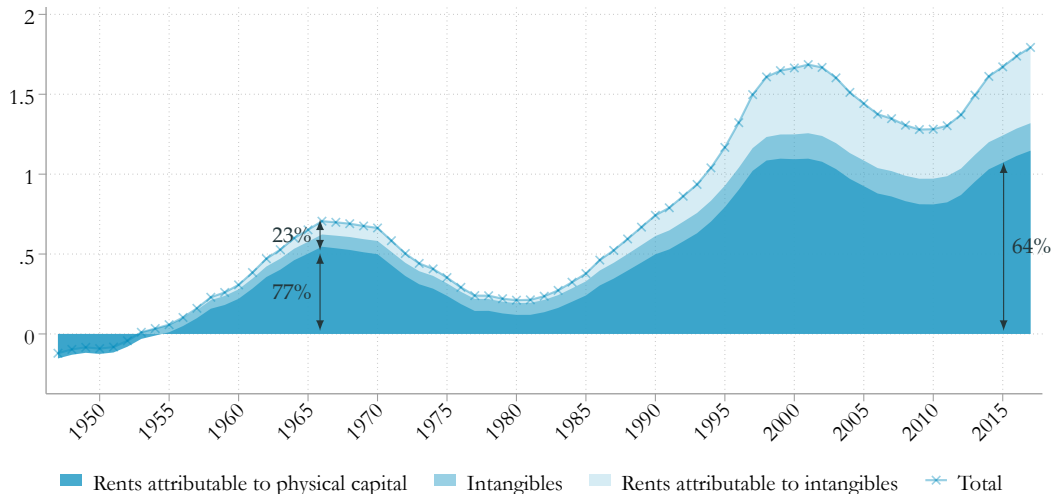
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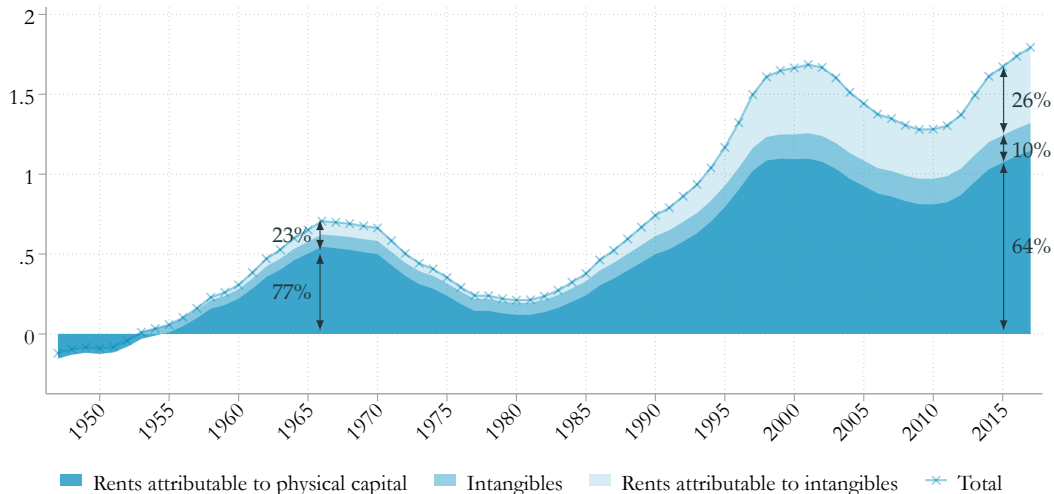
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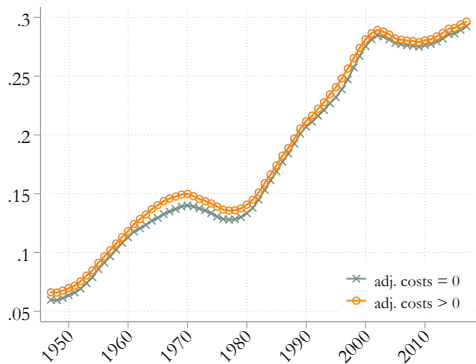
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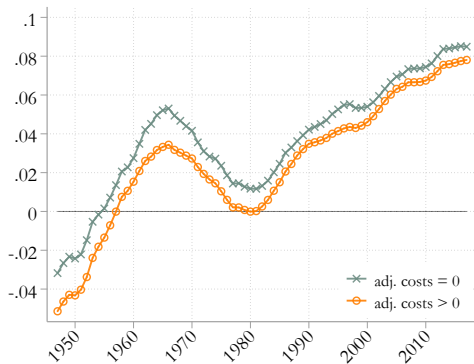
Adjustment costs

Underlying structural changes

Cobb-Douglas intan share $K_t = K_{1,t}^{1-\eta} K_{2,t}^{\eta}$

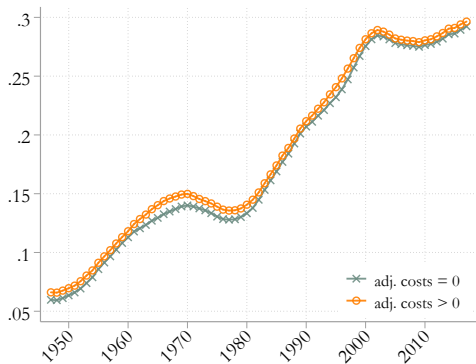


Rents/v.a. $s = (1 - WL/PY) \left(1 - \frac{1}{\mu}\right)$

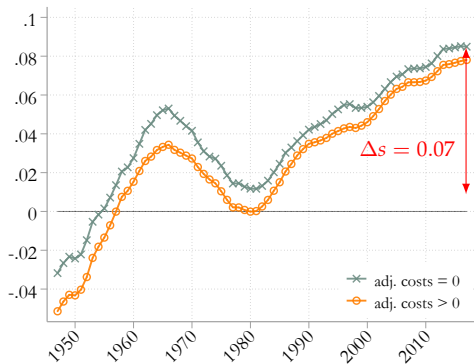


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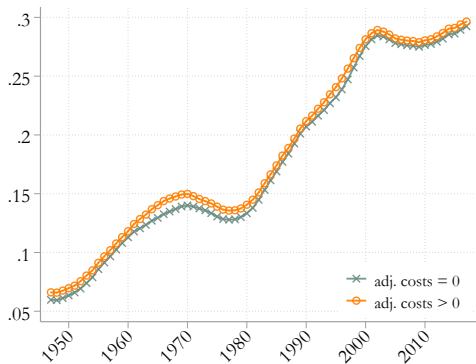


- Mild discount rate decline (7.9% → 5.6%), consisent with small rise in risk premia

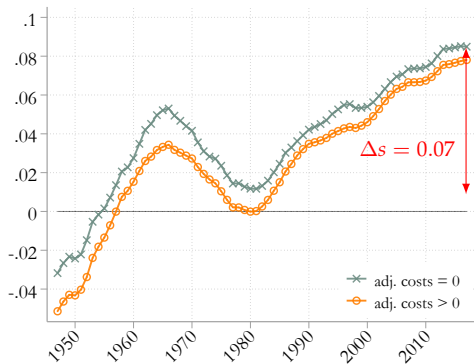
Caballero, Gourinchas and Farhi (2017), Farhi and Gourio (2018)

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User costs

Counterfactuals

Robustness

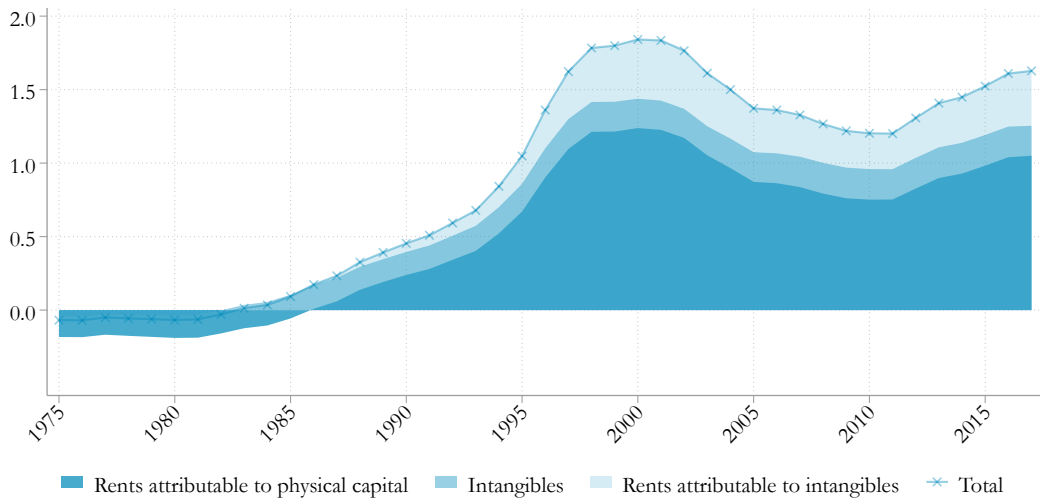
3. Measurement: firm-level data

The investment gap: publicly traded firms

(intan = R&D)

The investment gap: publicly traded firms

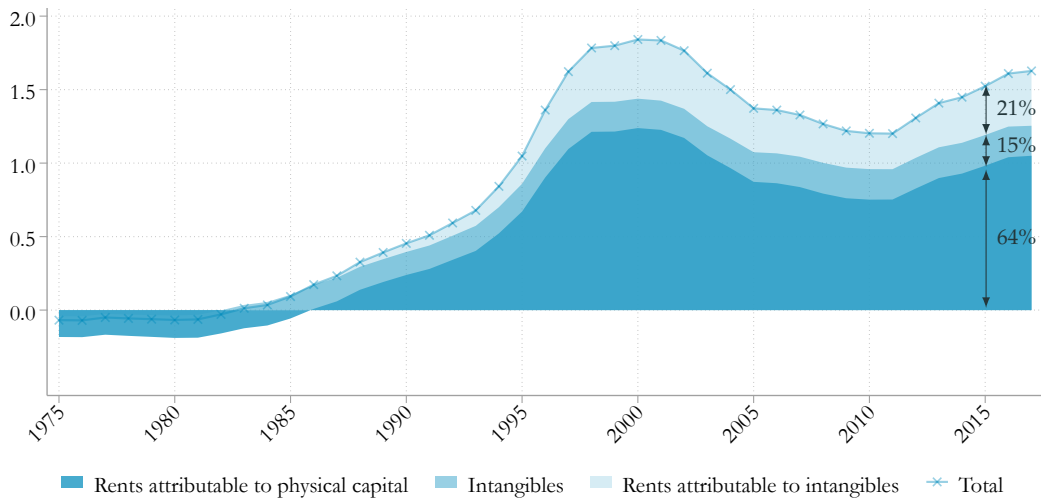
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Structural changes

The investment gap: publicly traded firms

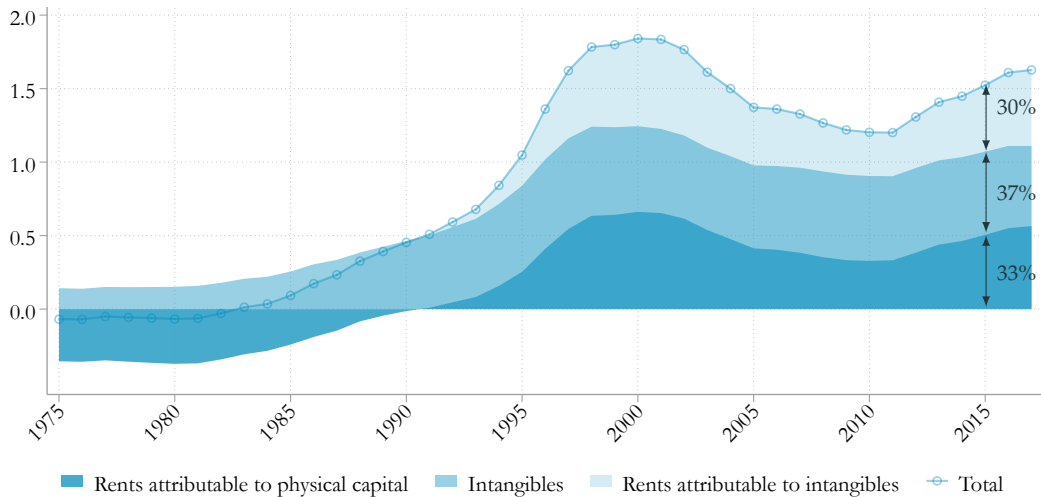
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Structural changes

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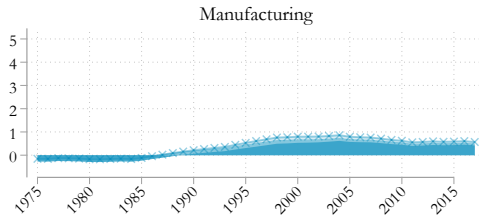
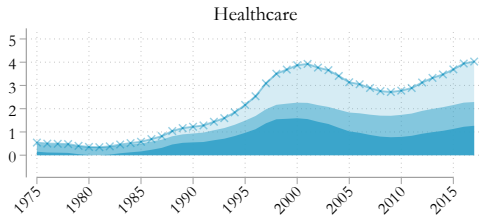
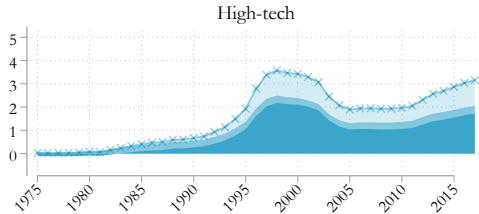
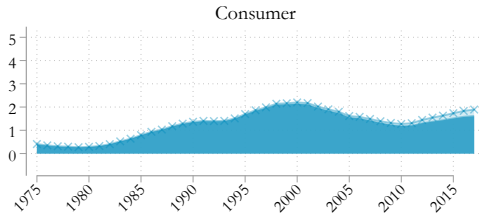
(intan = R&D + org. cap.)



Structural changes

The investment gap across sectors

(intan = R&D)



■ Rents attributable to physical capital ■ Intangibles ■ Rents attributable to intangibles * Total

Consumer sector

Conclusion

Conclusion

1. General decomposition of the investment gap:

$$\begin{aligned} Q_1 - q_1 &= \text{Rents} \rightarrow \text{physical capital} \\ &+ \text{Omitted capital effect} \\ &+ (\text{Rents} \rightarrow \text{intangibles}) \times (\text{Omitted capital effect}) \end{aligned}$$

2. Aggregate data: intan is $1/3 - 2/3$ of $Q_1 - q_1$; $\Delta s = 0.07$ instead of 0.12
3. Sectoral data: heterogeneous trends; intan is $> 2/3$ of the gap in Health, Tech

Additional slides

Related literature

1. Aggregate implications of rising rents:

- **Gutierrez and Philippon (2017, 2018), Farhi and Gourio (2018), Barkai (2019), Karabarbounis and Neiman (2019),** Autor et al. (2019), Caballero, Farhi, and Gourinchas (2017), Caballero and Farhi (2018), Eggertsson, Robbins and Wold (2018), Hall (2018), De Loecker and Eeckhout (2019), Basu (2019)

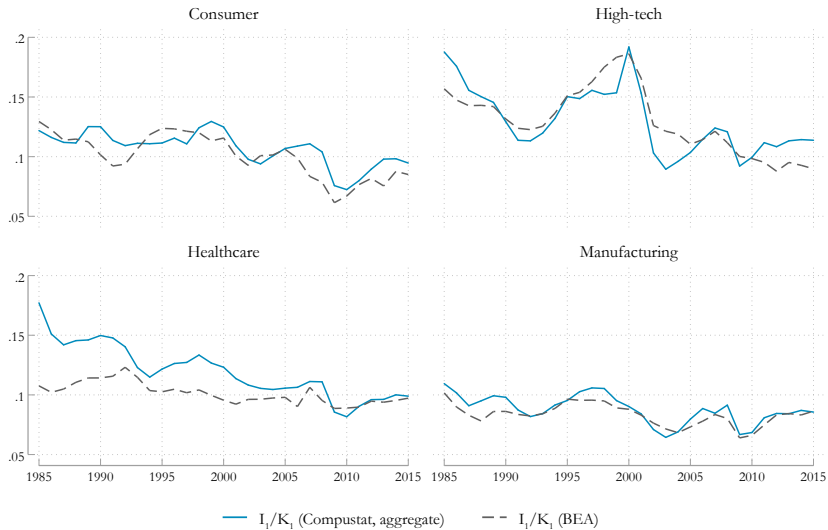
This paper : investment- Q ; new approach for estimating of rents; sectoral heterogeneity

2. Q theory and firm value:

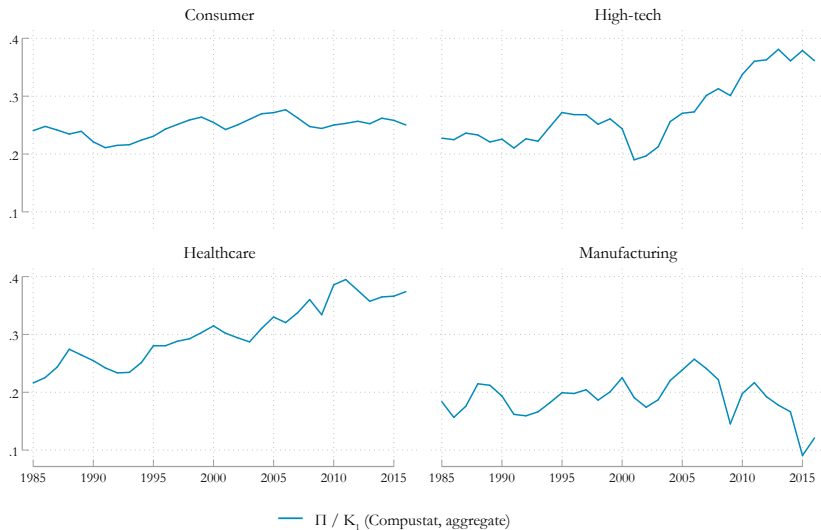
- Lindenberg and Ross (1981), Hayashi and Inoue (1991), Chirinko (1993), Abel and Eberly (1994), Cooper and Ejarque (2003), Hansen, Heaton and Li (2005), Abel and Eberly (2011), Eisfeldt and Papanikolaou (2013), Ai, Croce and Li (2013), **Hall (2001), Prescott and McGrattan (2010), Peters and Taylor (2017), Andrei, Mann, Moyen (2019), Belo, Gala, Salomao, Vitorino (2019)**

This paper : general decomposition of $Q - q$, including market power

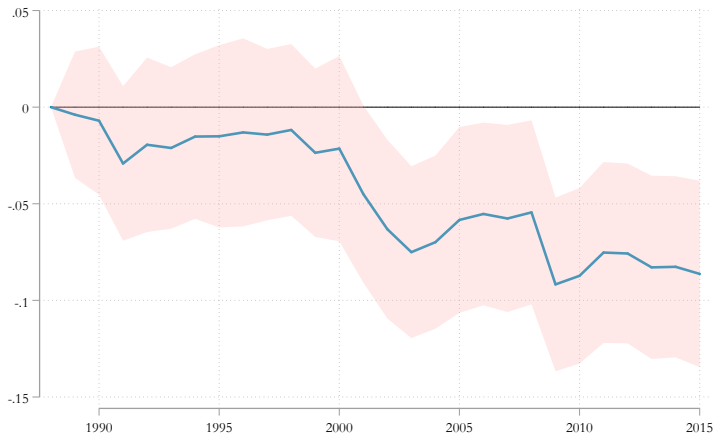
PPE investment is weak: sectoral data



PPE investment is weak despite high returns: sectoral data

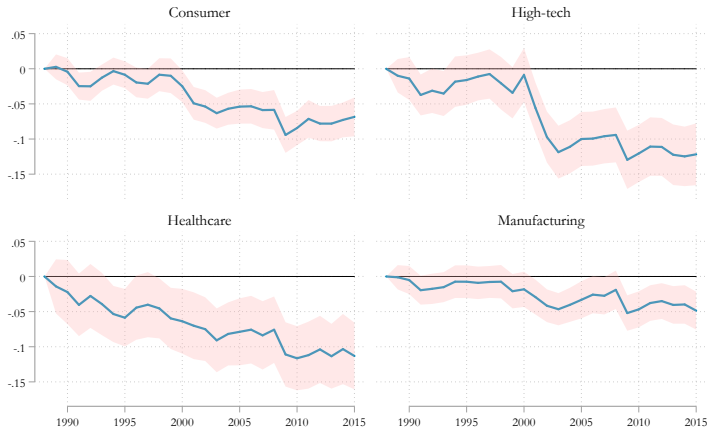


Investment is weak relative to Q



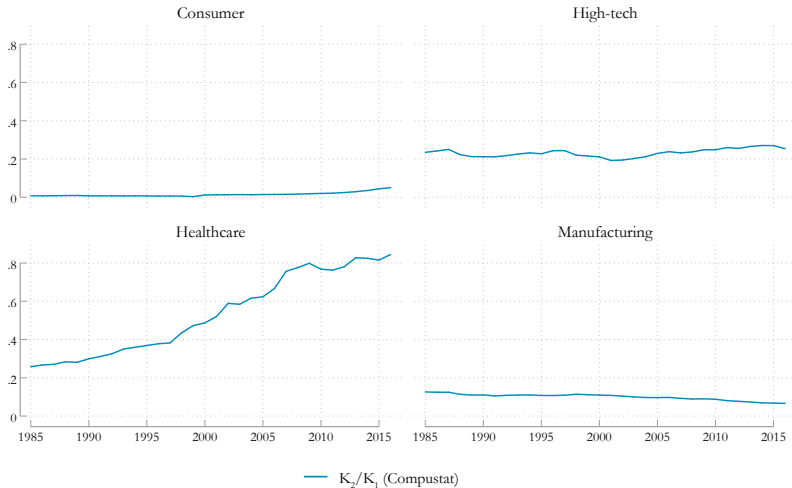
$$i_{j,t} = \alpha_j + \gamma_t + \delta Q_{j,t} + \beta CF_{j,t} + \epsilon_{j,t}$$

Investment is weak relative to Q: sectoral data



$$i_{j,t} = \alpha_j + \gamma_t + \delta Q_{j,t} + \beta CF_{j,t} + \epsilon_{j,t}$$

The growing importance of intangibles: sectoral data



K_1 = PPE and K_2 = R&D capital.

How general is this model?

- No restrictions on exogenous shifters to Π_t , F_t , and $\Phi_{n,t}$

- Particular cases of this framework:

Lindenberg and Ross (1981), Hayashi (1982), Abel (1983), Abel and Blanchard (1986), Hayashi and Inoue (1991), Abel and Eberly (1994, case I), Abel and Eberly (2011), Peters and Taylor (2017), ...

- What about labor?

The model can accommodate any flexible input: $\mu = \frac{\tilde{\mu} - \alpha}{1 - \alpha}$

- Which cases does this model **not** fit?

- Non-homogeneous and/or non-smooth adjustment costs
- Endogenous markups
- Financial frictions

The investment gap in the general case

The first-order condition for investment is:

$$g_{n,t+1} = \Psi_{n,t} (q_{n,t} - 1)$$

where:

$$\Psi_{n,t}(y) = (\Phi'_{n,t})^{-1} (1 + y) - 1.$$

Since $\Phi_{n,t}$ is convex, $\Psi_{n,t}$ is strictly increasing. Therefore:

$$\begin{aligned} g_{n,t+1} &= \Psi_{n,t} (q_{n,t} - 1) \\ &= \Psi_{n,t} (Q_{n,t} - 1 - G_{n,t}) \\ &< \Psi_{n,t} (Q_{n,t} - 1) \quad \text{iff} \quad G_{n,t} > 0 \end{aligned}$$

Total Q

Define the total investment rate as:
$$i_t^{(tot)} = \frac{\sum_{n=1}^N I_{n,t}}{\sum_{n=1}^N K_{n,t}} = \sum_{n=1}^N w_{n,t} i_{n,t}.$$

In the quadratic adj. cost case:

$$i_t^{(tot)} = \tilde{\delta}_t + \sum_{n=1}^N \frac{w_{n,t}}{\gamma_n} (q_{n,t} - 1), \quad \tilde{\delta}_t = \sum_{n=1}^N w_{n,t} \delta_n.$$

Let $Q_t^{(tot)} \equiv \frac{V_t^e}{\sum_{n=1}^N K_{n,t+1}}$. Then:

$$i_t^{(tot)} = \tilde{\delta}_t + \frac{1}{\gamma} (Q_t^{(tot)} - 1)$$

if and only if $\mu = 1$, and:

- $\gamma_n = \gamma$ for all n ;
- or, $q_{n,t} = q_t$ for all n .

Stochastic growth

Suppose A_t follows the “regime-switching process”:

$$\frac{A_{t+1}}{A_t} = 1 + g_t = \begin{cases} 1 + g_{t-1} & \text{w.p. } (1 - \lambda) \\ 1 + \tilde{g} & \text{w.p. } \lambda \end{cases}, \quad \tilde{g} \sim F(.).$$

Then:

$$\begin{aligned} G_{1,t} &= \frac{(\mu - 1)}{r - \nu(g_t)} R_1 && \text{(Rents } \rightarrow \text{ physical capital)} \\ &+ S && \text{(Omitted capital effect)} \\ &+ \frac{(\mu - 1)}{r - \nu(g_t)} R_2 S && \text{(Rents } \rightarrow \text{ intangibles)} \end{aligned}$$

where: $\frac{1}{r - \nu(g_t)} = \frac{1}{r - \mathbb{E}(\tilde{g})} \left(1 + \frac{g_t - \mathbb{E}(\tilde{g})}{1 + r} \right)$ if $\lambda = 1$.

Stochastic growth

The expression for $\nu(\cdot)$ is:

$$\nu(g_t) = g_t + \lambda(1 + g_t) \frac{(r - g_t)\zeta^* - (1 + r)}{(1 + r) + \lambda(1 + g_t)\zeta^*}$$

where ζ^* is a constant that only depends on $F(\cdot)$, λ and r .

Analytical example

A microfoundation for Example 1 (1/2)

Representative household:

$$U_t = \max \frac{C_t^{1-\sigma}}{1-\sigma} + \beta U_{t+1}, \quad (1)$$

implying $M_{t,t+1} = \beta \left(\frac{C_{t+1}}{C_t} \right)^{-\sigma}$.

Final goods producer

$$Y_t = \left(\int_0^1 Y_{j,t}^{\frac{1}{\tilde{\mu}}} dj \right)^{\tilde{\mu}}, \quad \tilde{\mu} > 1. \quad (2)$$

Intermediate goods producer: $Y_{j,t} = Z_{j,t} K_{j,t}^\alpha L_{j,t}^{1-\alpha}$, implying the profit function:

$$\begin{aligned} \Pi_{j,t} &= A_{j,t}^{\frac{1}{\mu}-1} K_{j,t}^{\frac{1}{\mu}} \\ \mu &= 1 + \frac{\tilde{\mu}-1}{\alpha}, \\ A_{j,t} &= (\alpha + \tilde{\mu} - 1)^{1+\frac{\alpha}{\tilde{\mu}-1}} \tilde{\mu}^{-\frac{\tilde{\mu}}{\tilde{\mu}-1}} (1-\alpha)^{\frac{1-\alpha}{\tilde{\mu}-1}} D_t W_t^{-\frac{1-\alpha}{\tilde{\mu}-1}} Z_{j,t}^{\frac{1}{\tilde{\mu}-1}}, \\ D_t &\equiv P_t^{\frac{\tilde{\mu}}{\tilde{\mu}-1}} Y_t. \end{aligned}$$

A microfoundation for Example 1 (2/2)

Rest of the solution to the problem is:

$$P_{j,t} = \tilde{\mu} MC_{j,t}$$

$$L_{j,t} = \left(\frac{(1-\alpha)MC_{j,t}Z_j}{W_t} \right)^{\frac{1}{\alpha}} K_{j,t}$$

$$MC_{j,t} = (1-\alpha)^{-\frac{(1-\alpha)(\tilde{\mu}-1)}{\tilde{\mu}-1+\alpha}} \tilde{\mu}^{-\frac{\alpha\tilde{\mu}}{\tilde{\mu}-1+\alpha}} D_t^{\frac{\alpha(\tilde{\mu}-1)}{\alpha+\tilde{\mu}-1}} W_t^{\frac{(1-\alpha)(\tilde{\mu}-1)}{\tilde{\mu}-1+\alpha}} Z_j^{-\frac{\tilde{\mu}-1}{\tilde{\mu}-1+\alpha}} K_{j,t}^{-\frac{(\tilde{\mu}-1)\alpha}{\tilde{\mu}-1+\alpha}}.$$

This implies:

$$LS_{j,t} \equiv \frac{W_t L_{j,t}}{P_{j,t} Y_t} = \frac{1-\alpha}{\tilde{\mu}}.$$

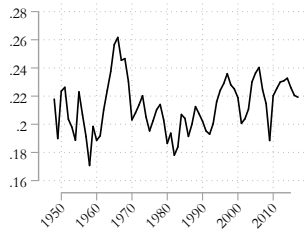
We have:

$$\tilde{\mu} = \alpha(\mu - 1) + 1 = (1 - \tilde{\mu} LS_{j,t})(\mu - 1) + 1,$$

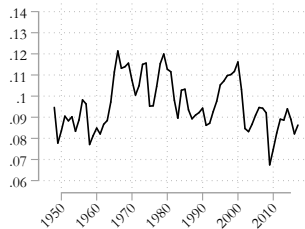
and so, solving for $\tilde{\mu}$:

$$\tilde{\mu} = \frac{\mu}{\mu LS_{j,t} + (1 - LS_{j,t})}.$$

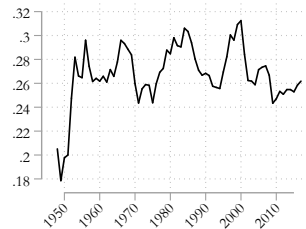
Returns to physical capital, ROA_1



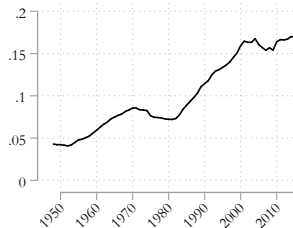
Physical investment rate, i_1



Intangible investment rate, i_2



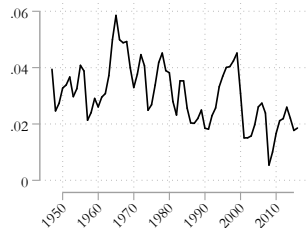
Ratio of intangible to physical capital, S



Average Tobin's Q of physical capital, Q_1

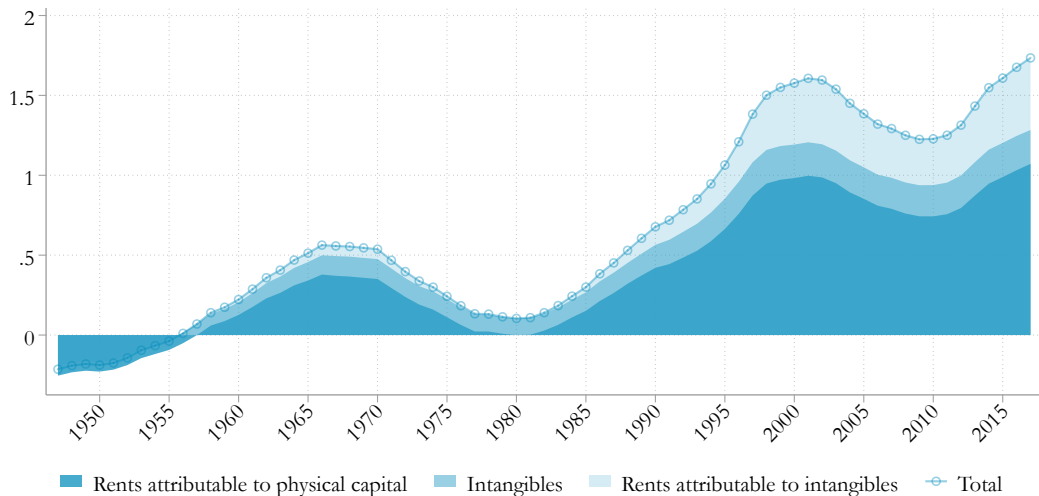


Growth rate of total capital stock, g



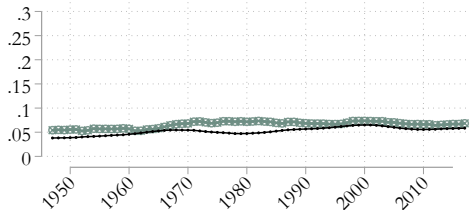
The investment gap in the non-financial sector

(adj. costs > 0)

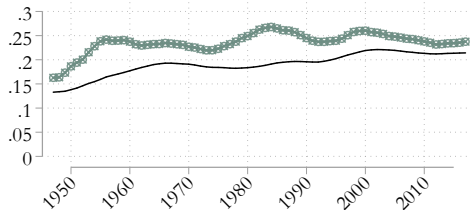


$$\gamma_1 = 3, \quad \gamma_2 = 12 \quad (\text{Belo et al., 2019})$$

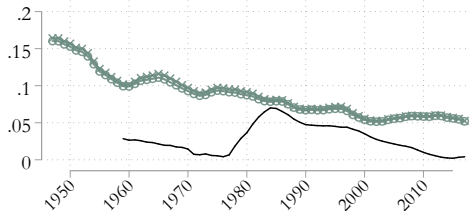
Implied depreciation rate, physical capital



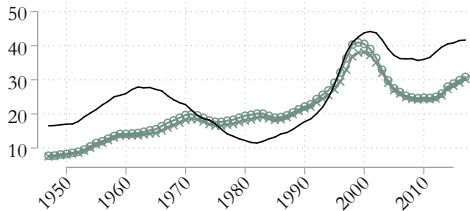
Implied depreciation rate, intangible capital



Implied discount rate



Implied PD ratio



✕ zero adjustment costs

○ positive adjustment costs

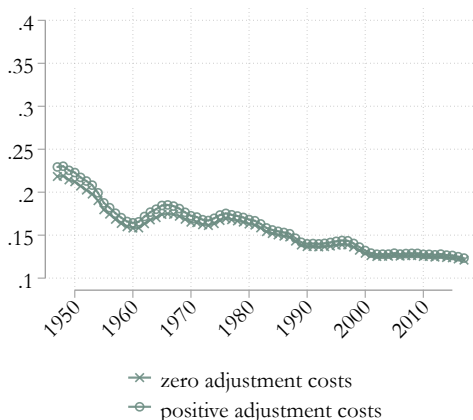
— data

User costs

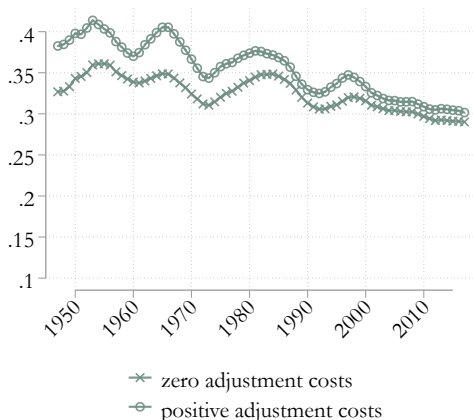
User costs

$$R_n = r + \delta_n + \gamma_n r g$$

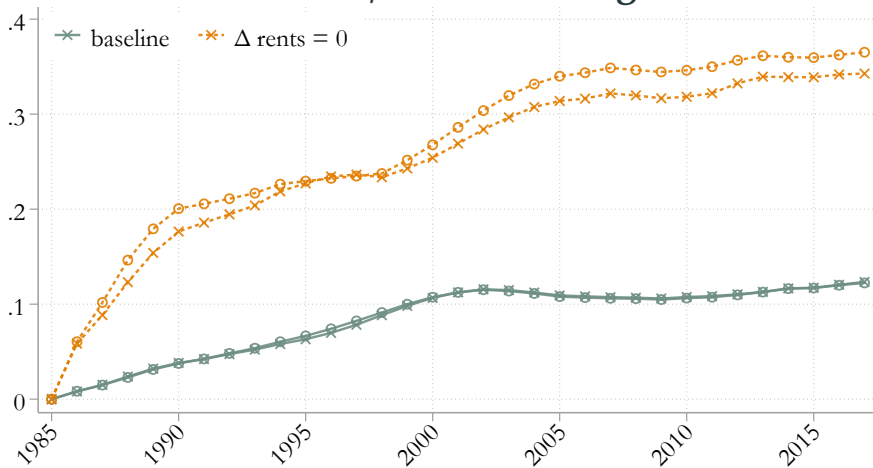
Physical capital



Intangible capital



Counterfactual: intan share η with no change in rents



$S_t^f = (K_{2,t}/K_{1,t})^f$: 9% $\rightarrow$ 39%, vs. 9% $\rightarrow$ 17% in the R&D data

Robustness

Robustness

- Adjustment costs $\gamma_1 \in [0, 10]$ and $\gamma_2 \in [0, 20]$

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Adjustment costs

$\gamma_1 = \gamma_2 = 0$: lowest contribution of intan to $Q_1 - q_1$; highest rents

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- Alternative measure of net claims on NFCB sector

Using net NFCB claims

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Matching PD ratio

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larger investment gap, particularly 1965-1975;

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- Implications for the labor share

Labor share

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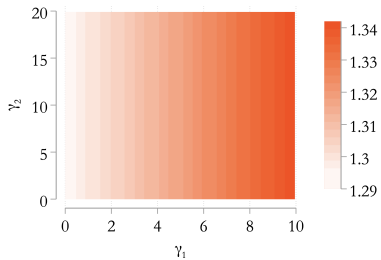
- Implications for the labor share

Labor share

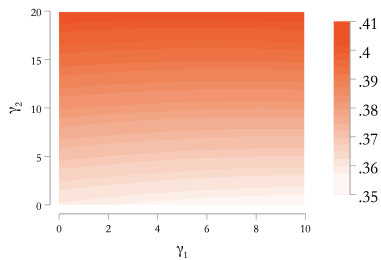
implied labor share $0.69 \rightarrow 0.64$, but earlier than in the data

Back

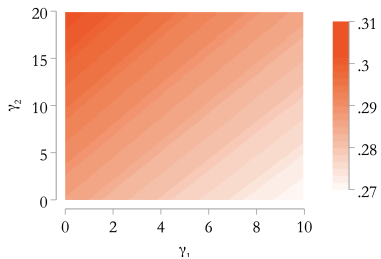
1985-2015 change in $Q_1 - q_1$



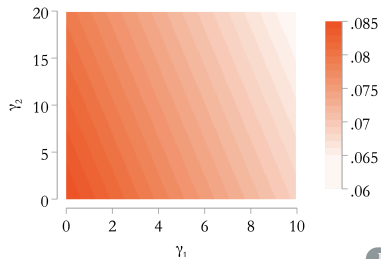
2015 contribution of intangibles to $Q_1 - q_1$



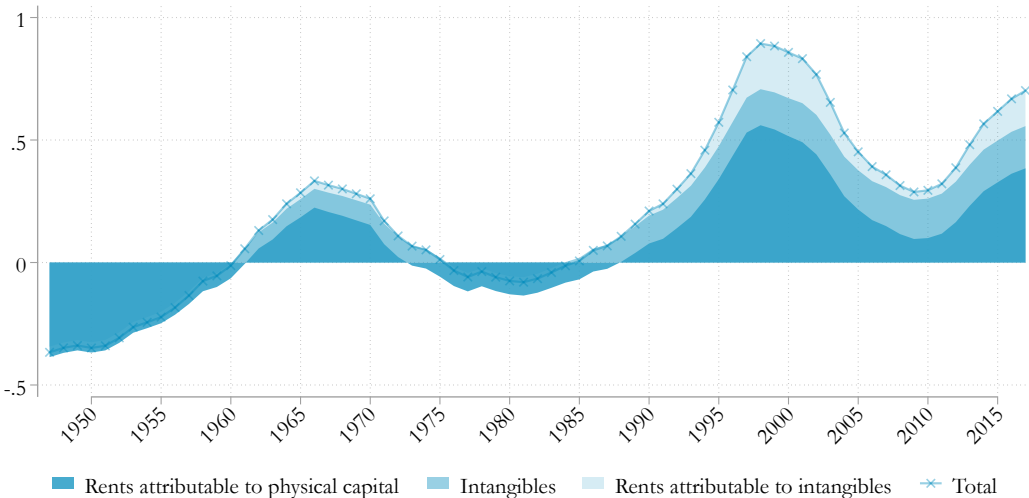
2015 intangible share



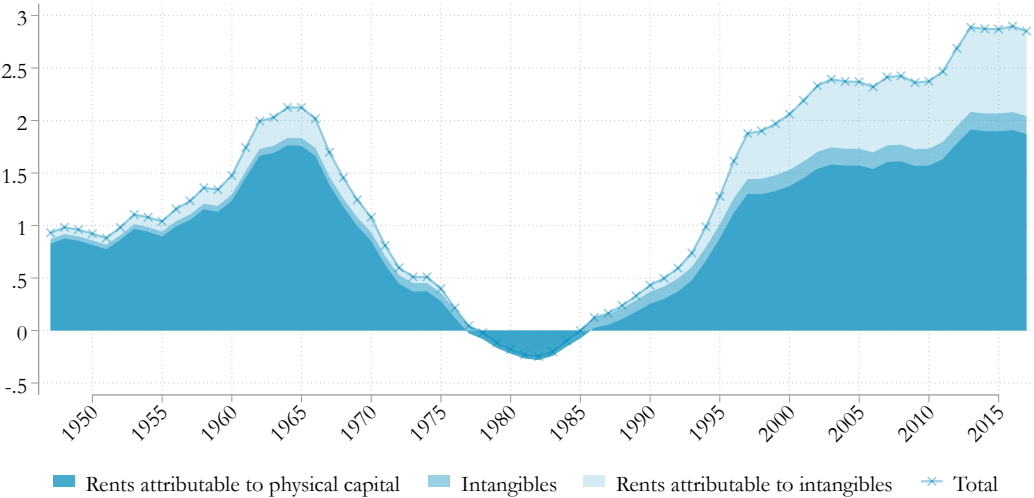
2015 rents as a fraction of value added



Netting out all financial assets (Hall, 2001)

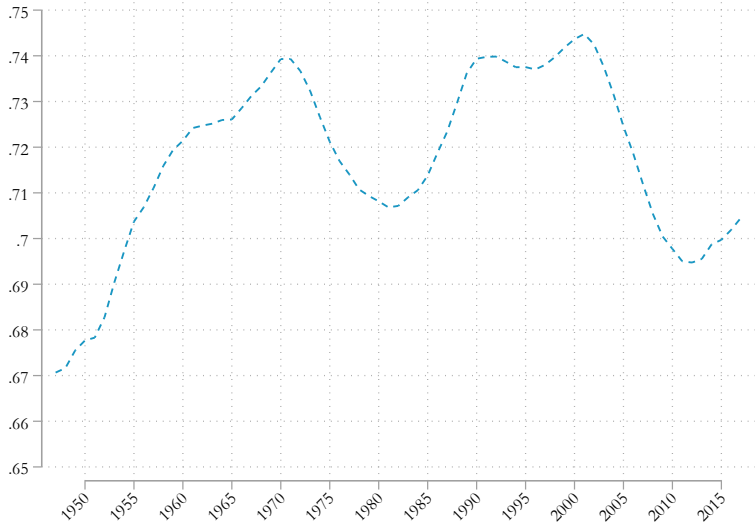


Matching the PD ratio



Implications for the labor share (1/2)

Value of $1-\alpha$ implied by the model when matching the labor share

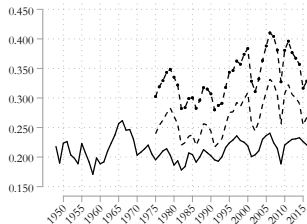


Implications for the labor share (2/2)

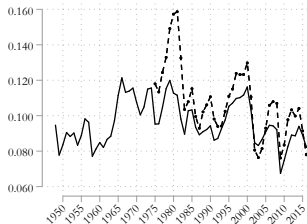
Value of the labor share implied by the model when setting $1-\alpha = 0.7$



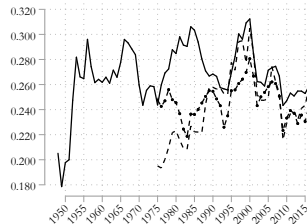
Returns to physical capital, ROA_1



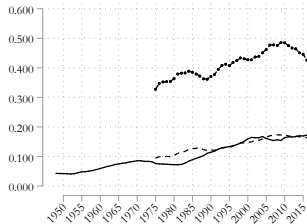
Physical investment rate, i_1



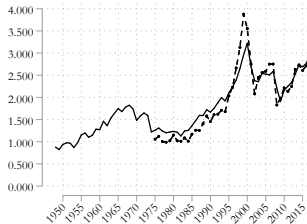
Intangible investment rate, i_2



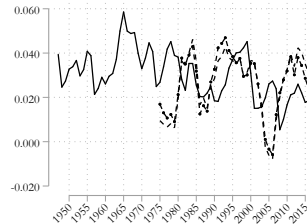
Ratio of intangible to physical capital, S



Average Tobin's Q of physical capital, Q_1



Growth rate of total capital stock, g

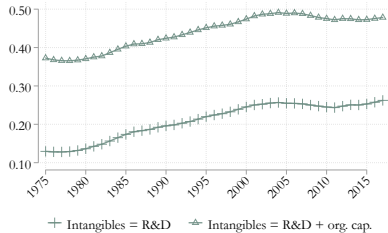


--- Compustat NF, intangibles = R&D

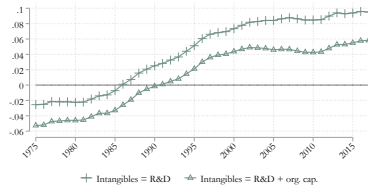
- - - Compustat NF, intan = R&D + organization capital

— NFCB

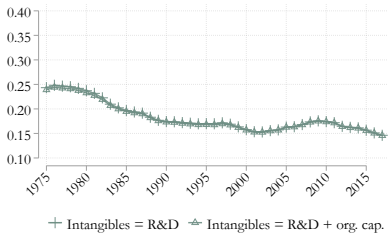
Intangible share



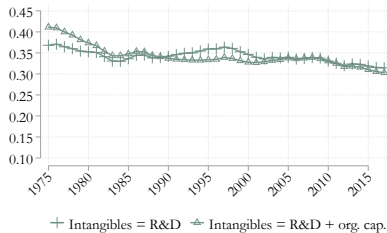
Rents as a fraction of value added



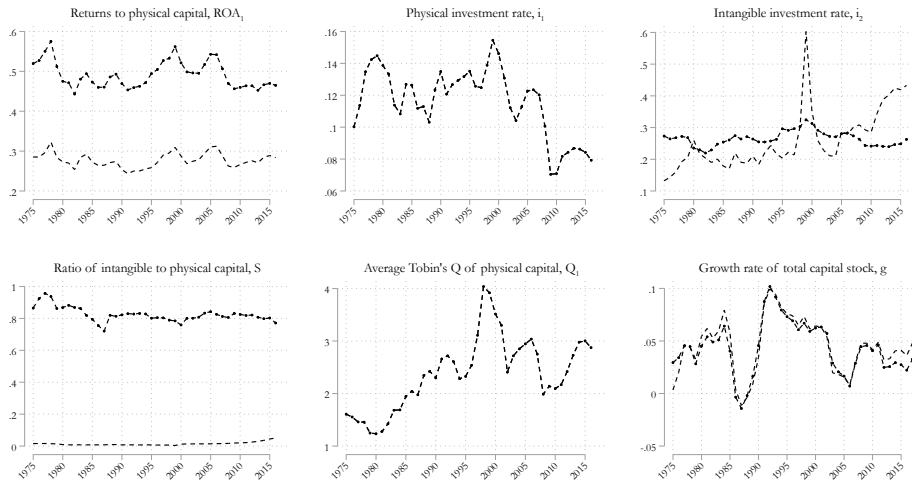
User cost of physical capital



User cost of intangible capital



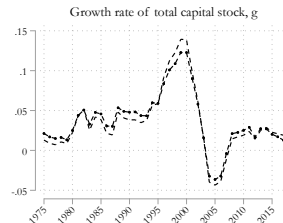
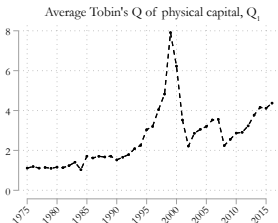
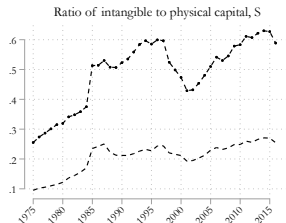
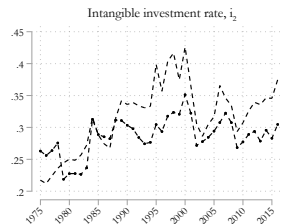
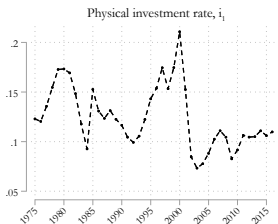
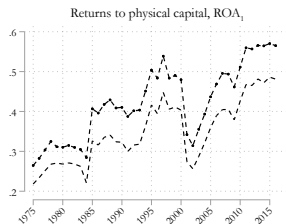
Consumer sector



--- Consumer sector, intangibles = R&D

— Consumer sector, intangibles = R&D + organization capital

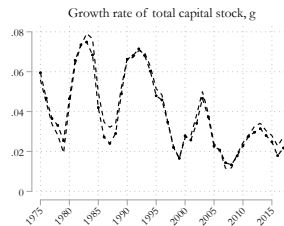
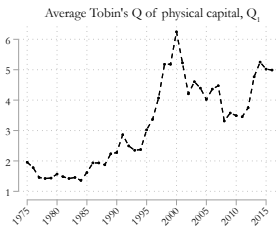
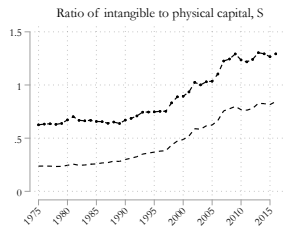
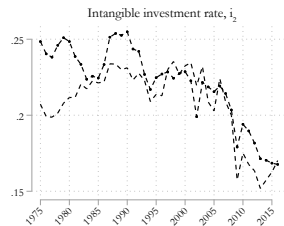
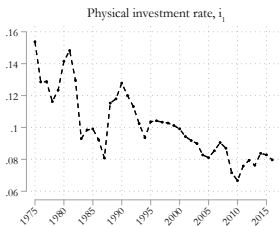
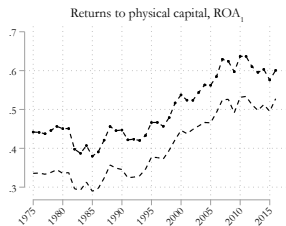
High-tech sector



-- High-tech sector, intangibles = R&D

-.- High-tech sector, intangibles = R&D + organization capital

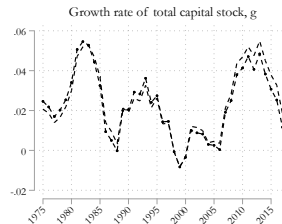
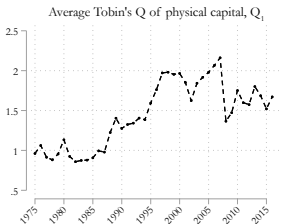
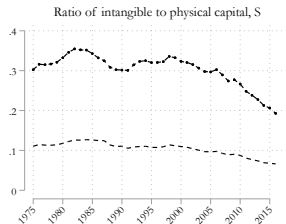
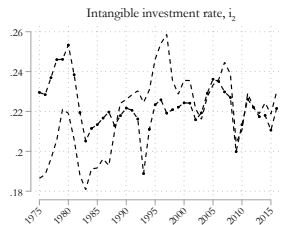
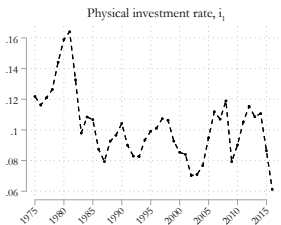
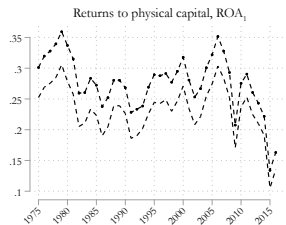
Healthcare sector



-- Healthcare sector, intangibles = R&D

-- Healthcare sector, intangibles = R&D + organization capital

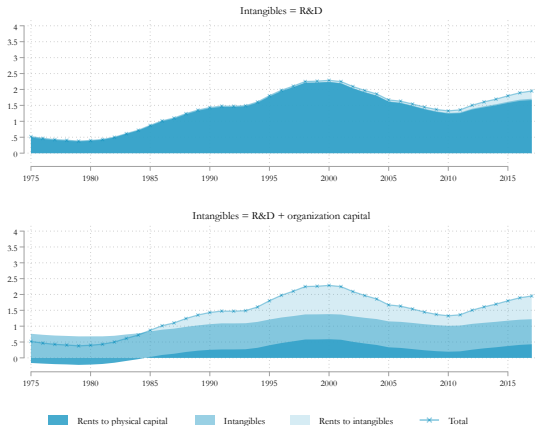
Manufacturing sector



-- Manufacturing sector, intangibles = R&D

— Manufacturing sector, intangibles = R&D + organization capital

The consumer sector: intangibles or rents?



- organization capital: no discernible **trend**, but high **level**
- still, including organization capital $\Rightarrow$ smaller markup trend after 1985