

# Spin Dynamics and Pairing in Iron Superconductors from DMFT perspective

RUTGERS  
THE STATE UNIVERSITY  
OF NEW JERSEY

Kristjan Haule



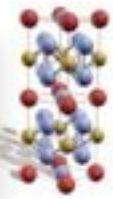
Support:



ACS  
Chemistry for Life™

Boston, 2013

# Work mainly contributed by



Zhiping Yin,  
(Rutgers)



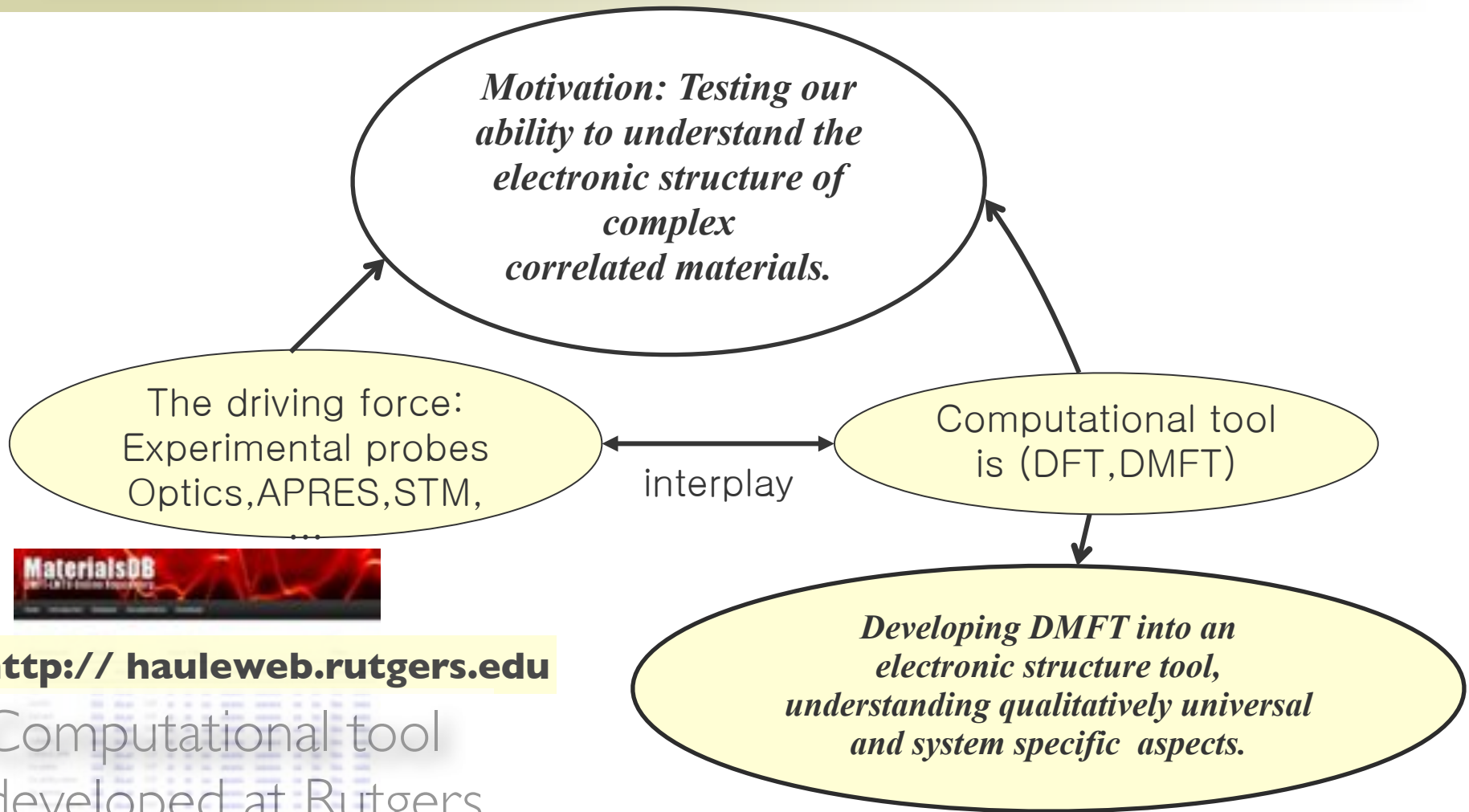
G. Kotliar  
(Rutgers)



Hyowon Park:  
(Columbia)



# Building Computational Theoretical Tools



[http:// hauleweb.rutgers.edu](http://hauleweb.rutgers.edu)

Computational tool  
developed at Rutgers

Wien2K+DMFT

multiorbital CTQMC, full potential basis, charge self-consistent.

Thermoelectricity in FeSi as Hunds semiconductors

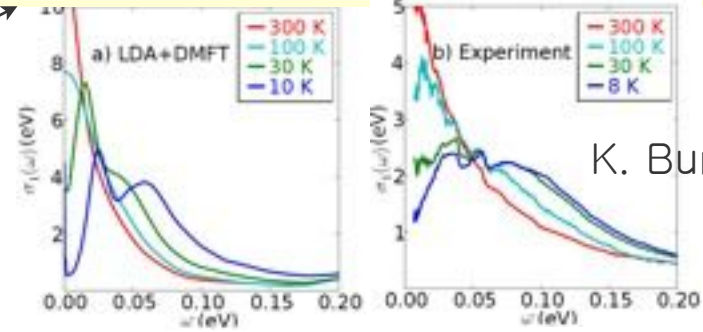
J. Tomczak, KH, G. Kotliar, PNAS (2012)

MIT in FeO

K. Ohta, R. Cohen, KH, PRL (2012)

Protracted screening and multiple hybridization Gaps in Ce115's.

J.H. Shim, KH, G. Kotliar, Science 318. 1615 (2007)

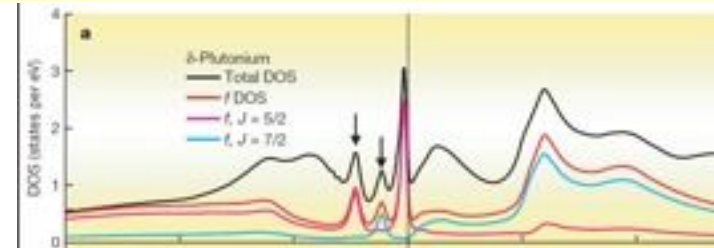


K. Burch et.al.

Computational tools allow to identify system specific fingerprints which give us confidence in our understanding of correlated electron materials

Quasiparticle multiplets in Plutonium and its Compounds.

J.H. Shim, KH, G. Kotliar, Nature 446, 513 (2007).



Strength of correlations in e and h doped cuprates.

C Weber, KH, G. Kotliar, Nature Physics 10, 1038 (2010)

Hidden Order in URu2Si2. Kondo effect and hexadecapole order.

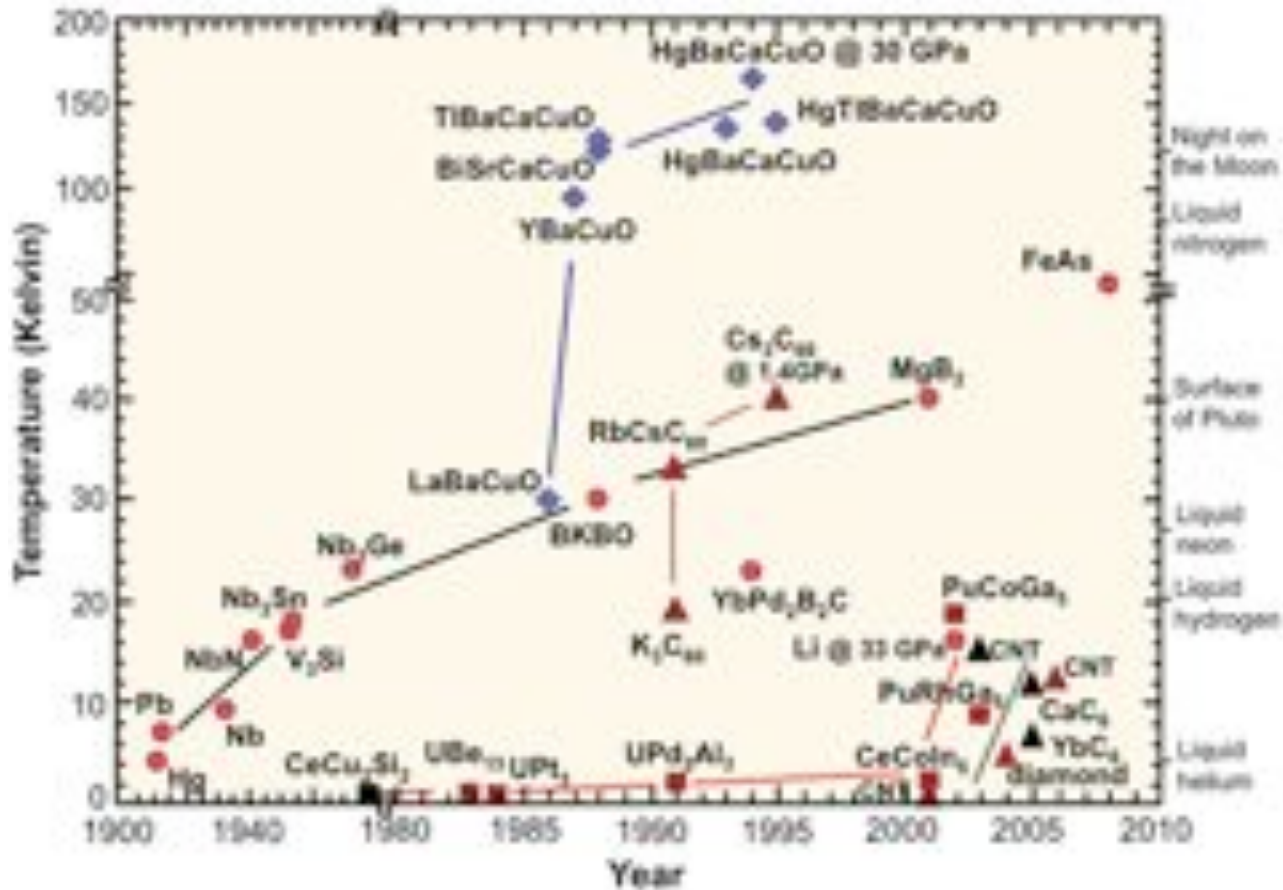
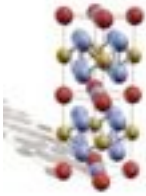
KH, G. Kotliar, Nature Physics 5, 796 - 799 (2009).

Magnetism and Charge Dynamics in Iron Pnictides.

Z. P. Yin, KH, G. Kotliar, Nature Physics (2011)

Z. P. Yin, KH, G. Kotliar, Nature Materials (2011)

# High temperature superconductors

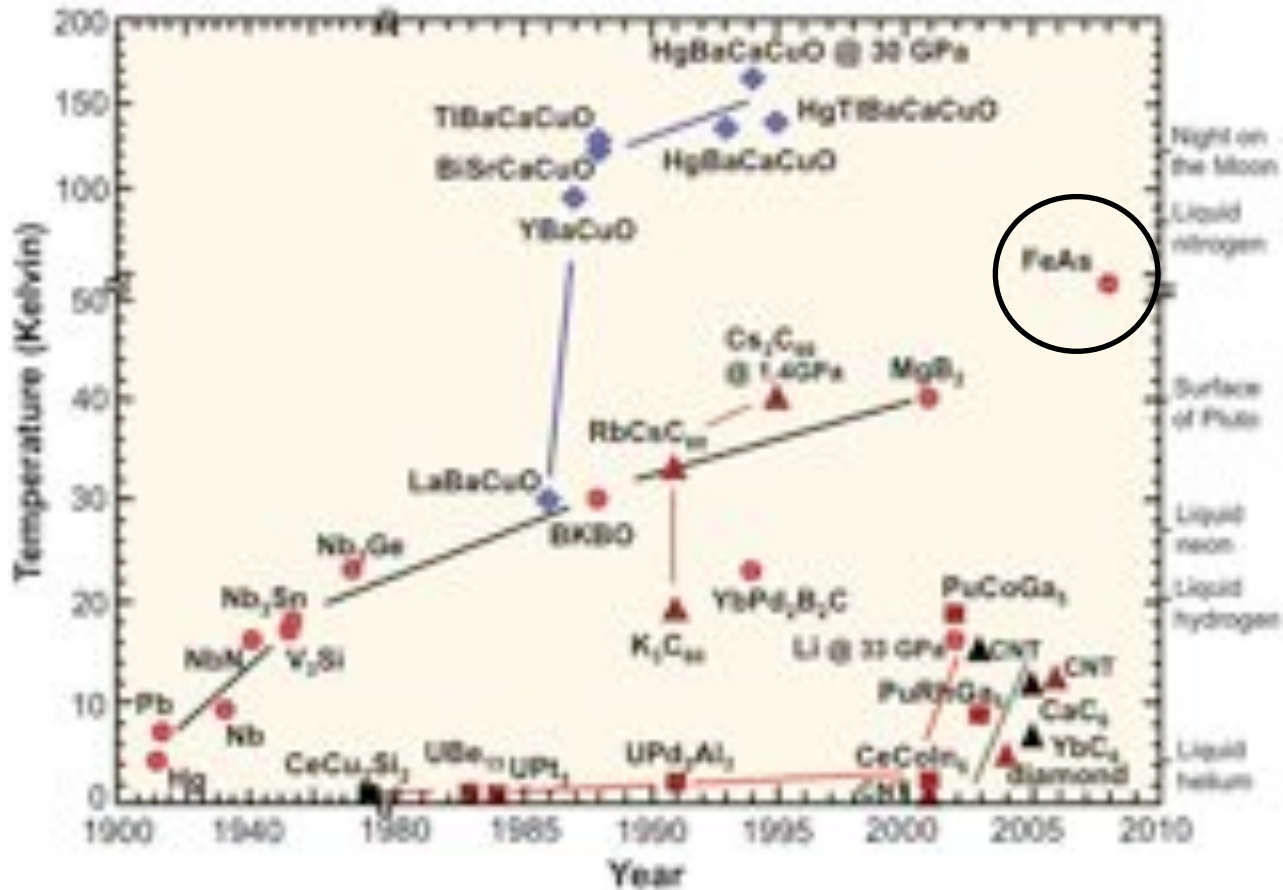
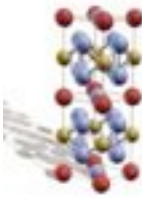


H. Hosono



Reenergize  
high-T<sub>c</sub> field

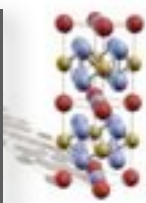
# High temperature superconductors



H. Hosono

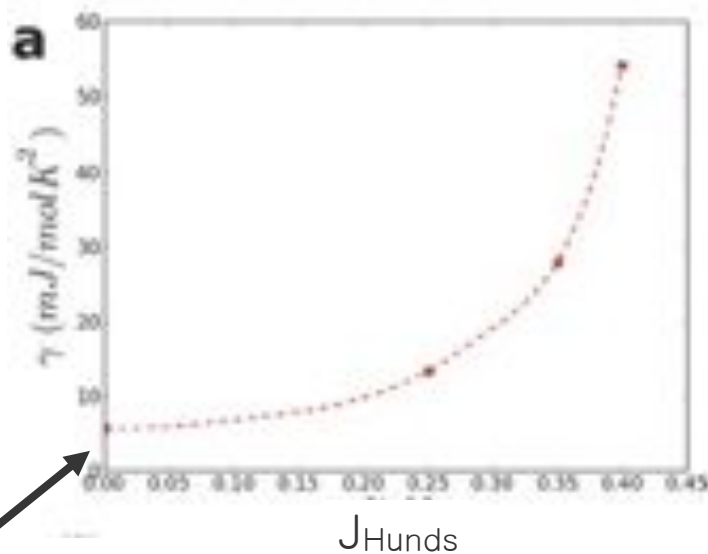


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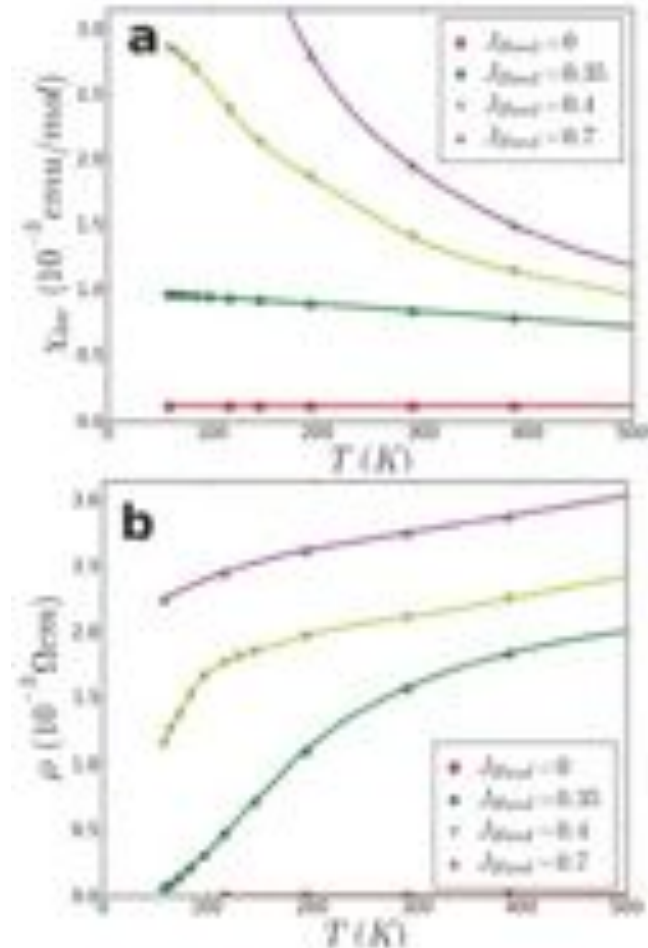
# Importance of Hund's rule in pnictides: **Hunds Metals**

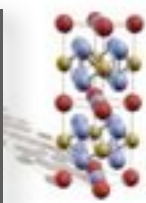
Significant Correlations in pnictides:  
effective mass 3–5 band mass  
KH, J.H. Shim, and G. Kotliar, PRL 100, 226402 (2008)



LDA value

For  $J=0$  there is negligible mass enhancement at  $U \sim W$ !





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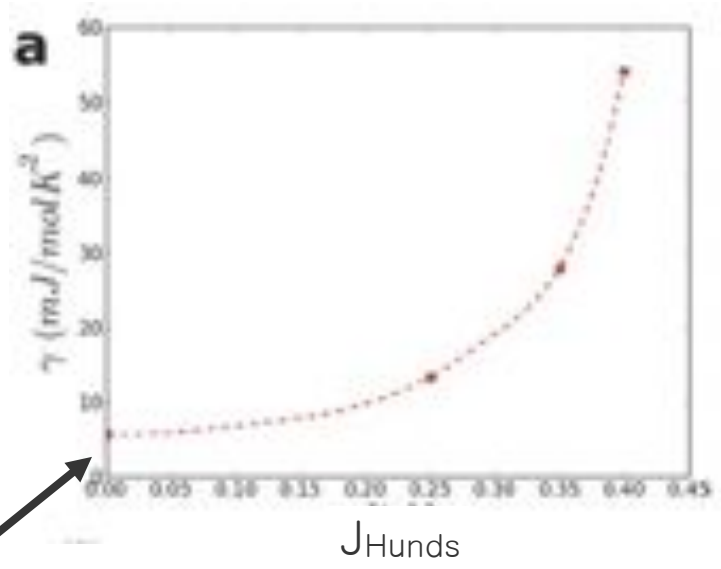
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Hubbard U not important

The **Hund's coupling** brings correlations!

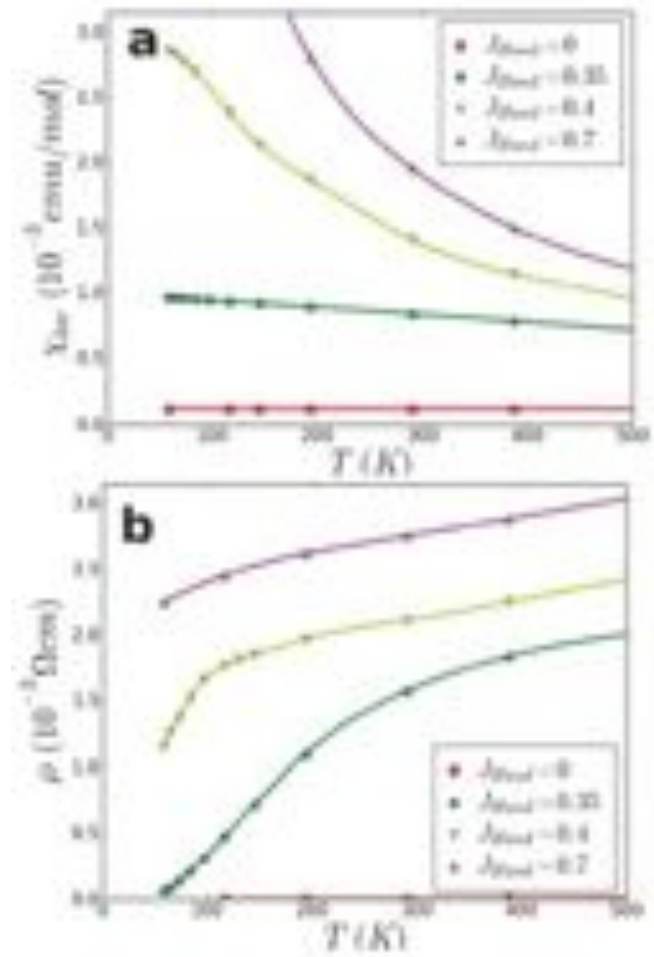
KH, G. Kotliar, arXiv:0805.0722

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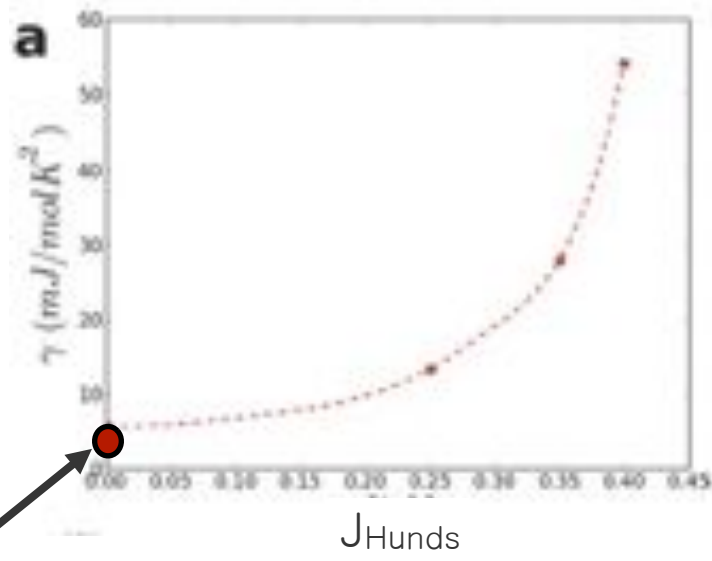
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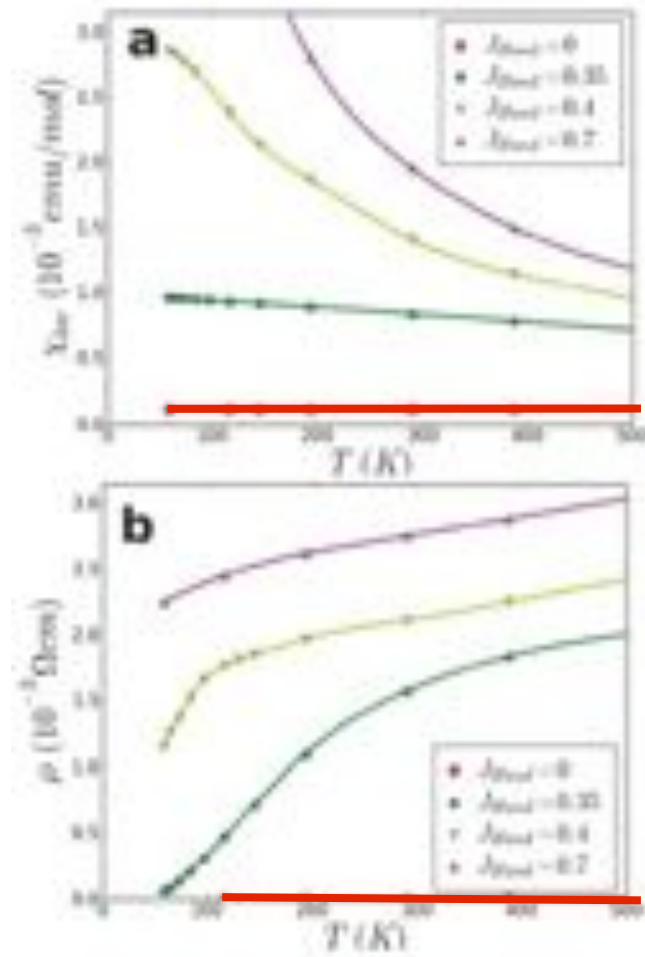
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**J=0**



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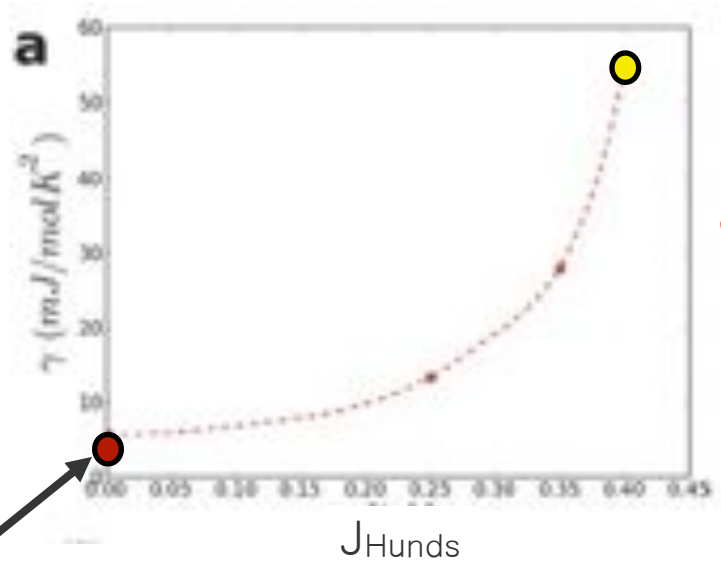
KH, J.H. Shim, and G. Kotliar, PRL 100, 226402 (2008)

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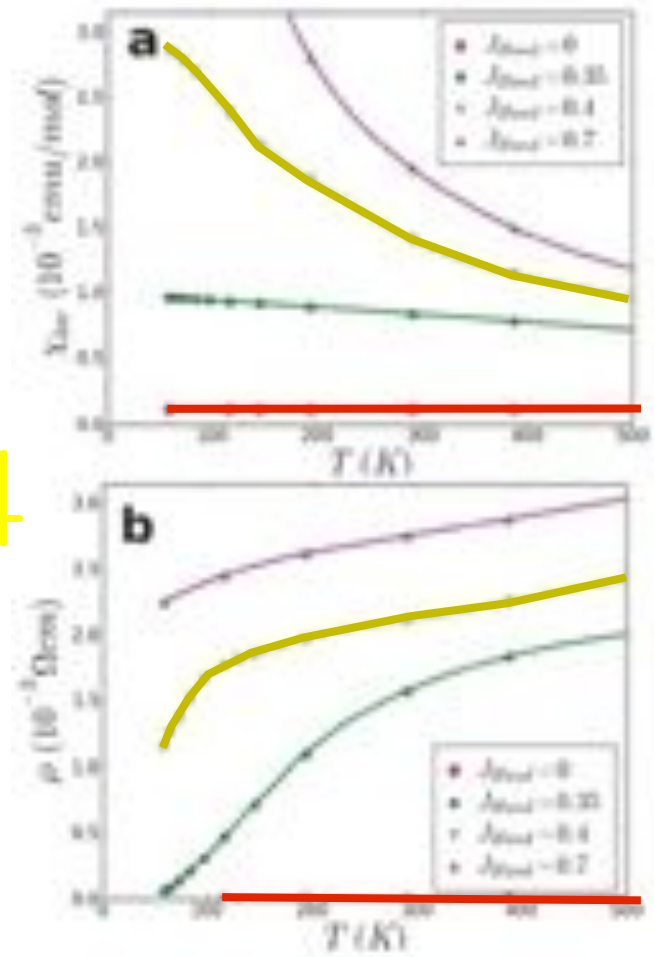
The **Hund's coupling** brings correlations!

KH, G. Kotliar, arXiv:0805.0722

New Journal of Physics, 11 025021 (2009).



J=0.4

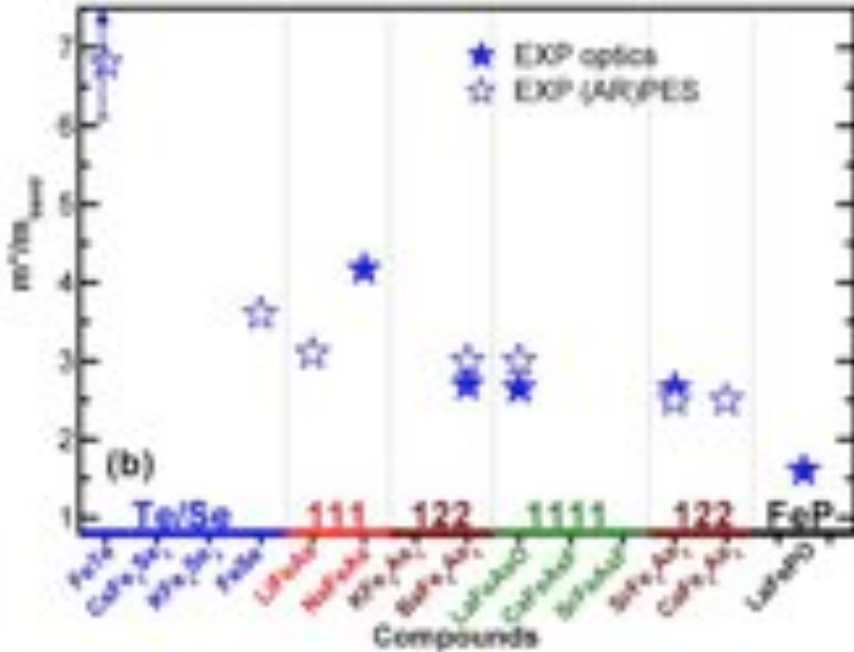


LDA value

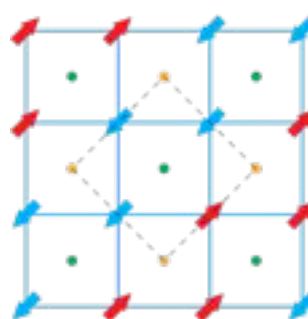
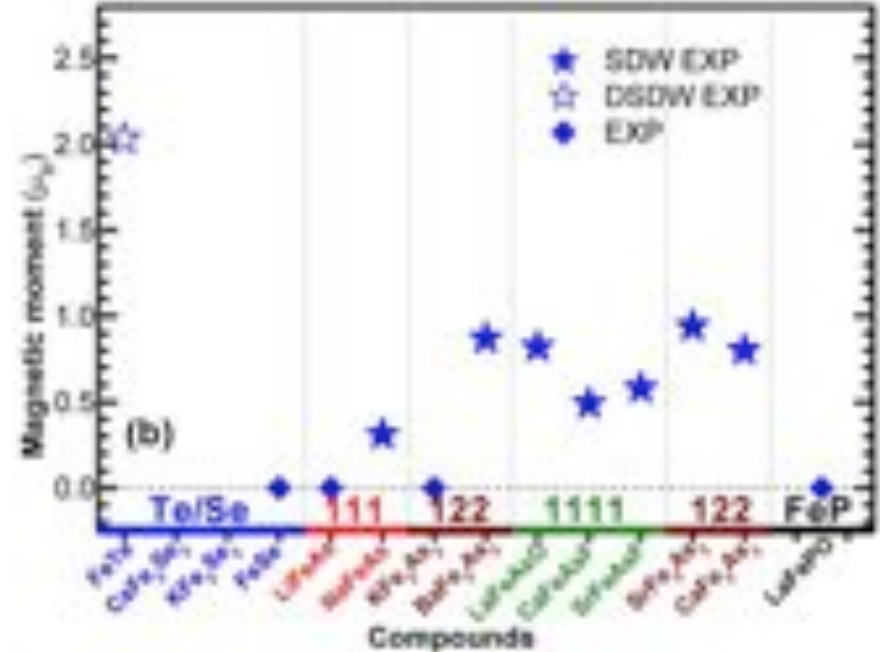
For J=0 there is negligible mass enhancement at U~W!

# All FeSCs share the same FePn layer, but there are large variations among them.

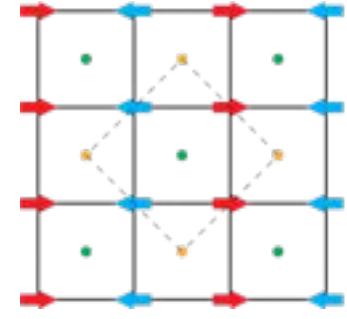
Mass enhancement in the PM phase.



Magnetic moment in the ordered phases.



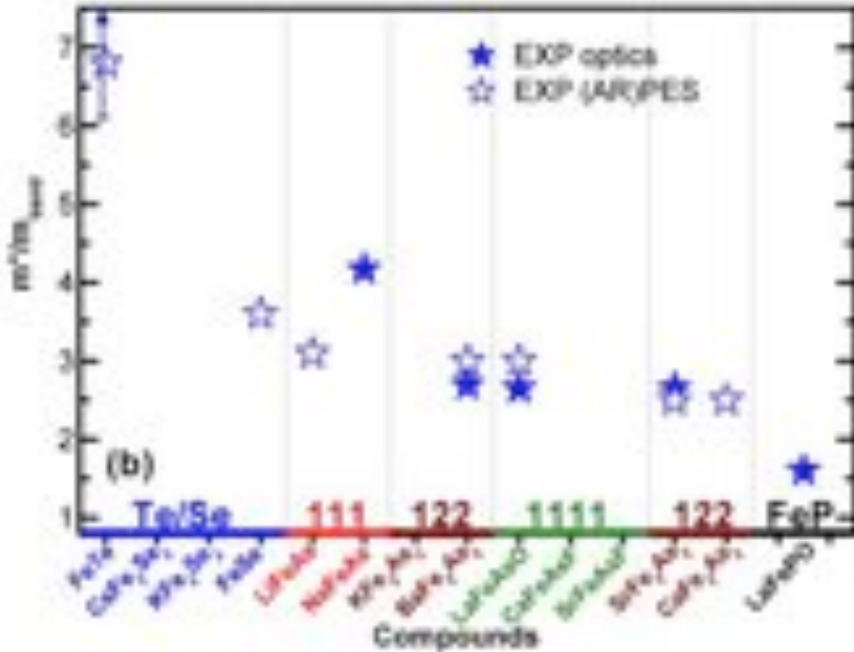
DSDW



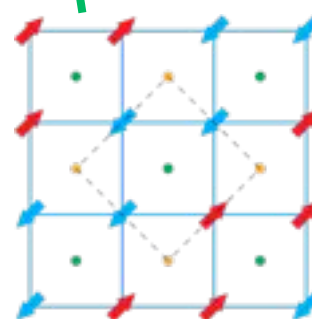
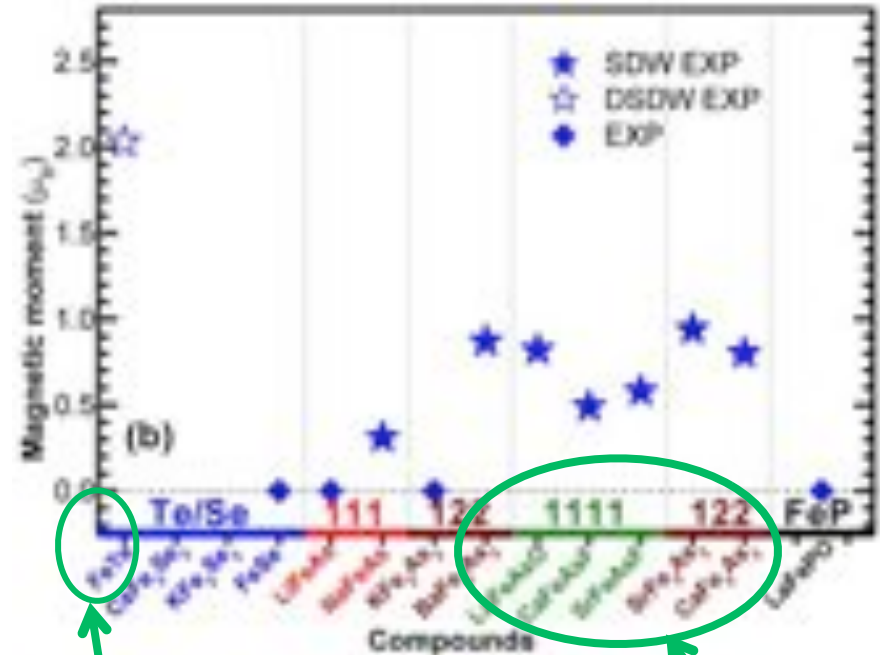
SDW

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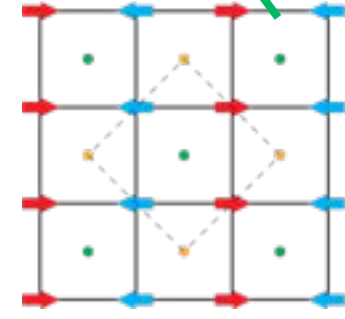
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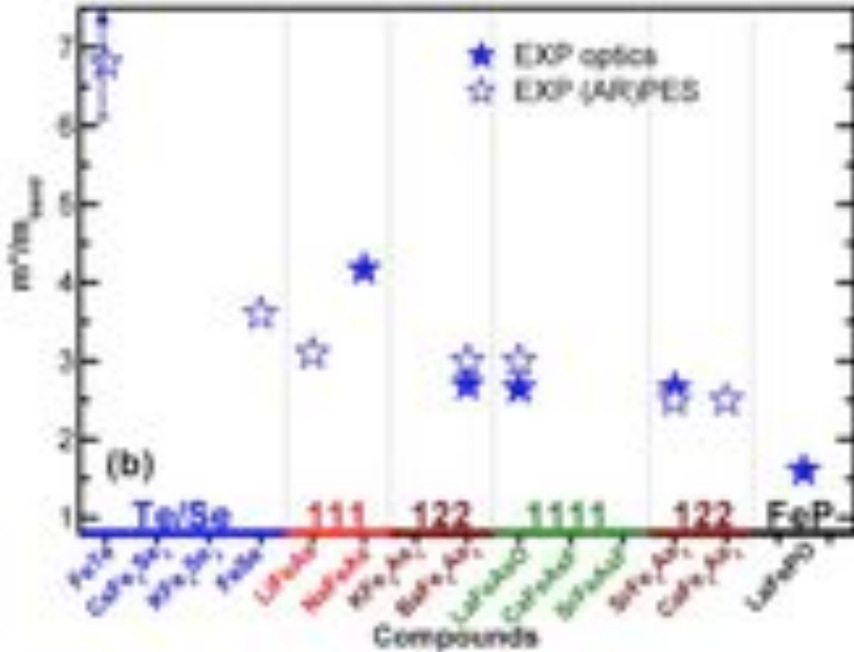
DSDW



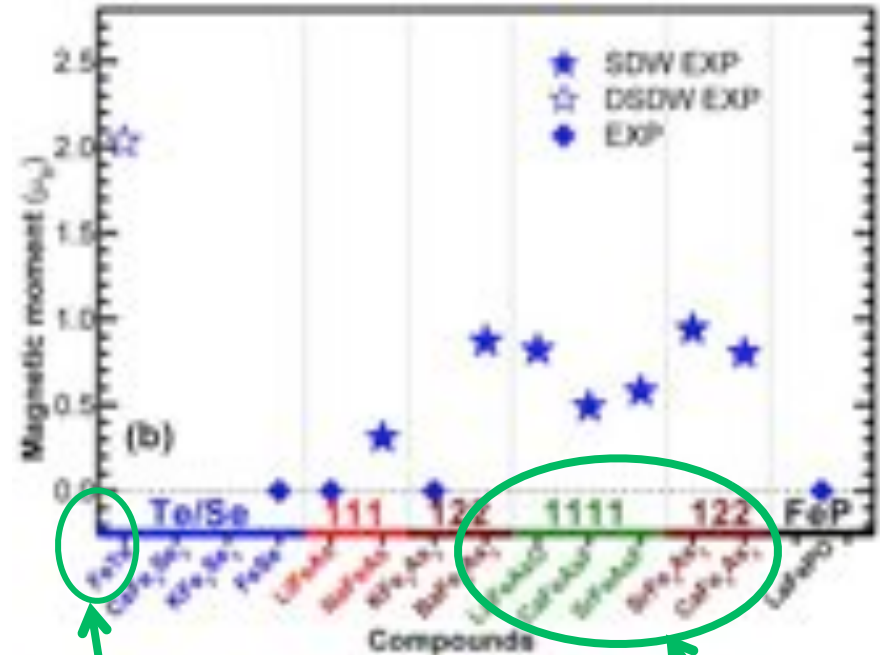
SDW

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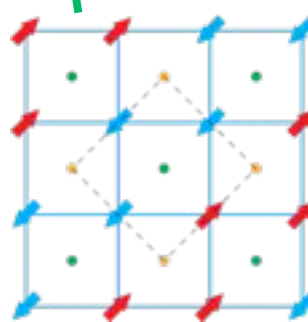
Mass enhancement in the PM phase.



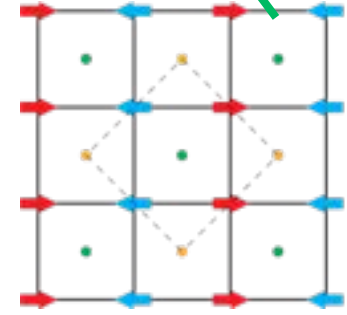
Magnetic moment in the ordered phases.



Neither the local picture nor the itinerant picture can fully describe them.



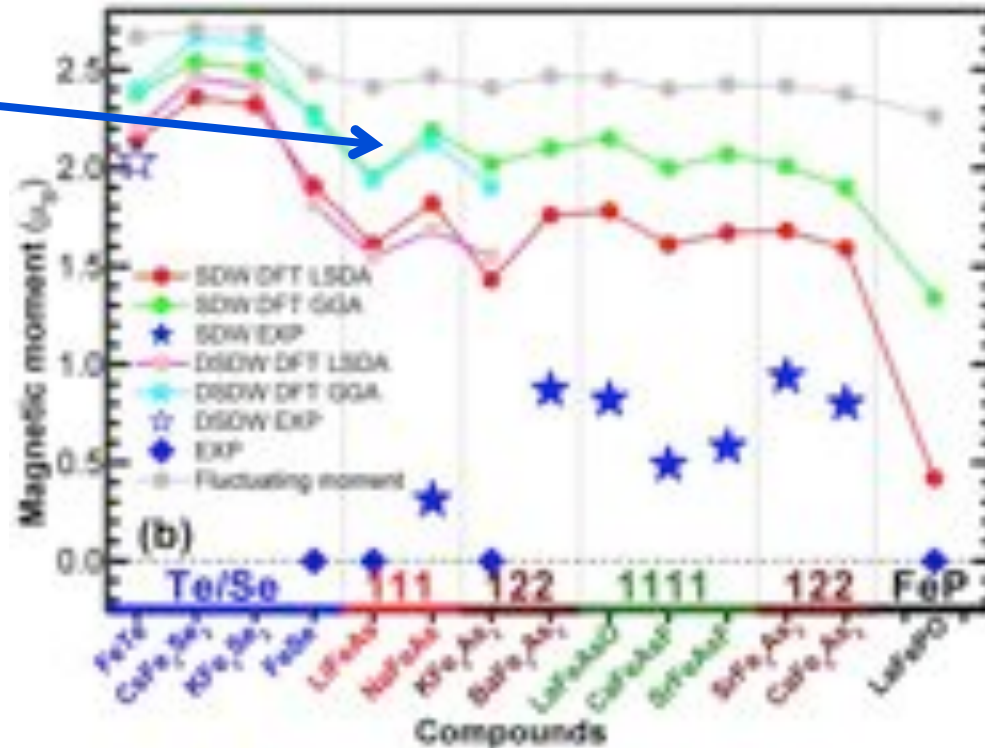
DSDW



SDW

# Moments and Magnetism

Moments by DFT are around  $2 \mu_B$ , overestimated by a factor of two (ZPY et al, PRL **101**, 047001 (2008).)



Experimental moment ( $\mu_B$ ):

- FeTe: 2.03, W. Bao et al., PRL **102**, 247001 (2009).
- NaFeAs: 0.31, L. Ma et al., PRB **83**, 132501 (2011).
- Ba122: 0.87, Q. Huang et al., PRL **101**, 257003 (2008).
- LaFeAsO: 0.82, H.-F. Li et al., PRB **82**, 064409 (2010).
- CaFeAsF: 0.49, Y. Xiao et al., PRB **79**, 060504(R) (2009).
- SrFeAsF: 0.58, Y. Xiao et al., PRB **81**, 094523 (2010).
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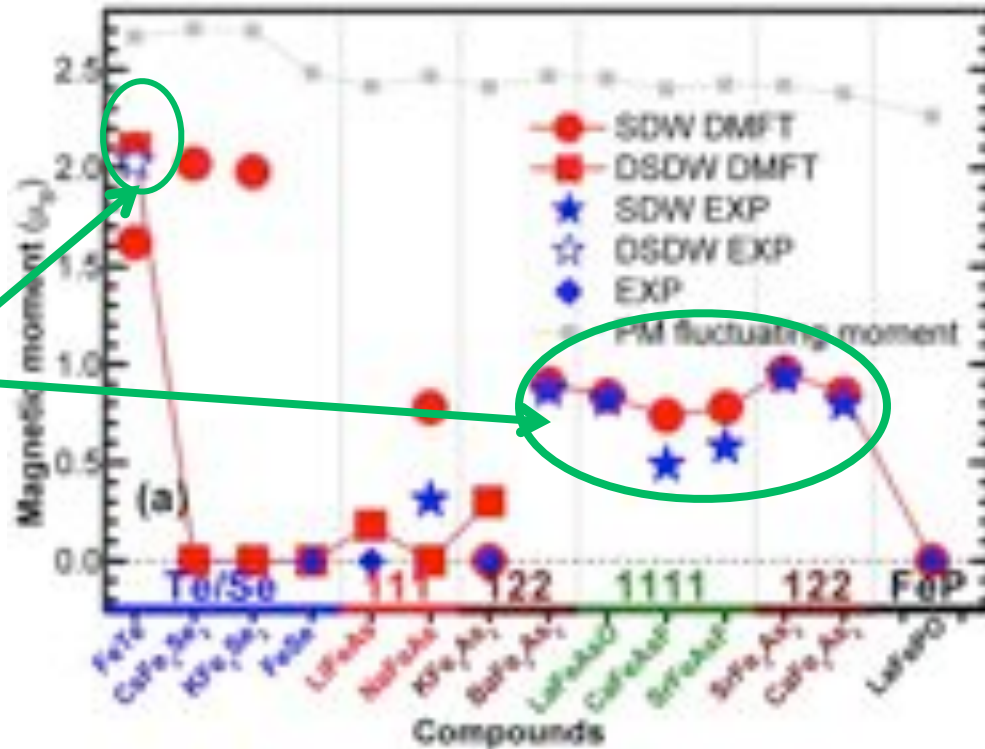
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Moments by DFT+DMFT are in good agreement with experiments

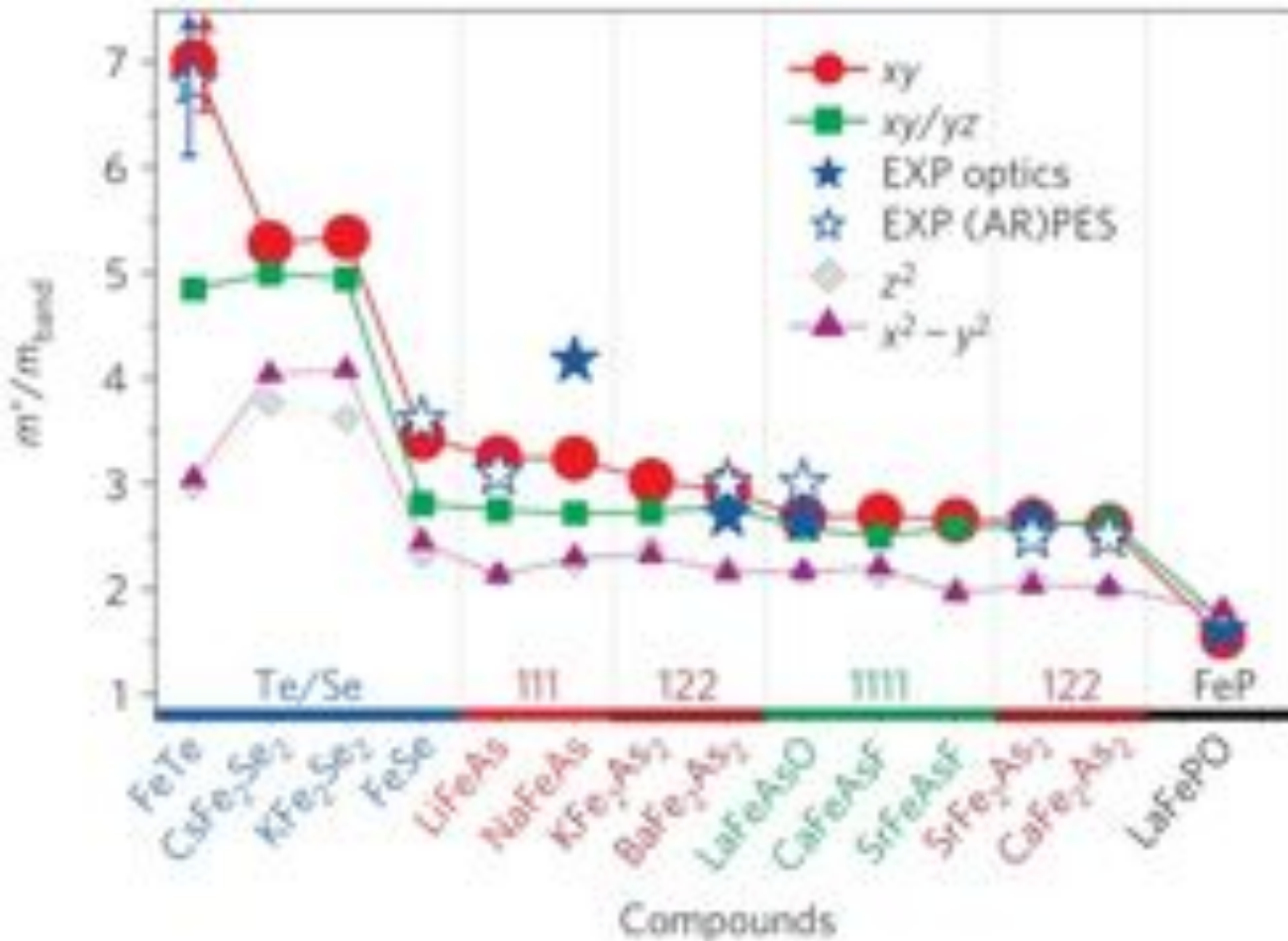
Theory  
ZPY, K. Haule and G. Kotliar, Nature Materials **10**, 932 (2011).

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# Mass enhancement

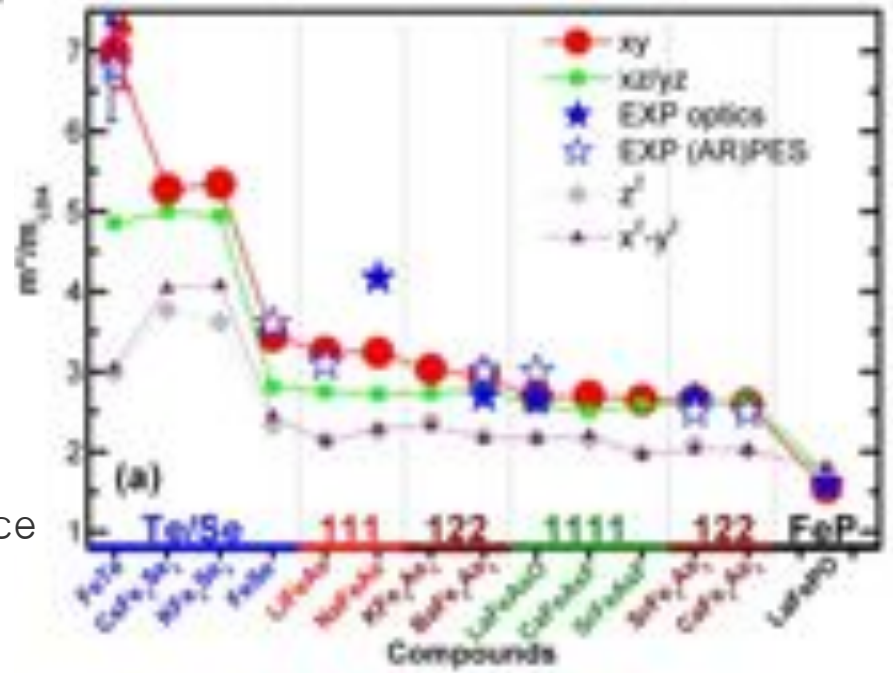
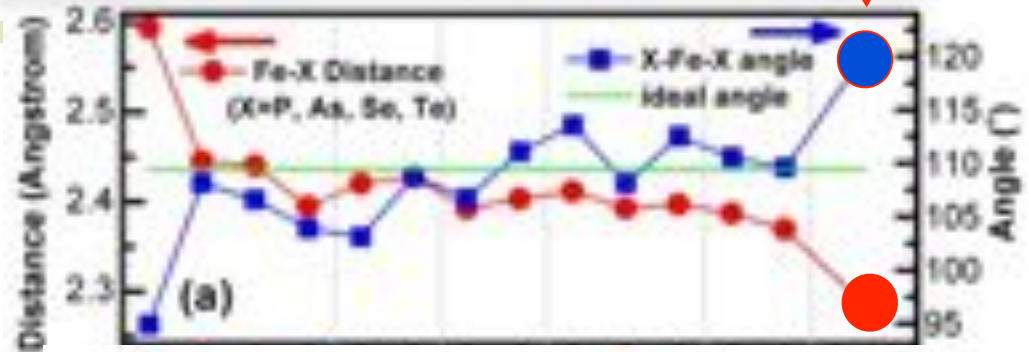
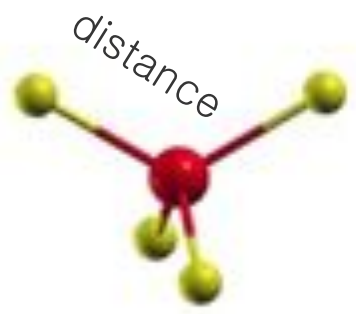
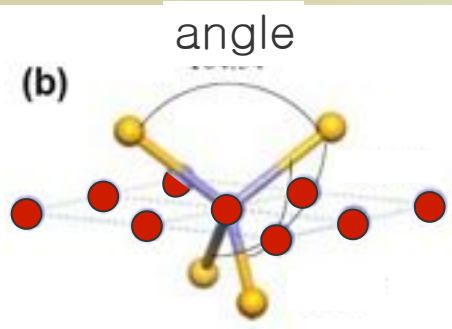


ZPY, K. Haule and G. Kotliar,  
 Nature Materials **10**, 932 (2011).

DFT+DMFT accounts for the variations in all families  
 without tuning parameter (U or J)!



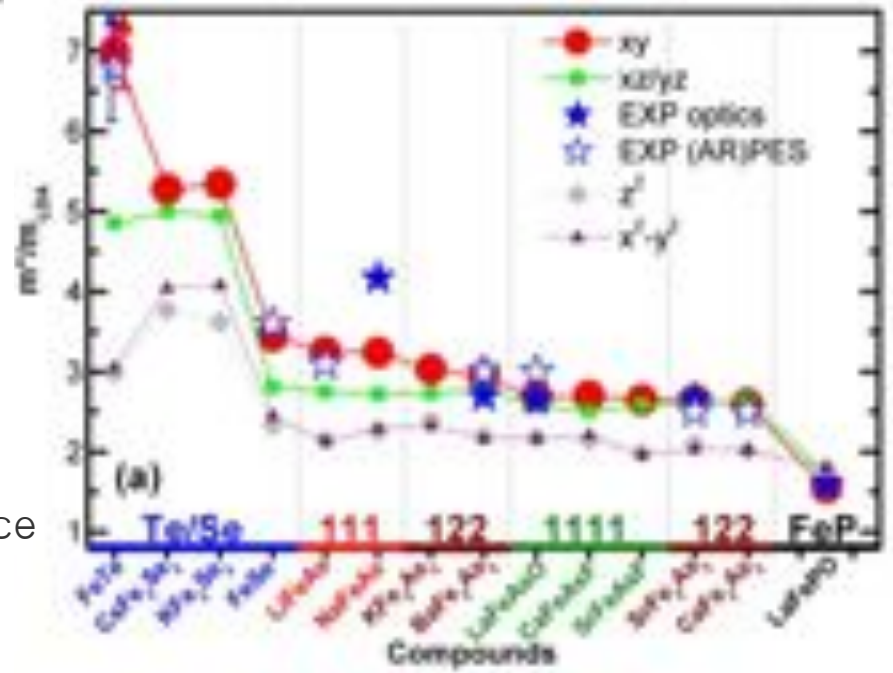
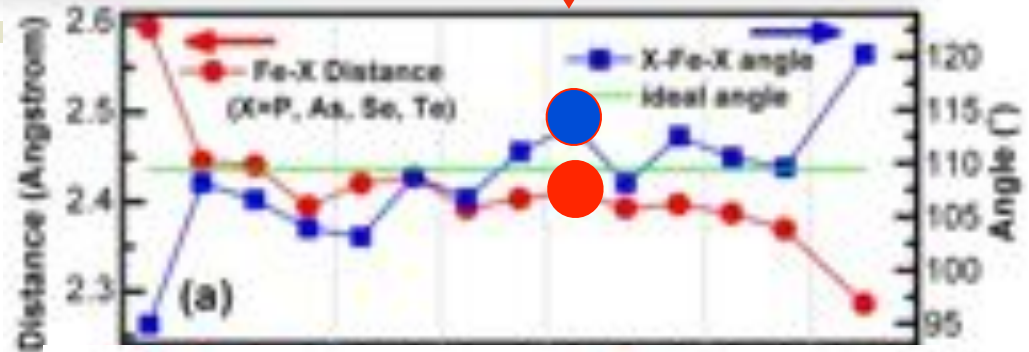
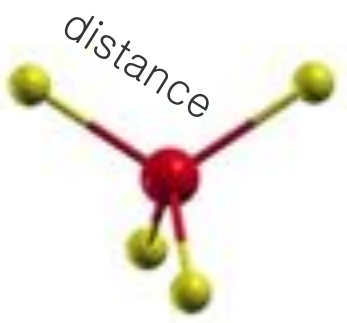
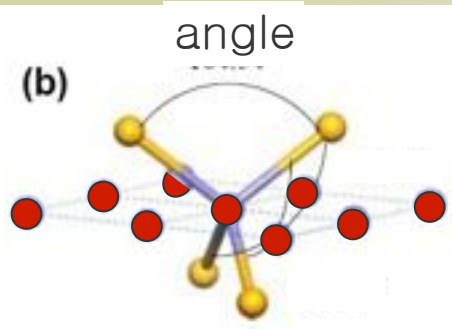
# Strength of correlations



Overall trend consistent with Fe-As distance

Hybridization with pnictogen

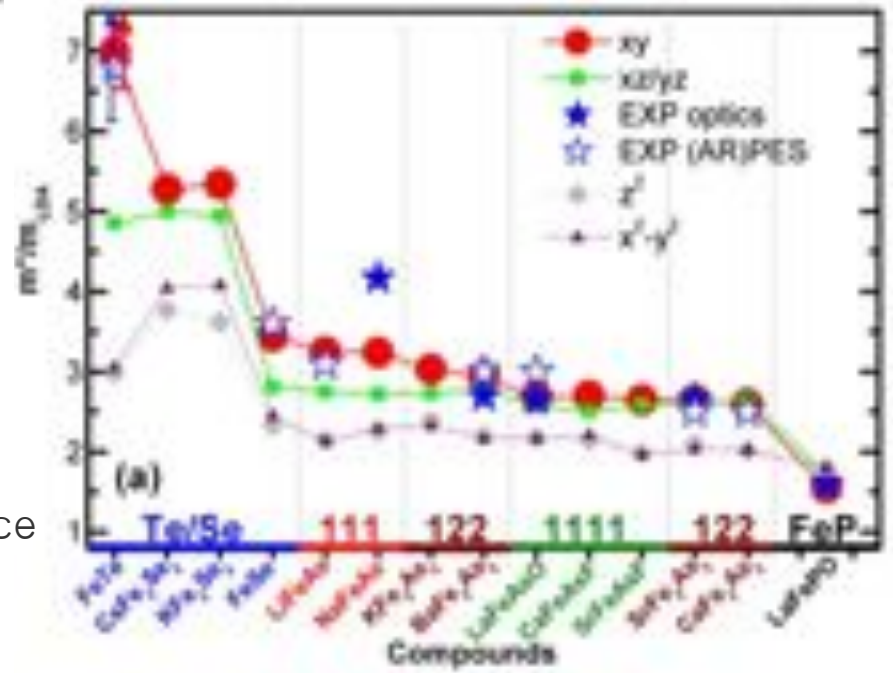
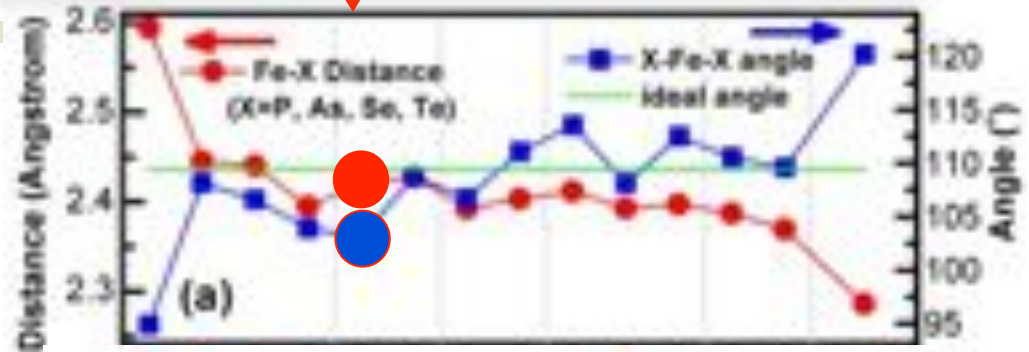
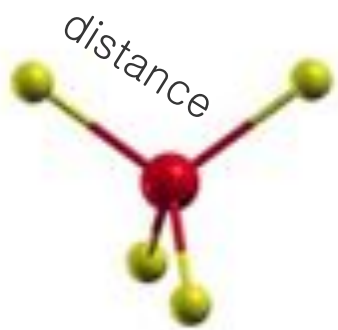
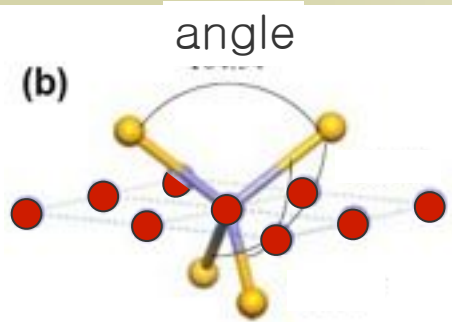
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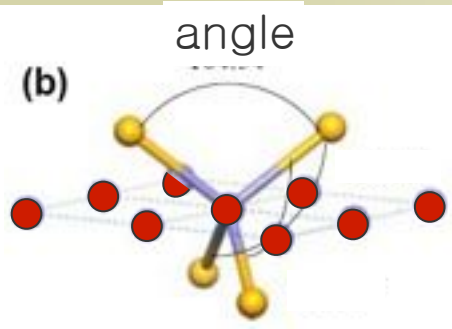
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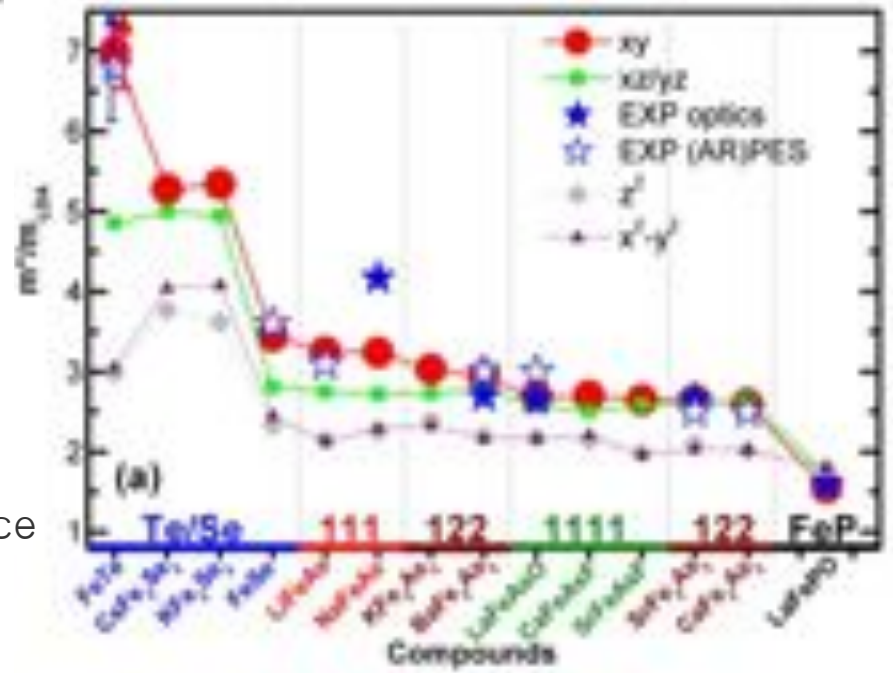
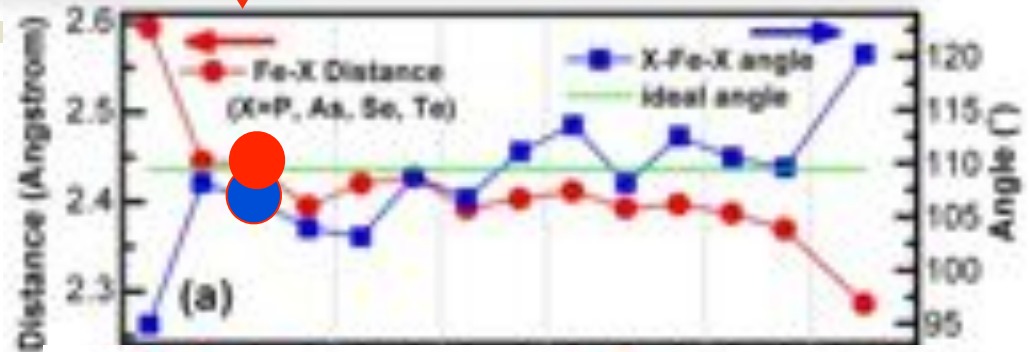
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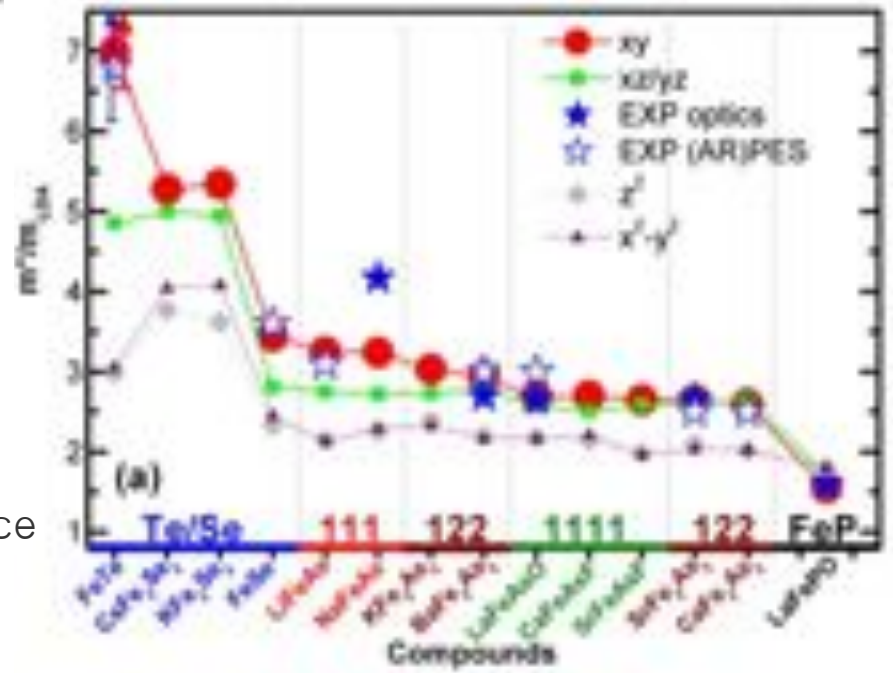
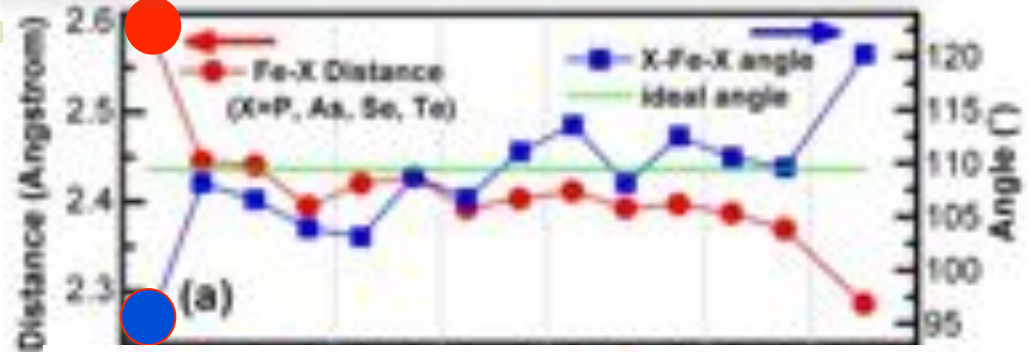
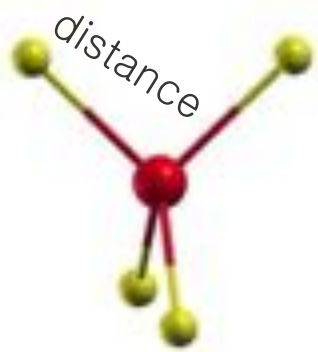
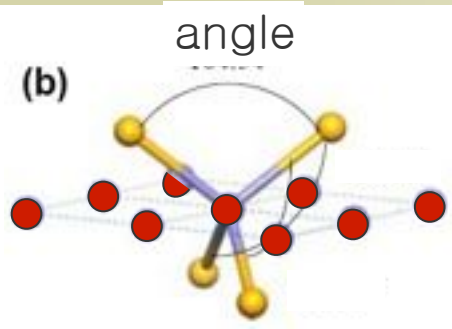
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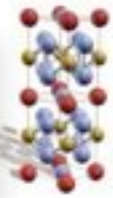
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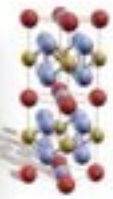
Hybridization with pnictogen

# Two particle response of Hund's metals: Dynamical structure factor



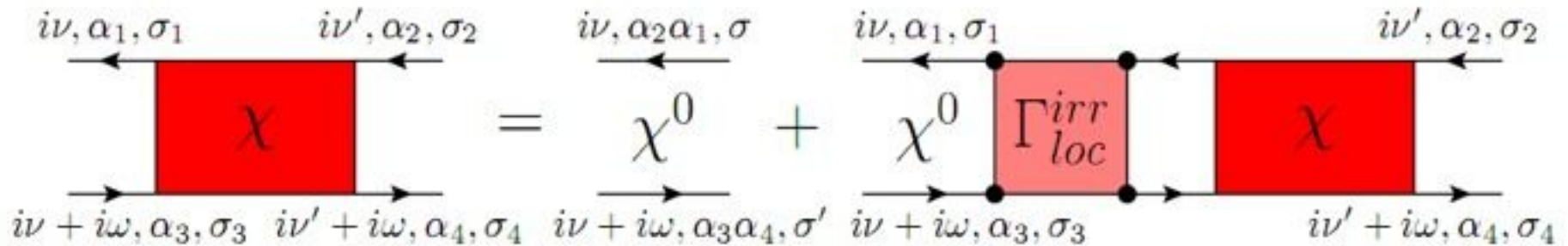
$$S(\mathbf{q}, \omega) = \frac{\chi''(\mathbf{q}, \omega)}{1 - e^{-\hbar\omega/k_B T}}$$

# Two particle response of Hund's metals: Dynamical structure factor



$$S(\mathbf{q}, \omega) = \frac{\chi''(\mathbf{q}, \omega)}{1 - e^{-\hbar\omega/k_B T}}$$

Computed from the two particle response functions using the fact that the irreducible vertex is local.

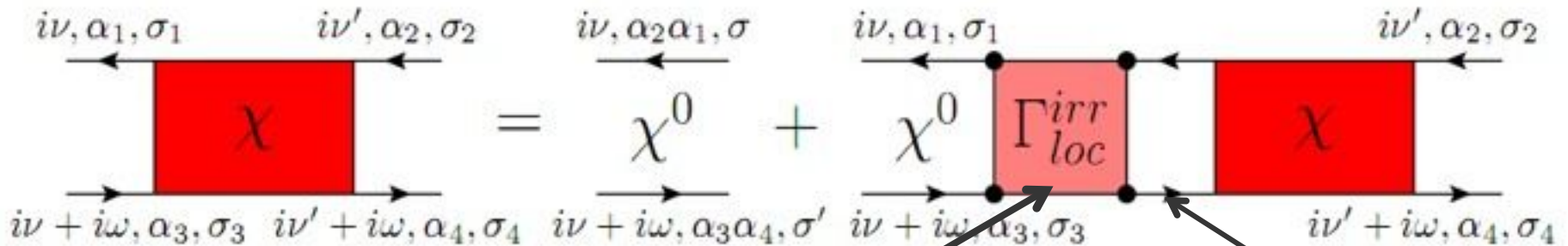


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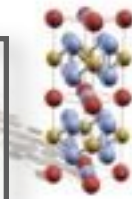


The two particle irreducible vertex function of the impurity

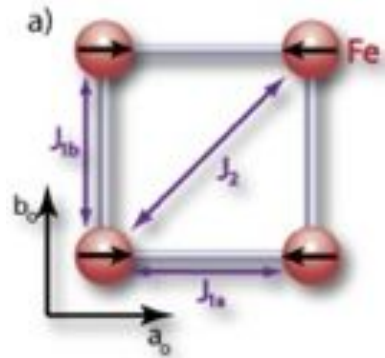
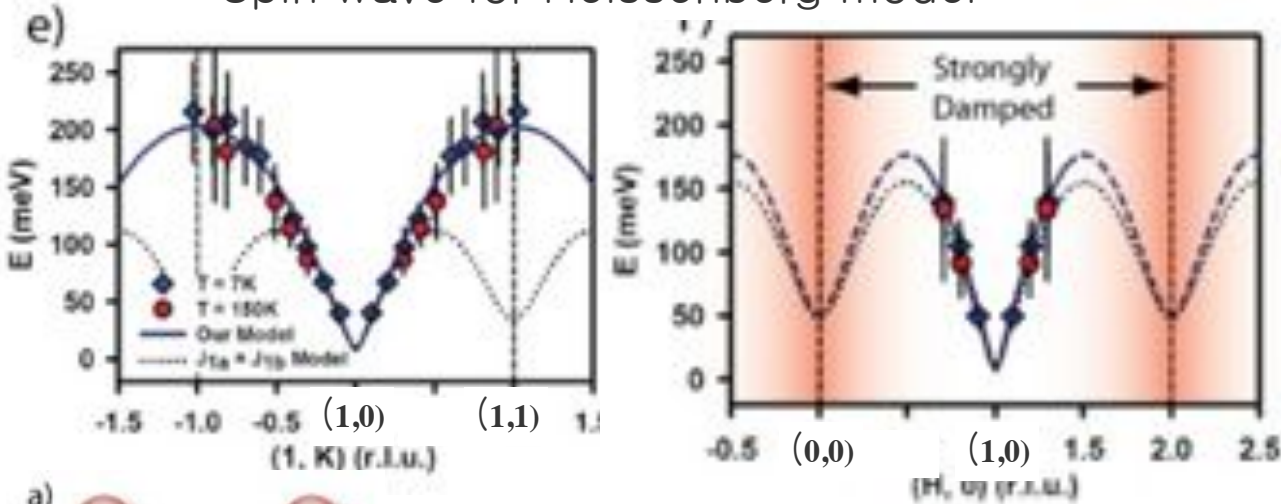
The LDA+DMFT self-consistent lattice Green's function



# Dynamical structure factor of $\text{BaFe}_2\text{As}_2$

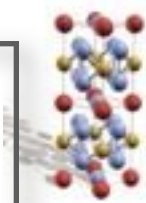


Spin wave for Heisenberg model

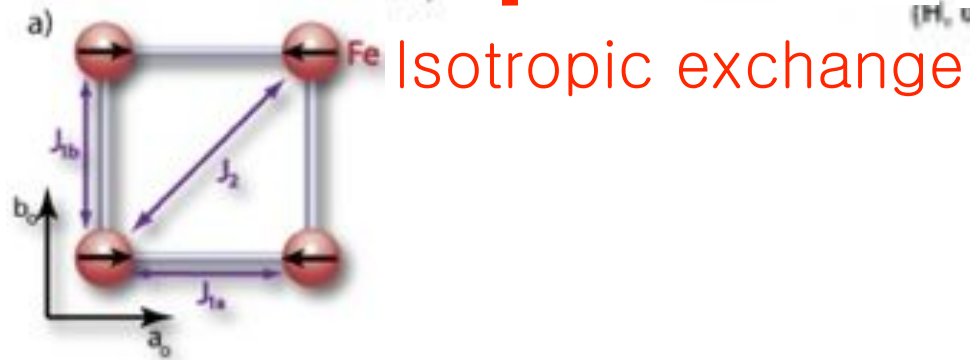
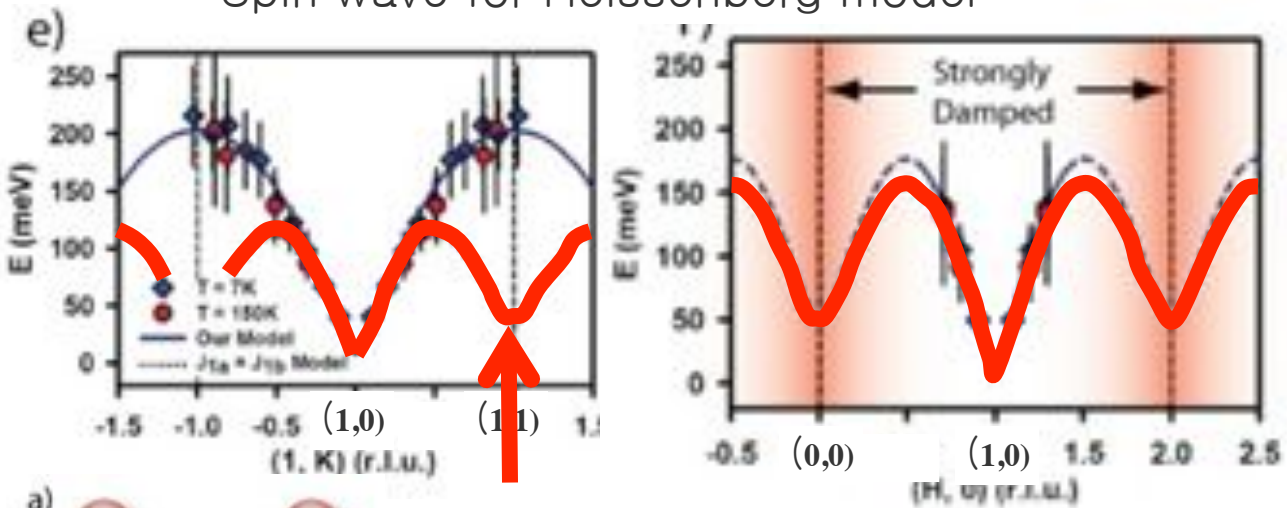


Leland W. Harriger, Pengcheng Dai et al., *PRB* 84, 054544 (2011).

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Spin wave for Heisenberg model

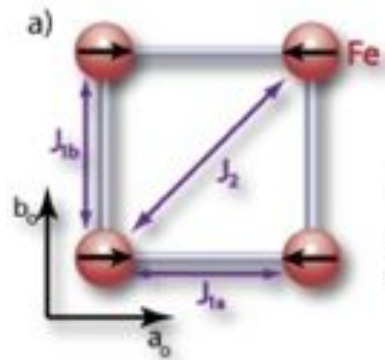
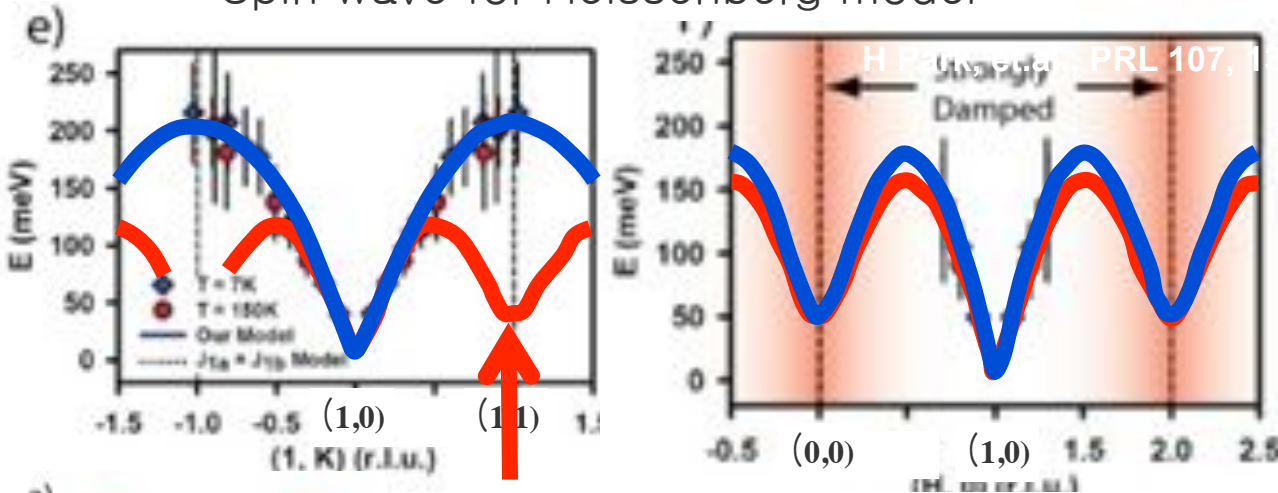


Leland W. Harriger, Pengcheng Dai et al., PRB 84, 054544 (2011).

# Dynamical structure factor of BaFe<sub>2</sub>As<sub>2</sub>



Spin wave for Heisenberg model



Very anisotropic exchange

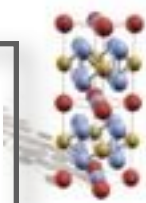
$$SJ_{1a} \approx 59.2 \text{ meV}$$

$$SJ_{1b} \approx -9.2 \text{ meV}$$

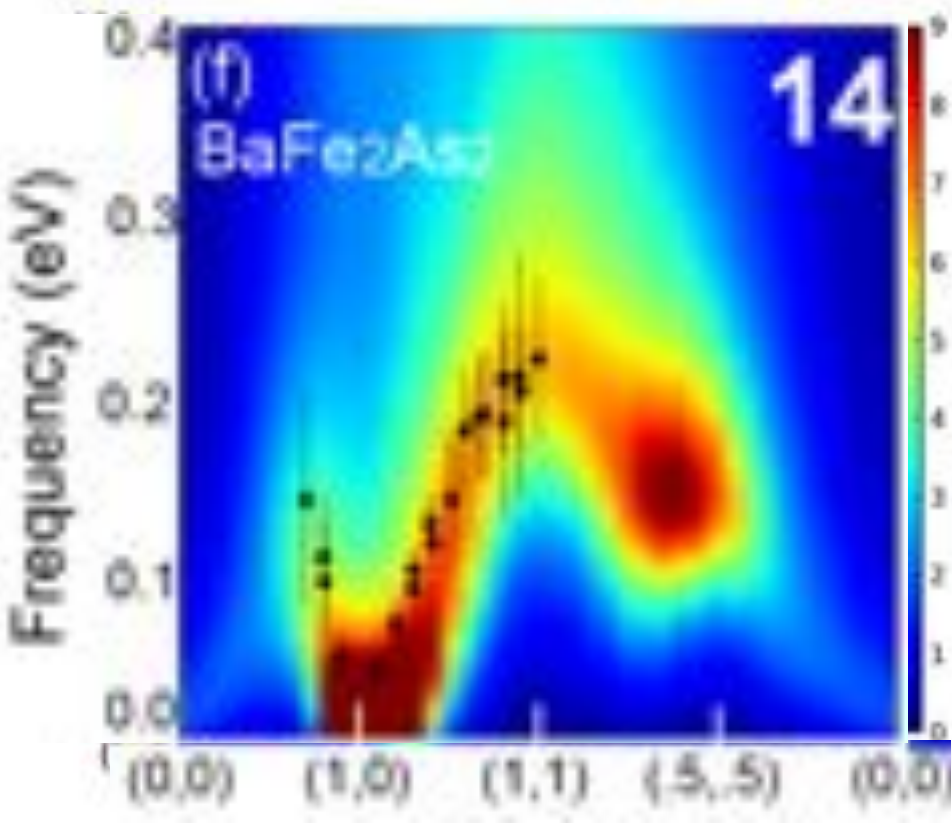
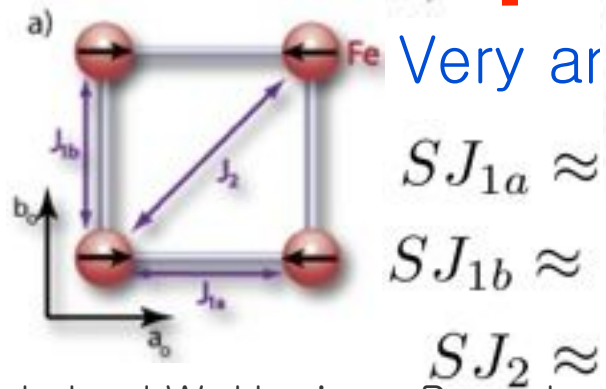
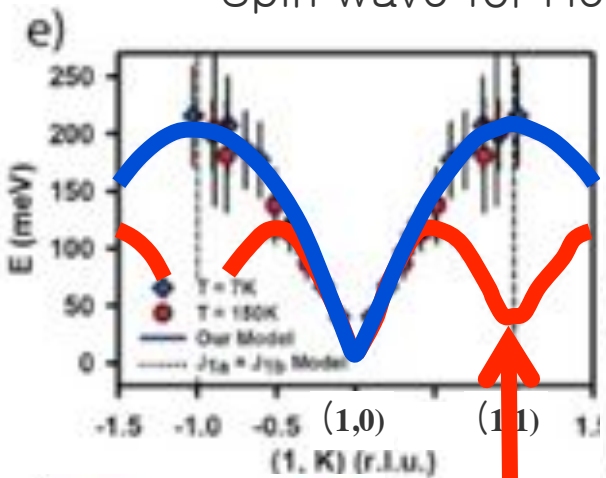
$$SJ_2 \approx 13.6 \text{ meV}$$

Leland W. Harriger, Pengcheng Dai et al., PRB 84, 054544 (2011).

# Dynamical structure factor of BaFe<sub>2</sub>As<sub>2</sub>



Spin wave for Heisenberg model

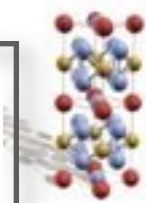


DMFT

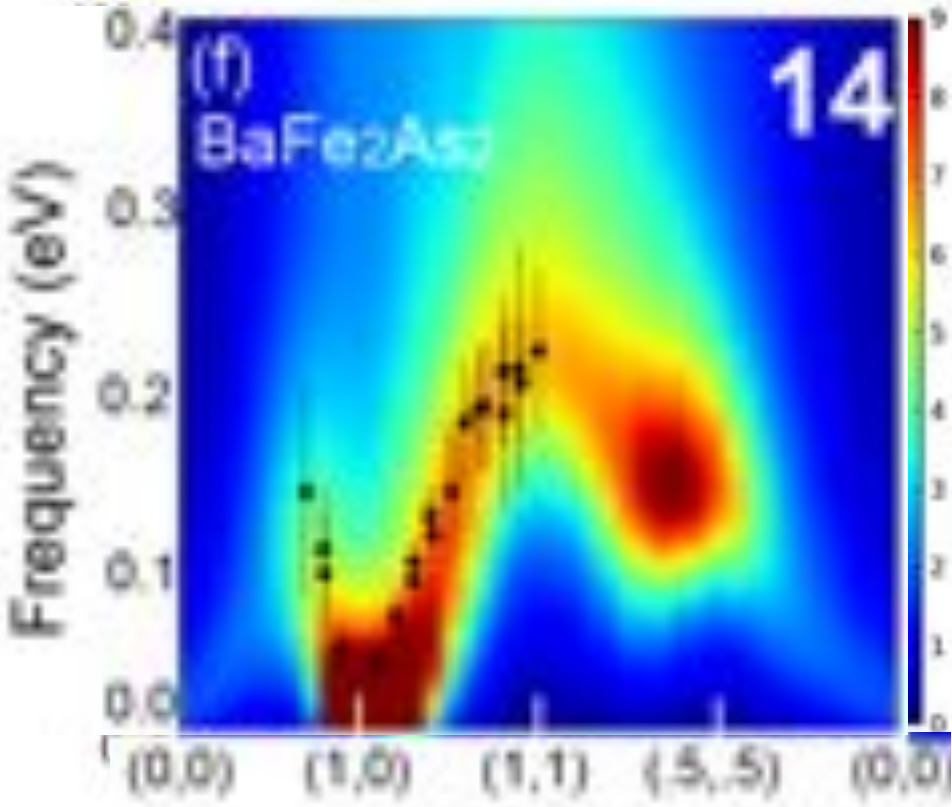
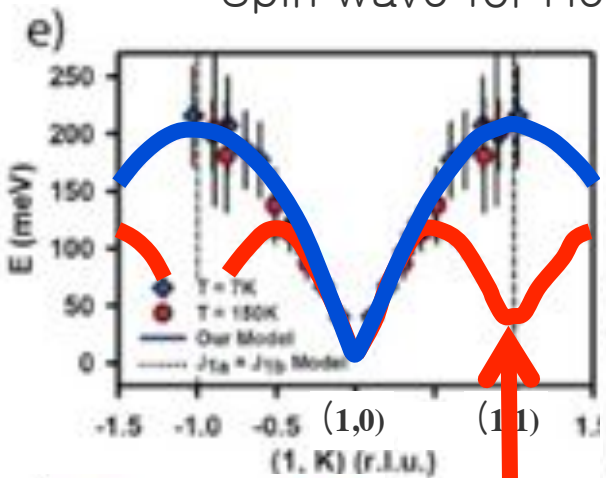


Leland W. Harriger, Pengcheng Dai et al., PRB 84, 054544 (2011).

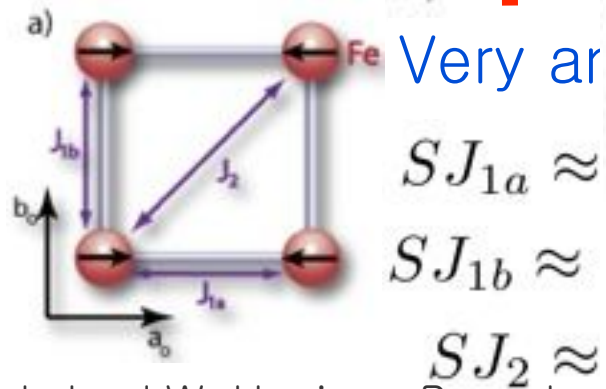
# Dynamical structure factor of BaFe<sub>2</sub>As<sub>2</sub>



Spin wave for Heisenberg model



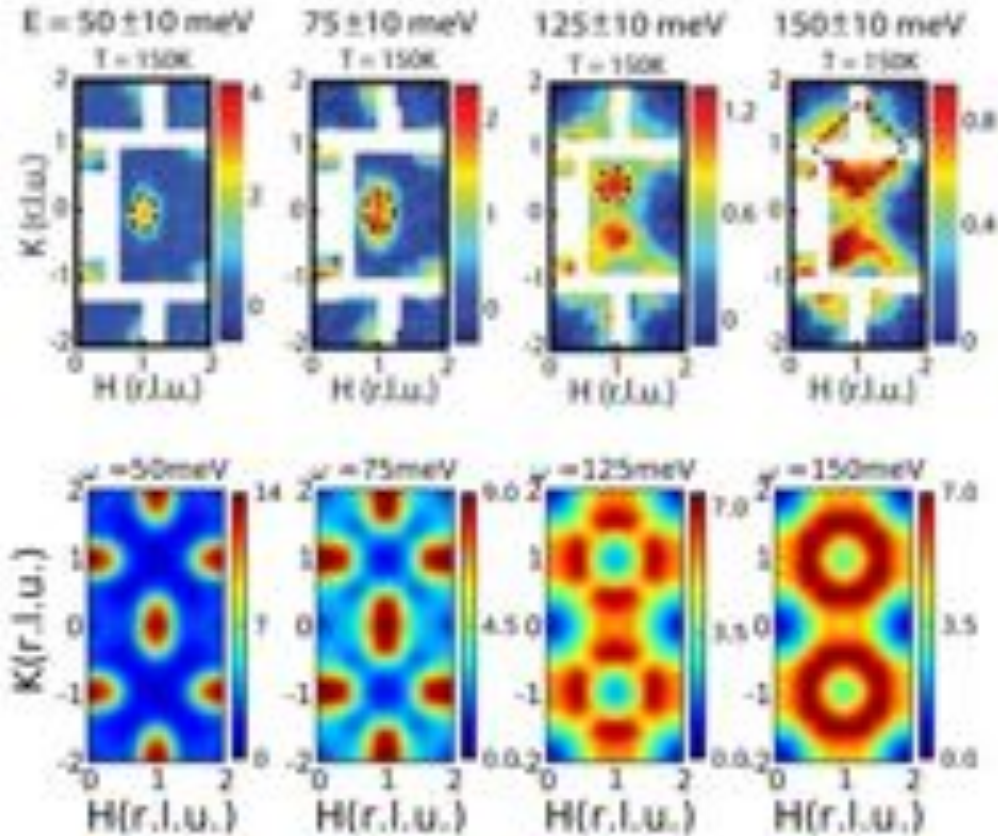
DMFT



Leland W. Harriger, Pengcheng Dai et al., PRB 84, 054544 (2011).

$S(\mathbf{q}, \boldsymbol{\omega})$  in paramagnetic phase similar to AFM phase!  
 No anisotropy needed (above  $T_S$ ) to explain neutrons.

# Dynamical structure factor



Experiment: J. T. Park, et al.,  
PRB 82, 134503 (Oct 2010).

LDA+DMFT: H. Park, et.al.,  
PRL 107, 137007 (2011)

# Large fluctuating moment



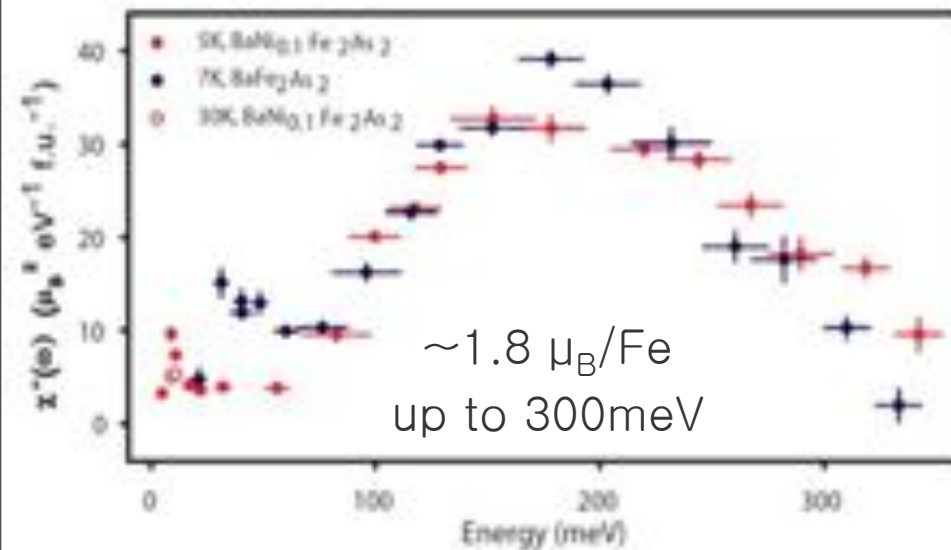
Fluctuating moment by neutrons:  $\langle \mu^2 \rangle = \int \frac{d\omega}{\pi} n(\omega) \chi''(\omega)$

# Large fluctuating moment



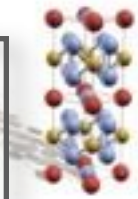
Fluctuating moment by neutrons:  $\langle \mu^2 \rangle = \int \frac{d\omega}{\pi} n(\omega) \chi''(\omega)$

Experiment by Pengcheng Dai



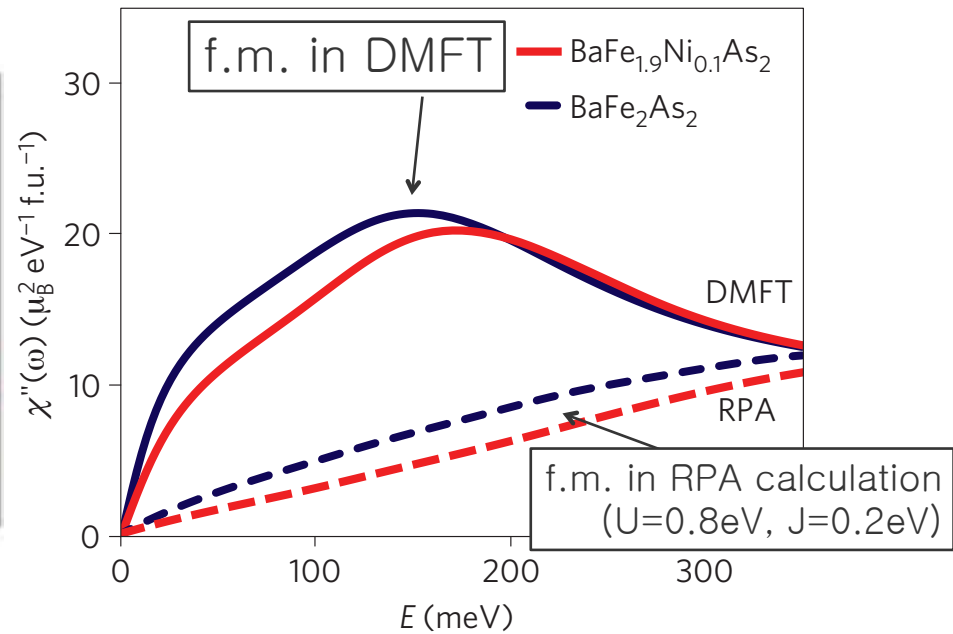
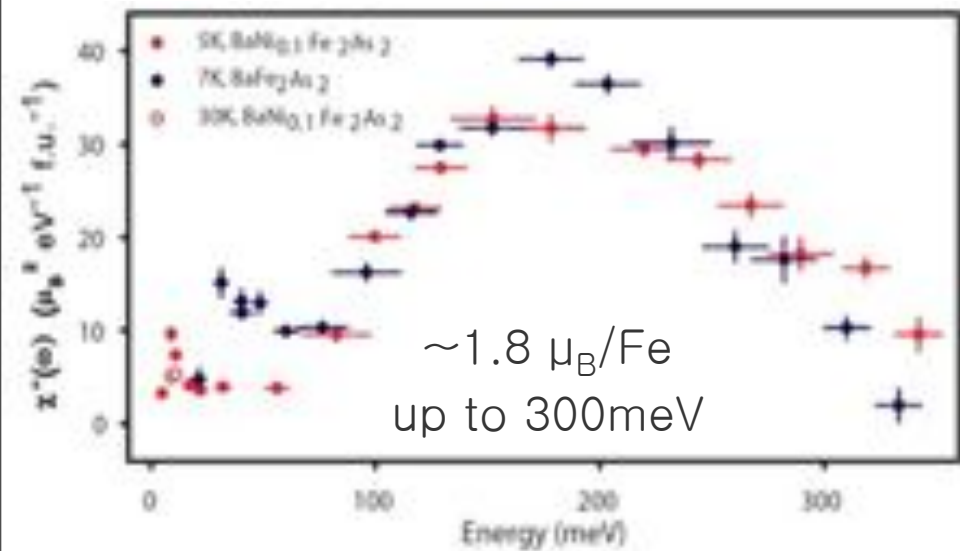


# Large fluctuating moment

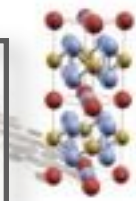


Fluctuating moment by neutrons:  $\langle \mu^2 \rangle = \int \frac{d\omega}{\pi} n(\omega) \chi''(\omega)$

Experiment by Pengcheng Dai

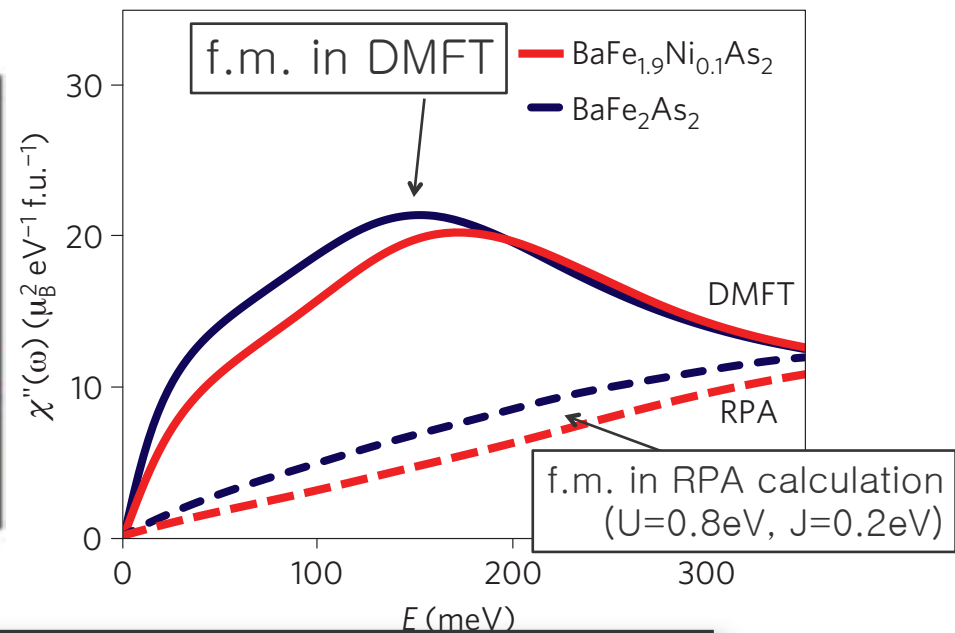
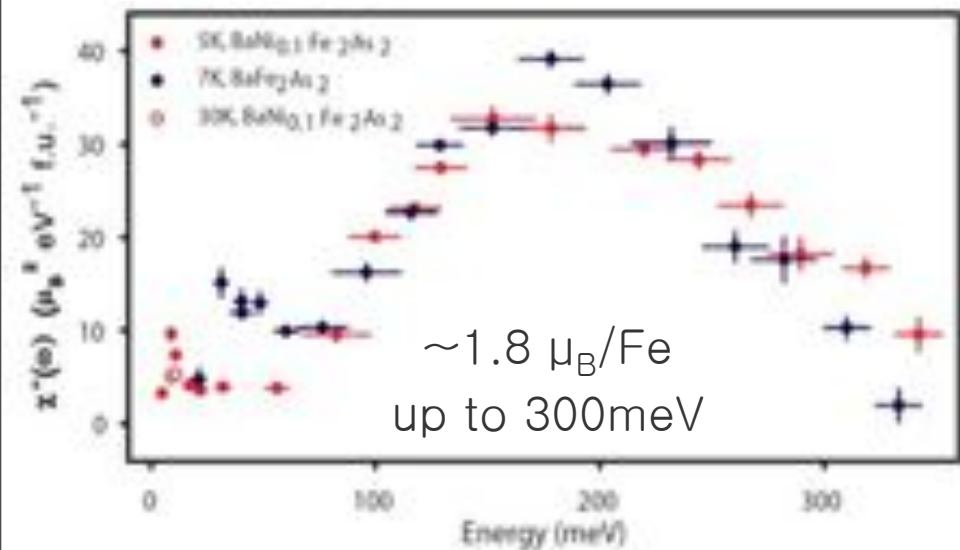


# Large fluctuating moment



Fluctuating moment by neutrons:  $\langle \mu^2 \rangle = \int \frac{d\omega}{\pi} n(\omega) \chi''(\omega)$

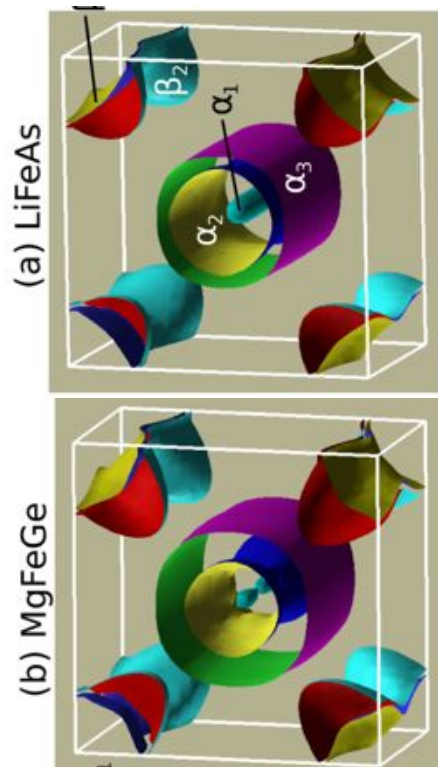
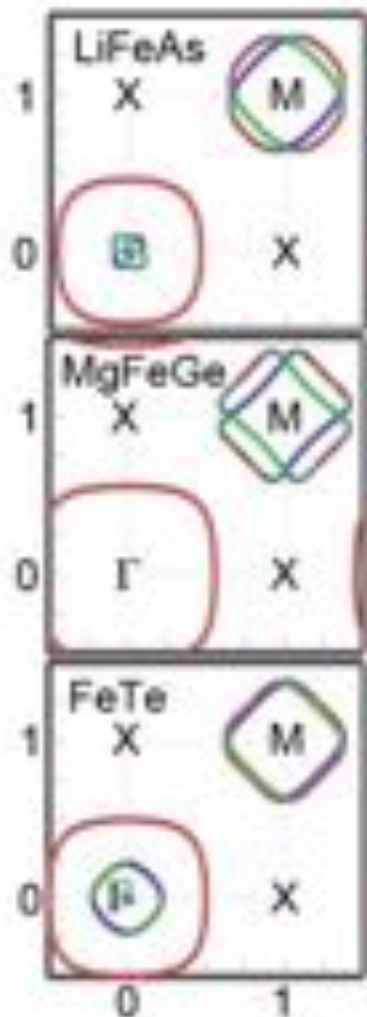
Experiment by Pengcheng Dai



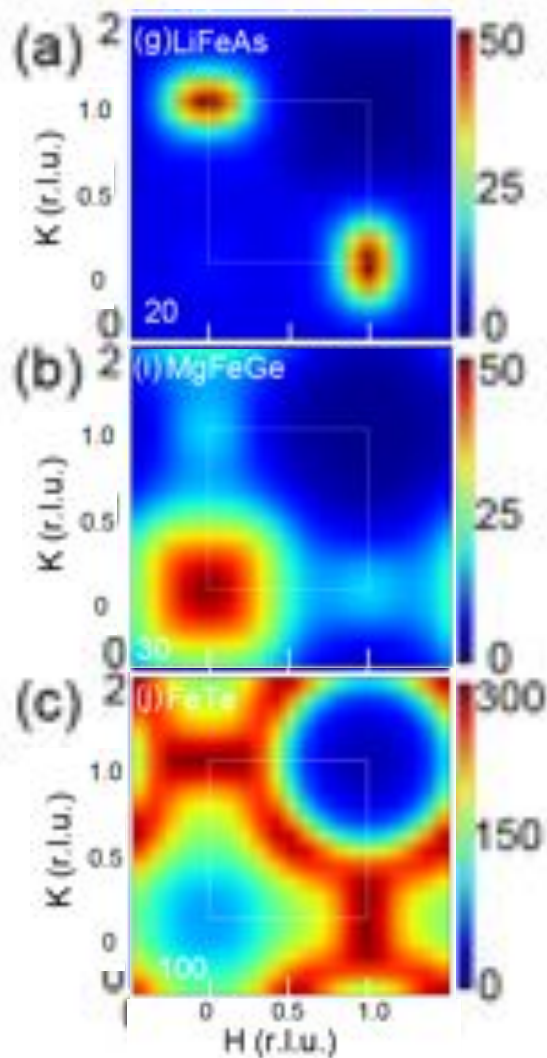
Large fluctuating moment can not be explained by a purely itinerant model - property of Hundness!  
The DMFT account for a dual nature of electrons in Hund's metals: itinerant and localized nature.

# Magnetism not determined only by FS!

Theory: DFT+DMFT



$\omega = 5$  meV



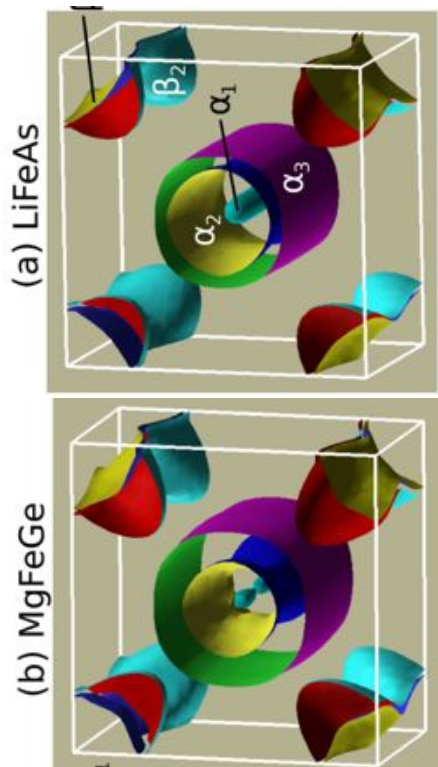
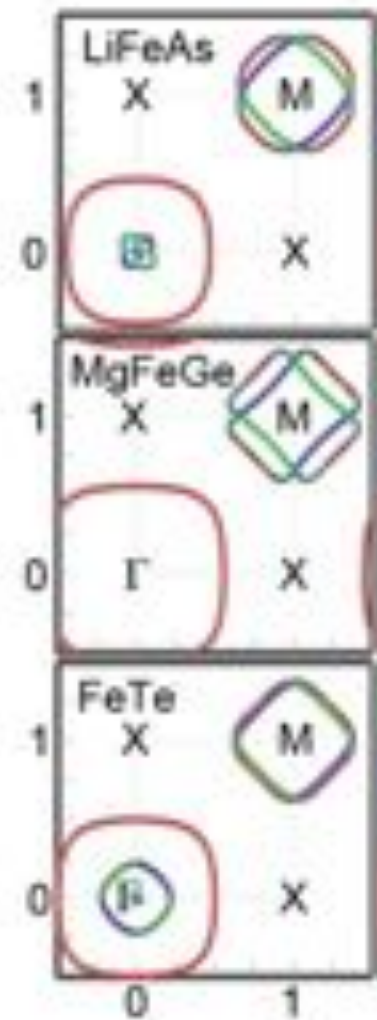
ZPY et al, to be published.

# Magnetism not determined only by FS!

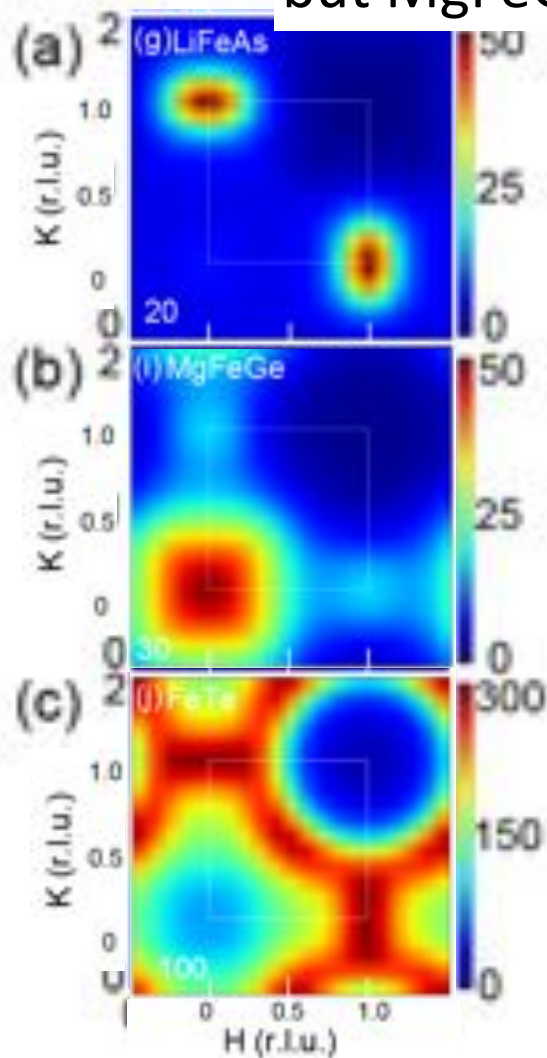
Theory: DFT+DMFT

Why is LiFeAs SC

but MgFeGe/FeTe not?



$\omega = 5$  meV



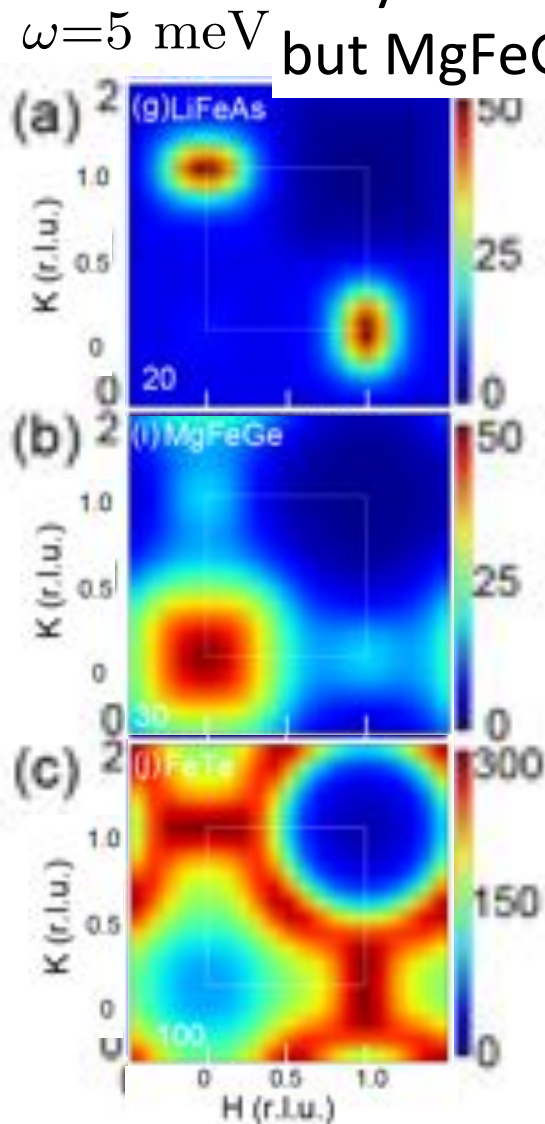
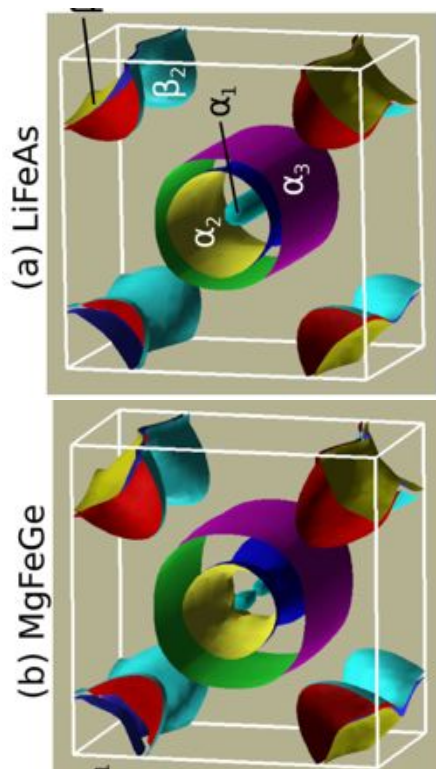
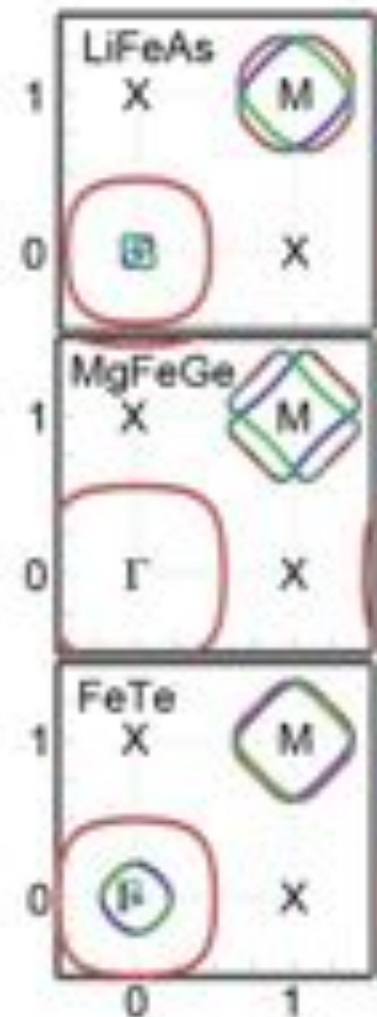
ZPY et al, to be published.

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Theory: DFT+DMFT

Why is LiFeAs SC

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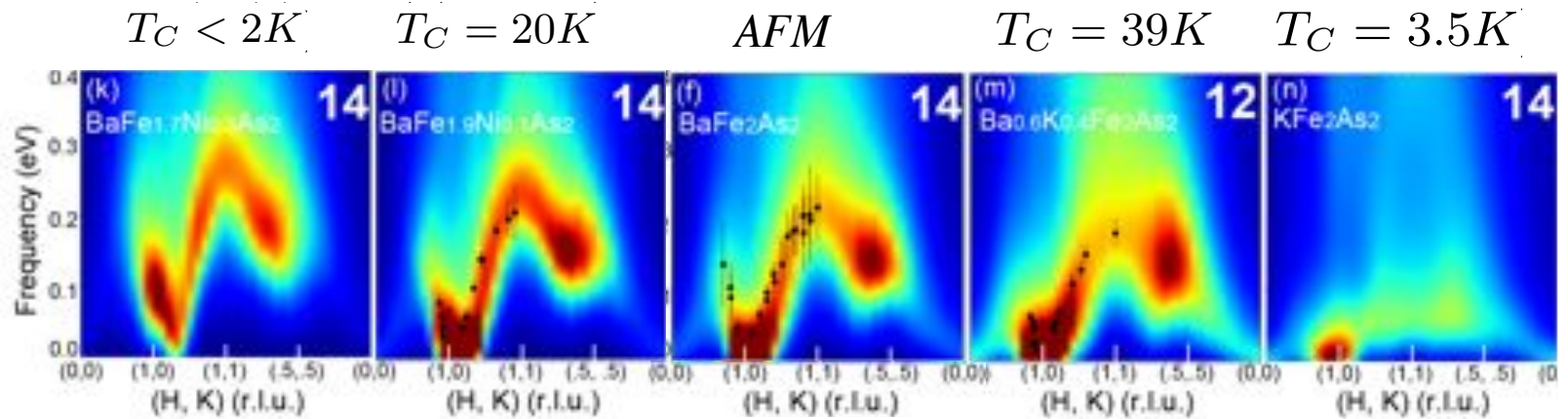


Very different  
magnetic  
excitations

ZPY et al, to be published.

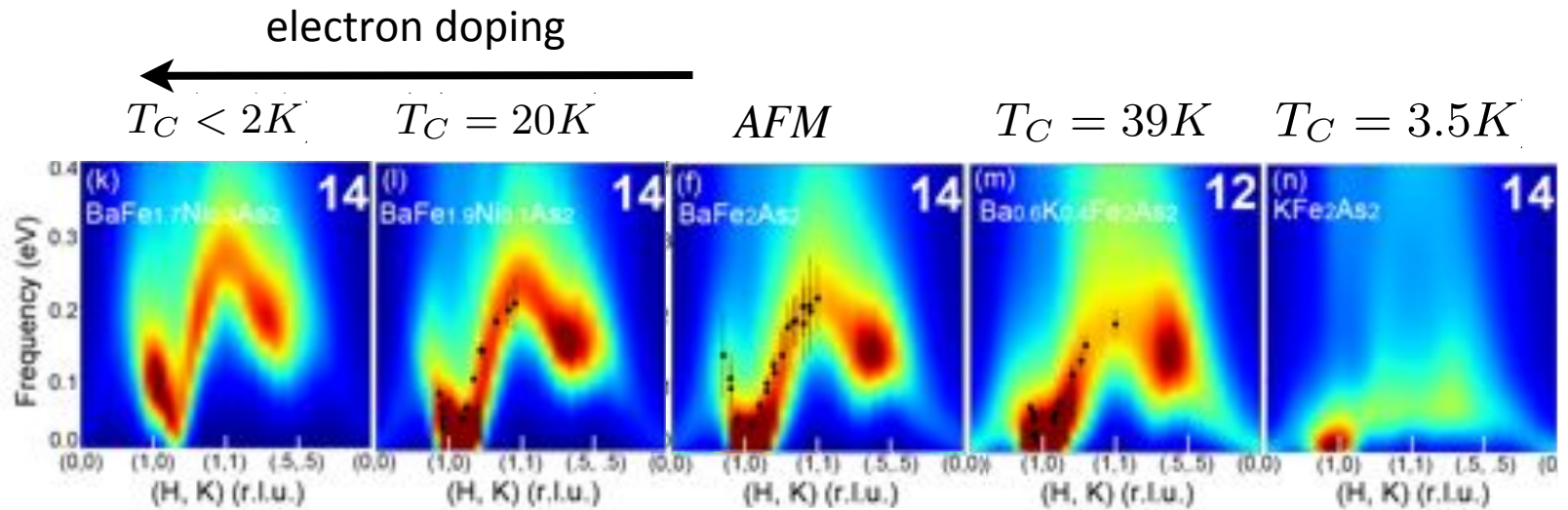
# Theoretical Magnetic excitations

## Doping variation



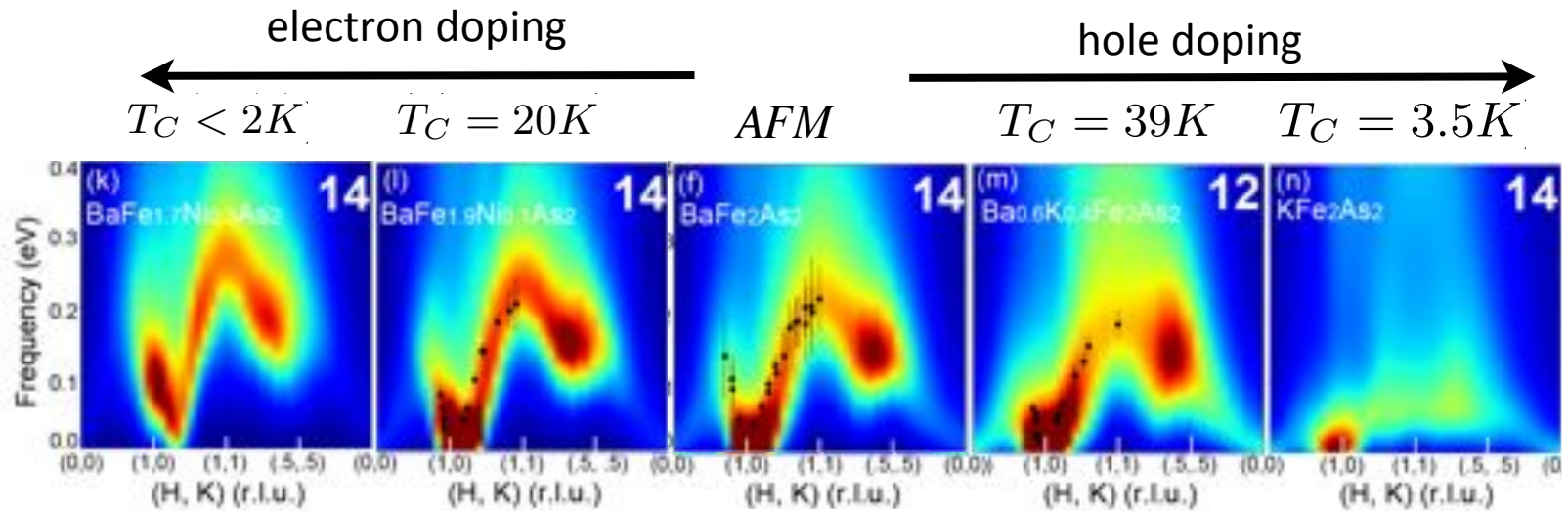
# Theoretical Magnetic excitations

## Doping variation



# Theoretical Magnetic excitations

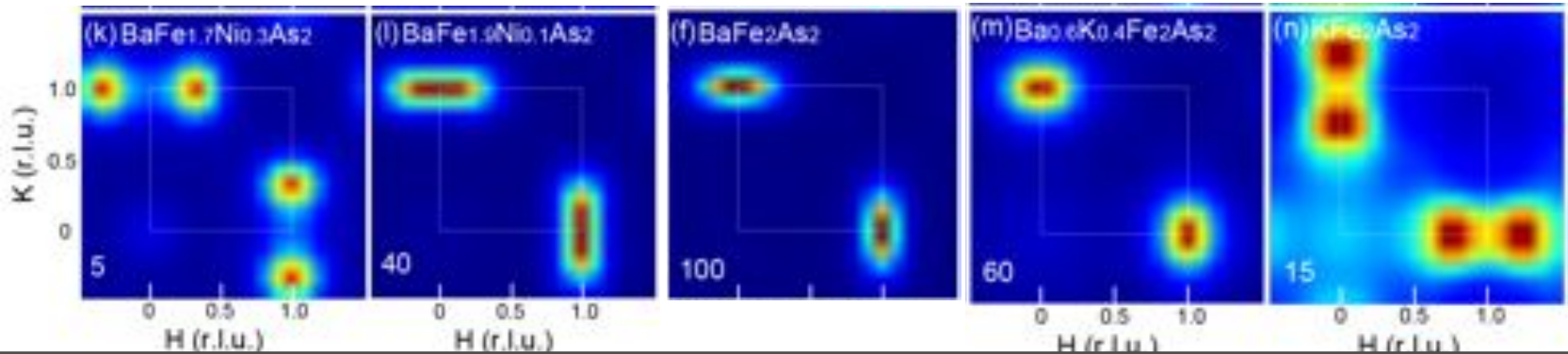
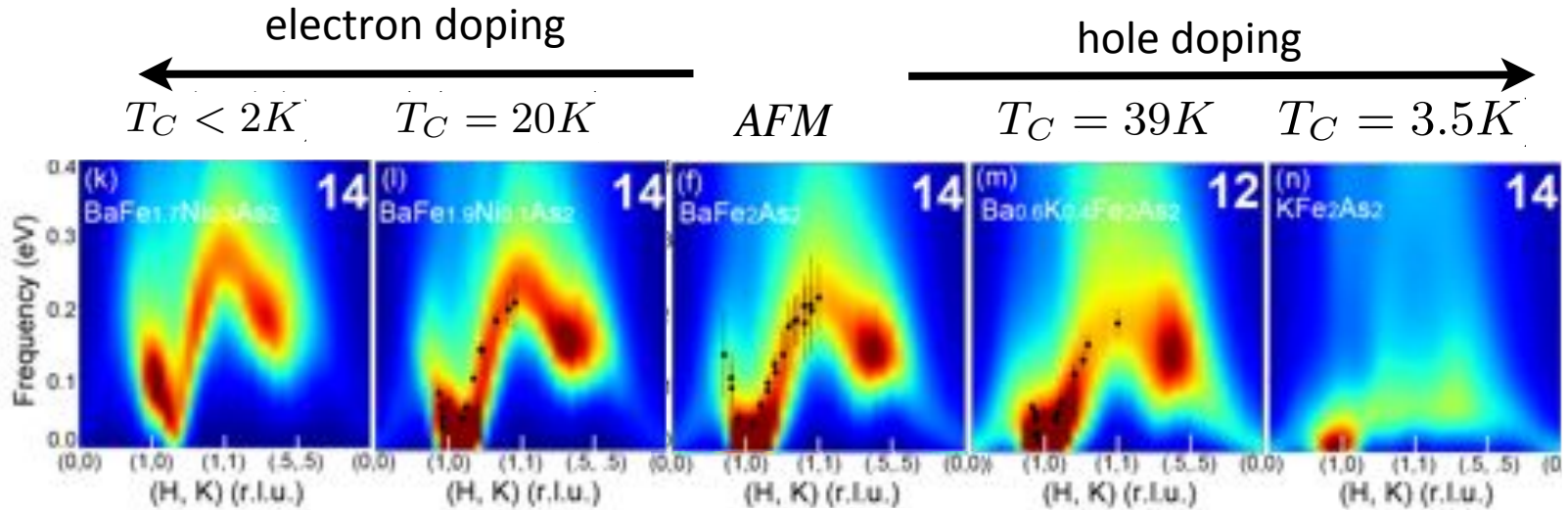
## Doping variation





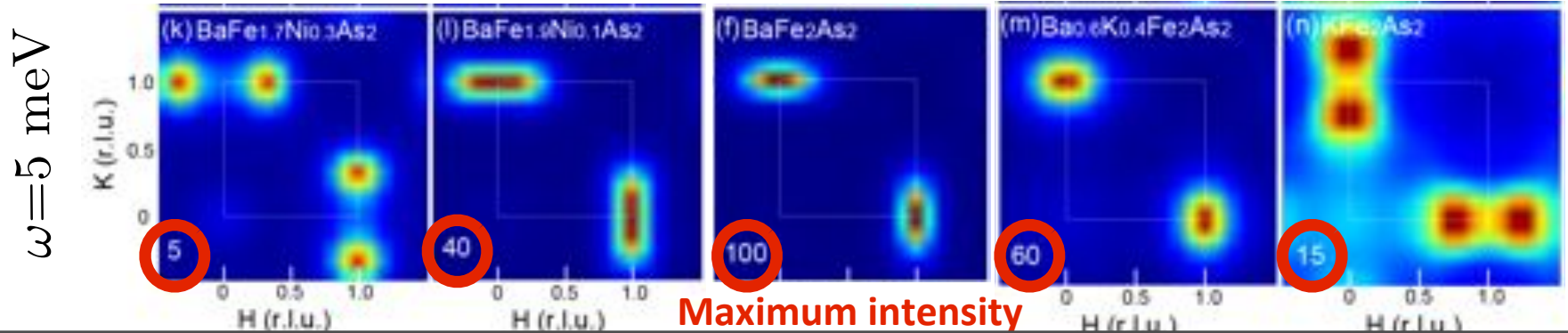
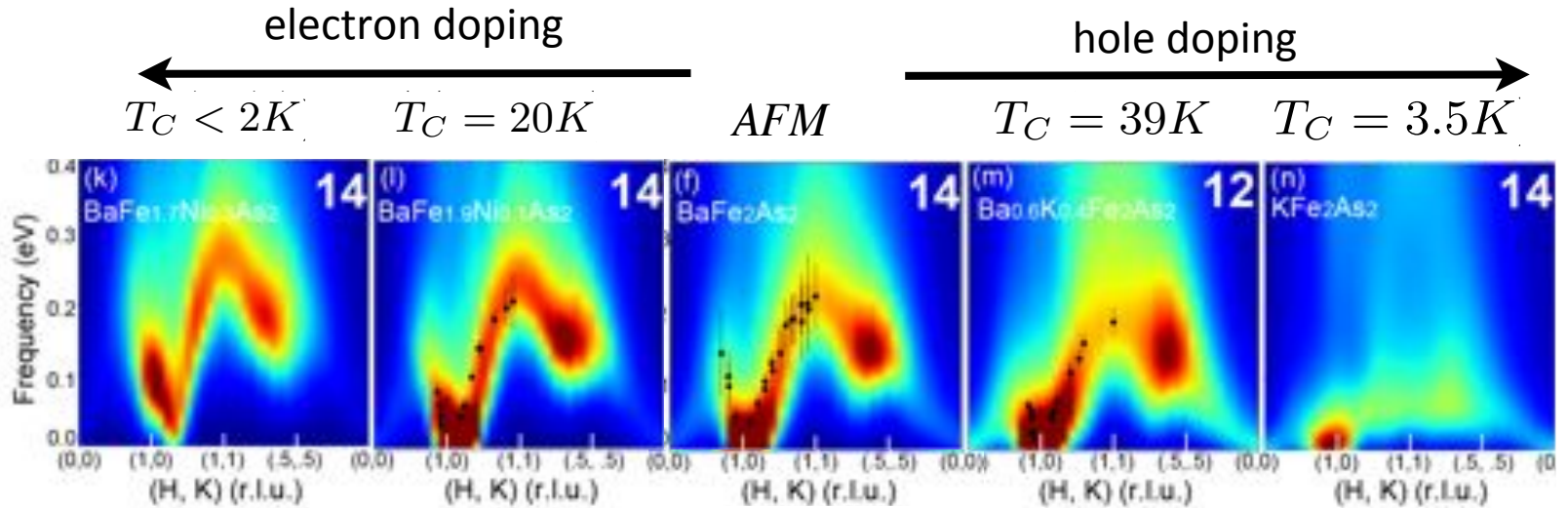
# Theoretical Magnetic excitations

## Doping variation



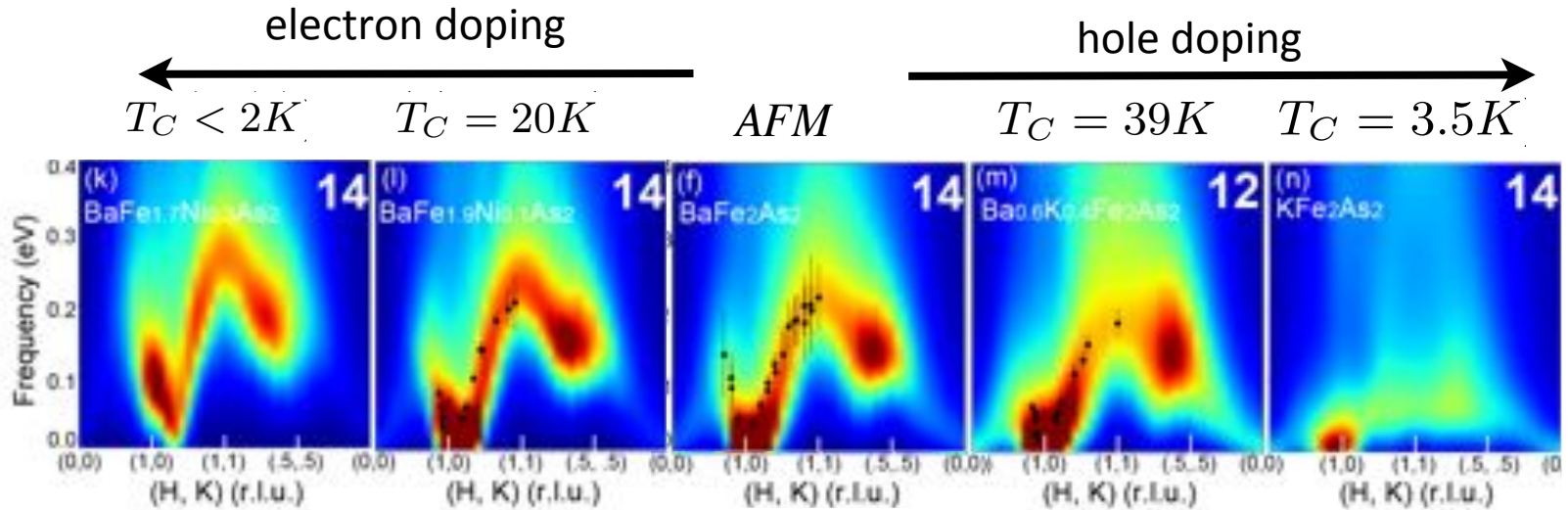
# Theoretical Magnetic excitations

## Doping variation

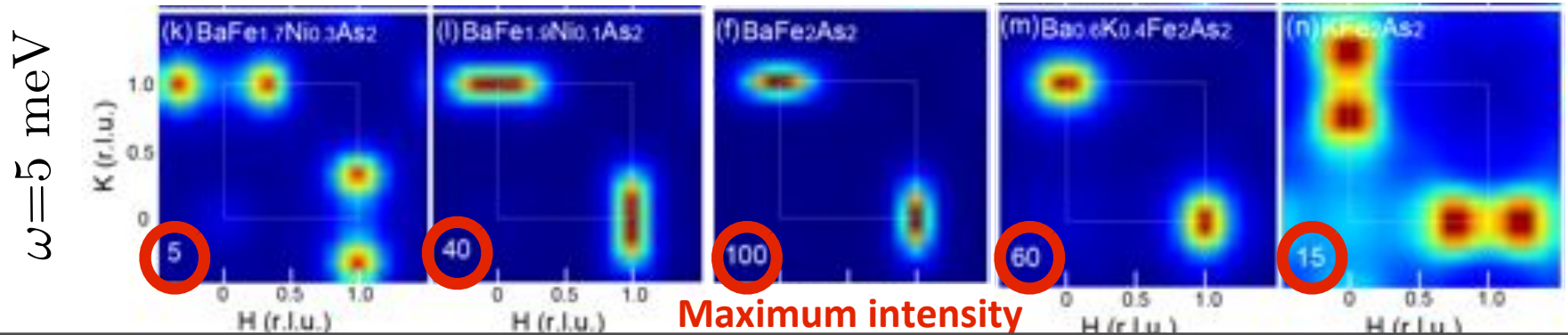


# Theoretical Magnetic excitations

## Doping variation

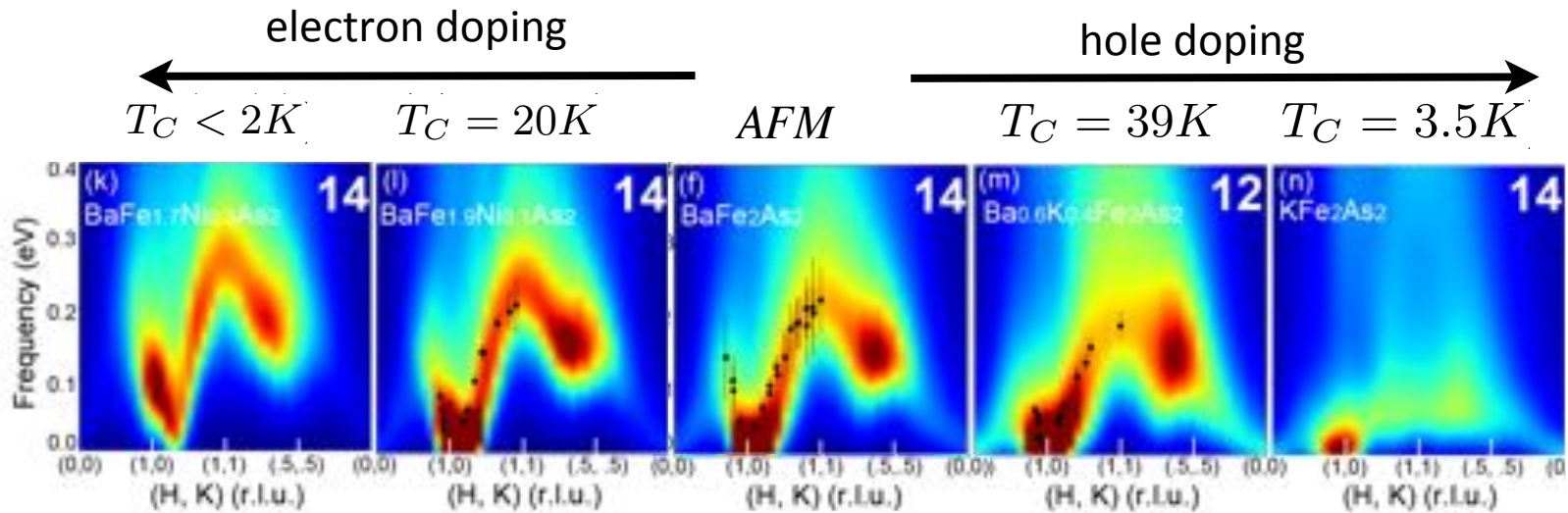


electron overdoped:  
 low energy spin excitations  
**very weak**  
 and become **incommensurate**



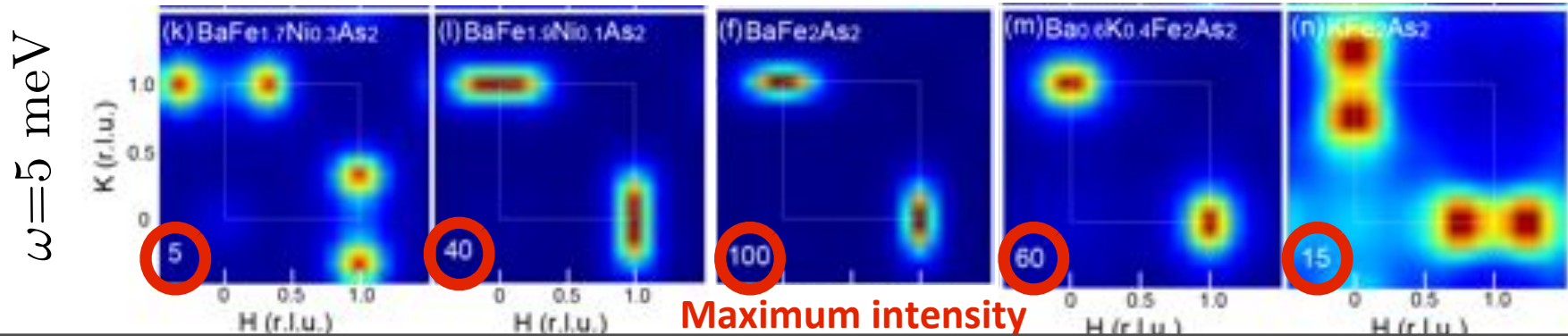
# Theoretical Magnetic excitations

## Doping variation



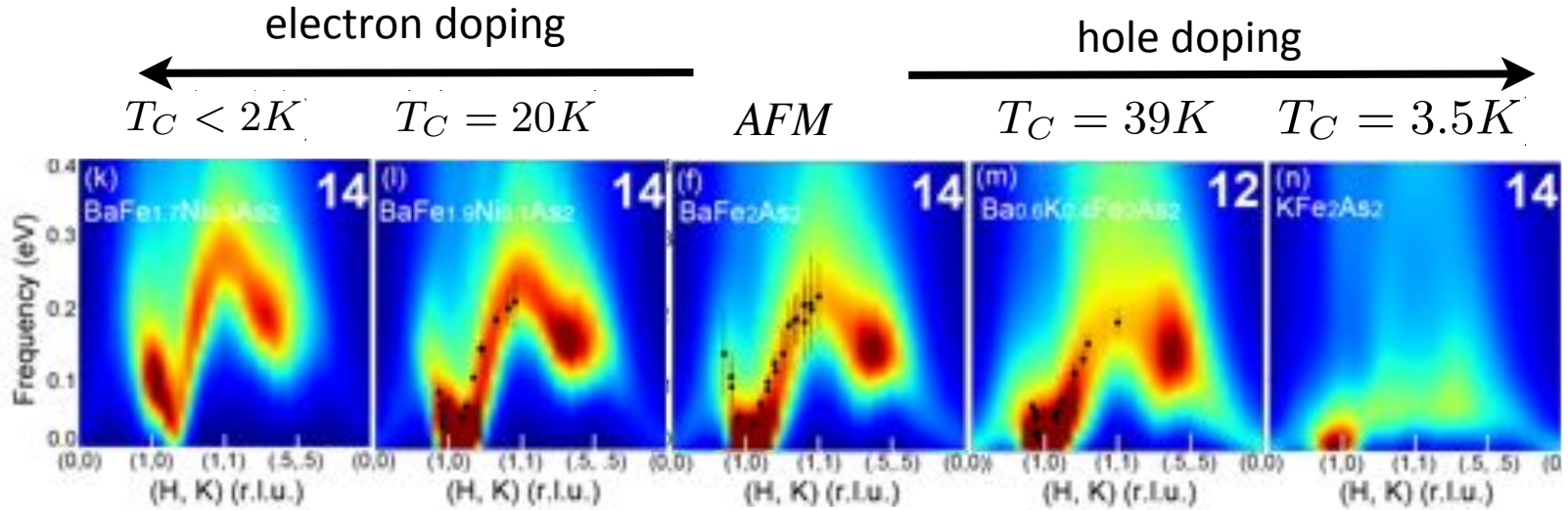
electron overdoped:  
 low energy spin excitations  
**very weak**  
 and become **incommensurate**

hole overdoped:  
 low energy spin excitations  
**weaker**  
 and **incommensurate**



# Theoretical Magnetic excitations

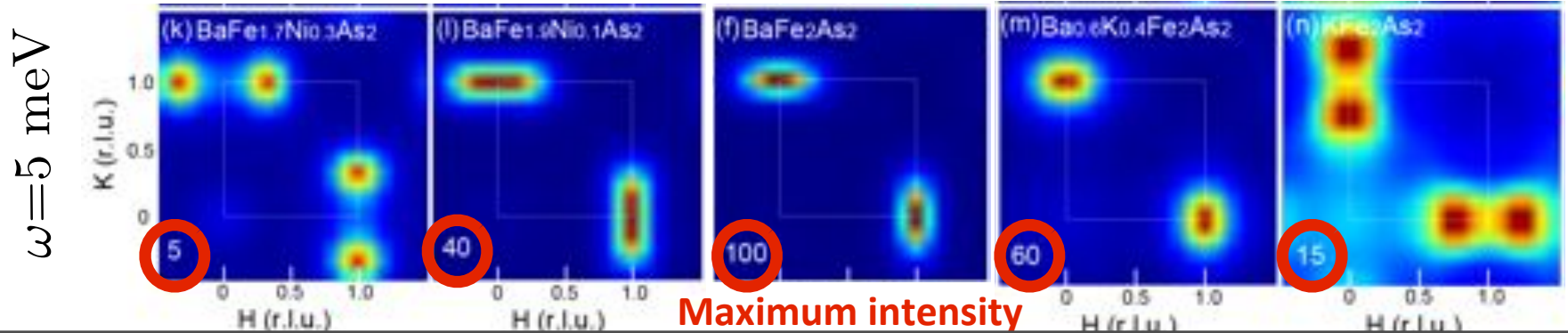
## Doping variation



electron overdoped:  
 low energy spin excitations  
**very weak**  
 and become **incommensurate**

Optimally doped:  
 Commensurate low energy  
 strong low energy  
 strong high energy

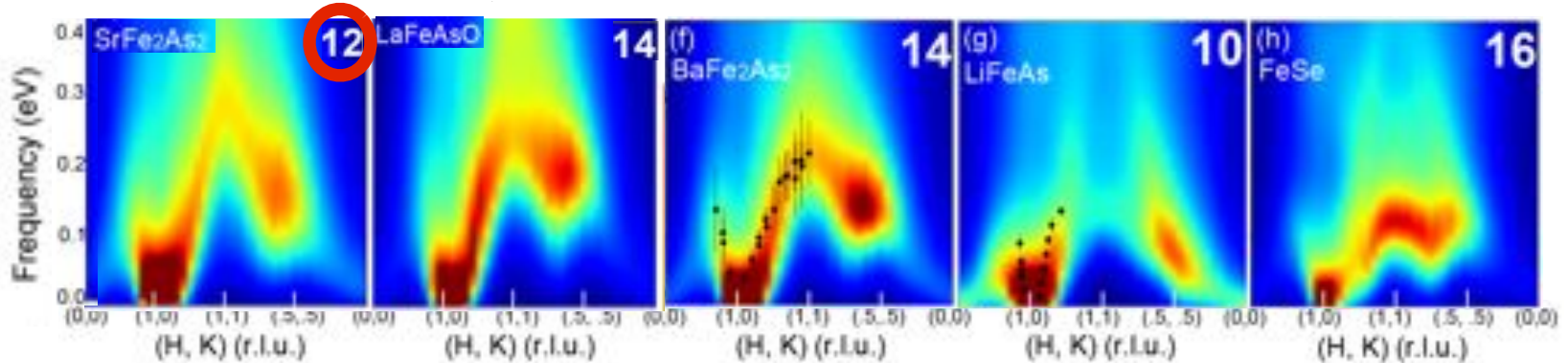
hole overdoped:  
 low energy spin excitations  
**weaker**  
 and **incommensurate**



# Variation across families

## High-T<sub>c</sub> compounds

$$T_C^{max} = 37K \quad T_C^{max} = 43K \quad T_C^{max} = 39K \quad T_C = 18K \quad T_C^{max} = 37K$$

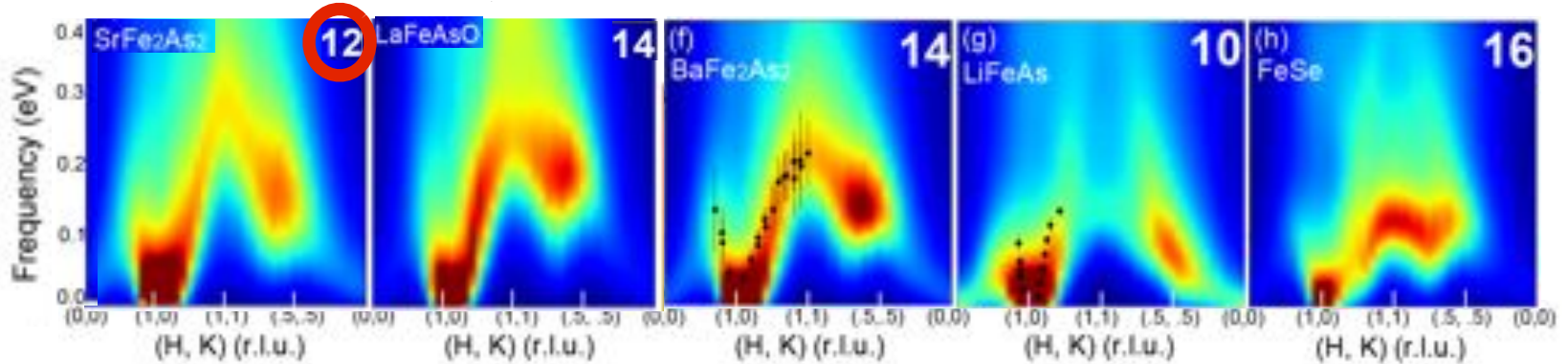


Maximum intensity

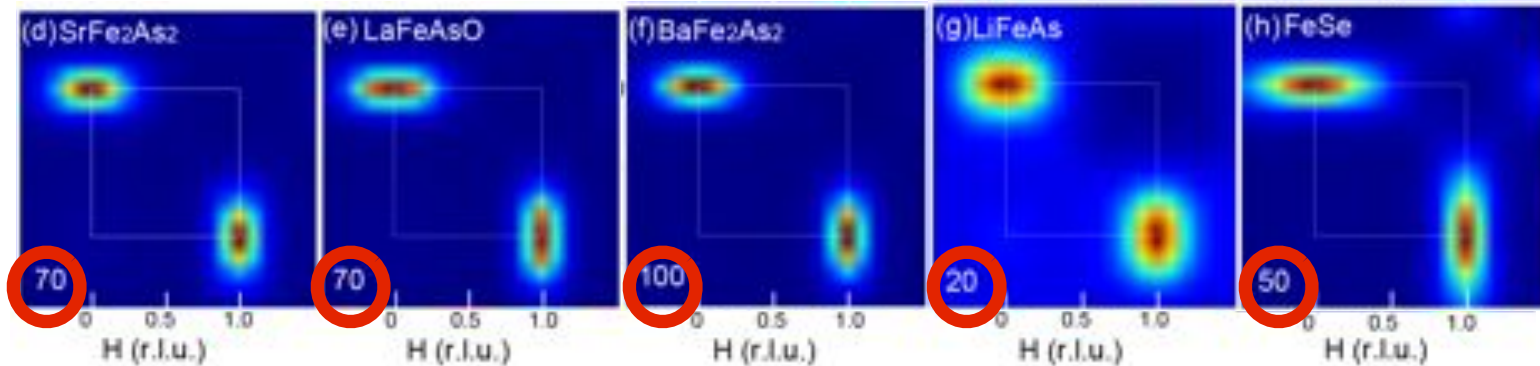
# Variation across families

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$$T_C^{max} = 37K \quad T_C^{max} = 43K \quad T_C^{max} = 39K \quad T_C = 18K \quad T_C^{max} = 37K$$



$\omega = 5$  meV

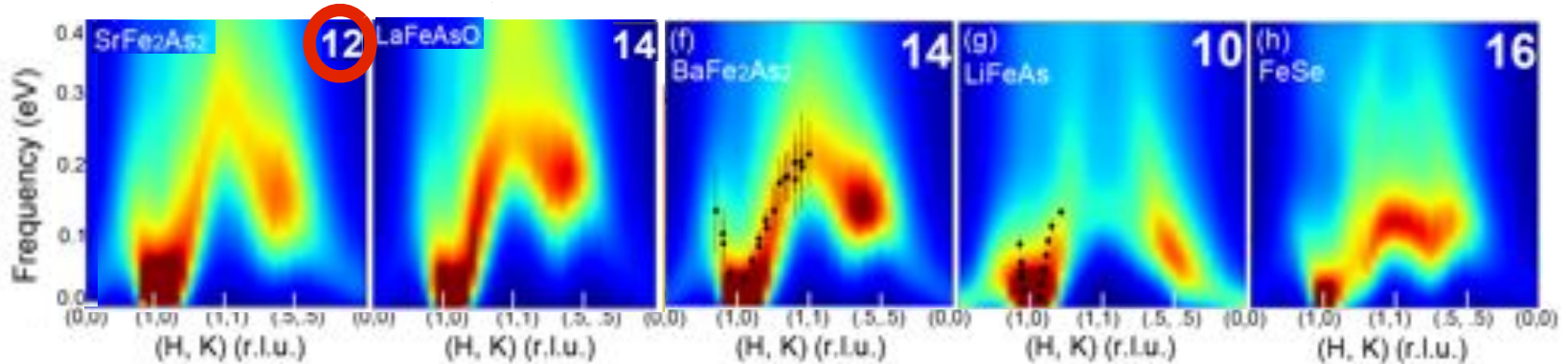


Maximum intensity

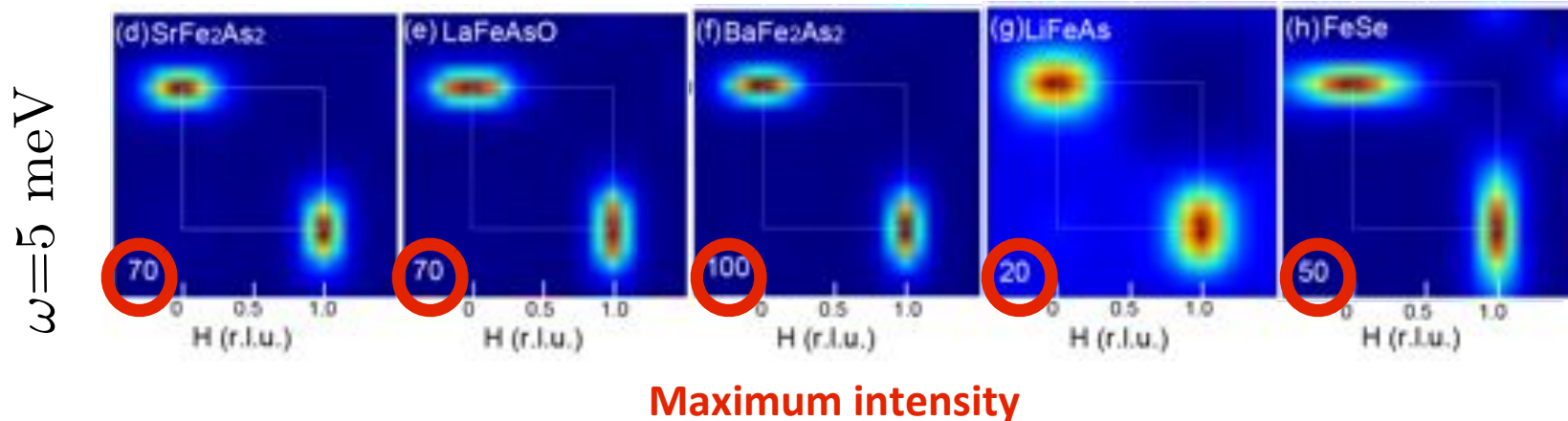
# Variation across families

## High-Tc compounds

$$T_C^{max} = 37K \quad T_C^{max} = 43K \quad T_C^{max} = 39K \quad T_C = 18K \quad T_C^{max} = 37K$$



high Tc: **Strong commensurate low energy excitations, strong high energy dispersive exc.**



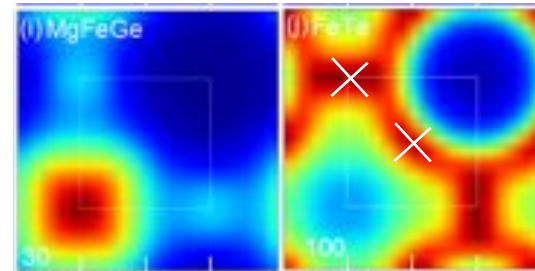
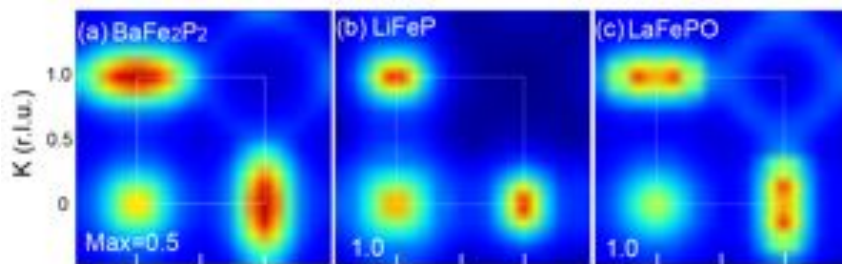
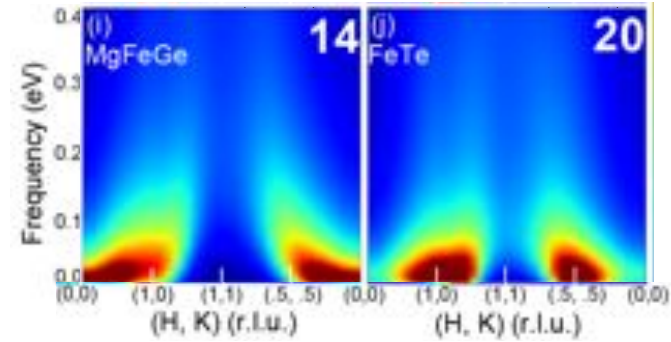
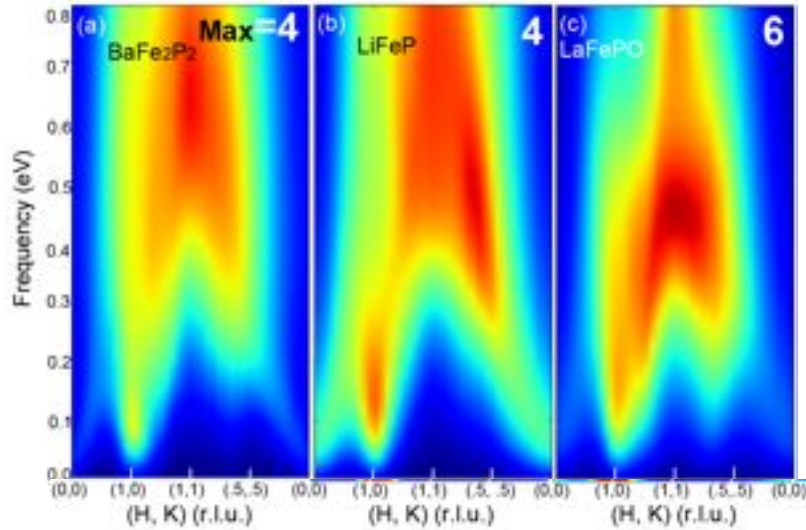


# Variation across families

## Low- $T_c$ compounds

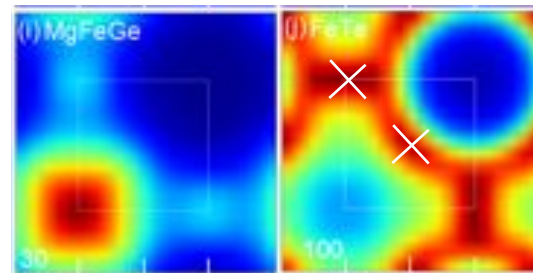
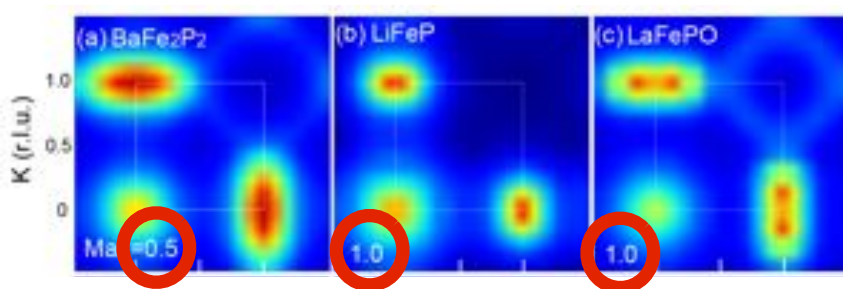
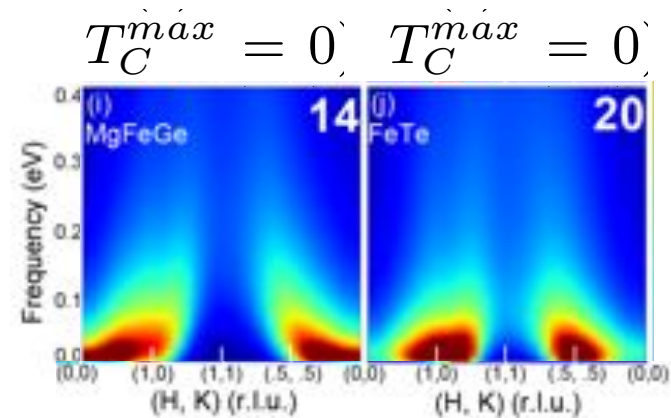
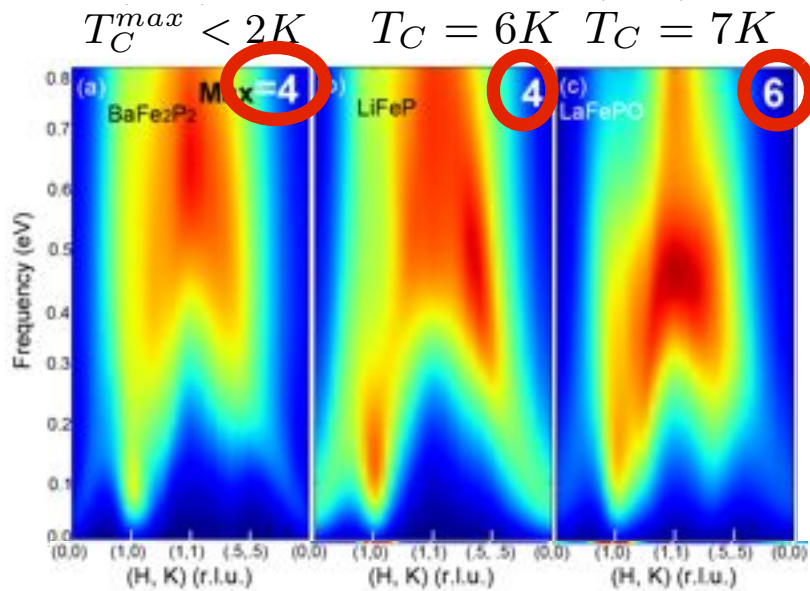
$T_C^{max} < 2K$     $T_C = 6K$     $T_C = 7K$

$T_C^{max} = 0$     $T_C^{max} = 0$



# Variation across families

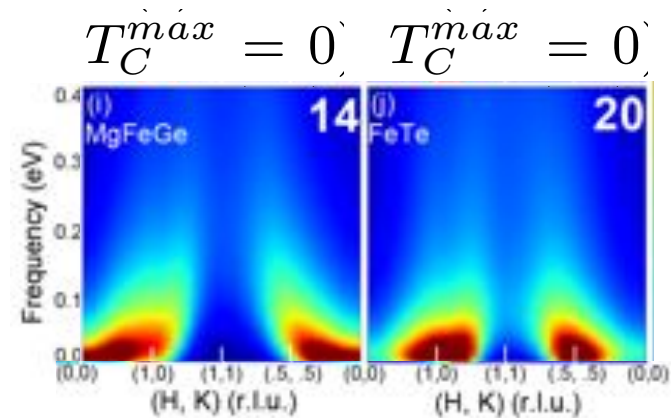
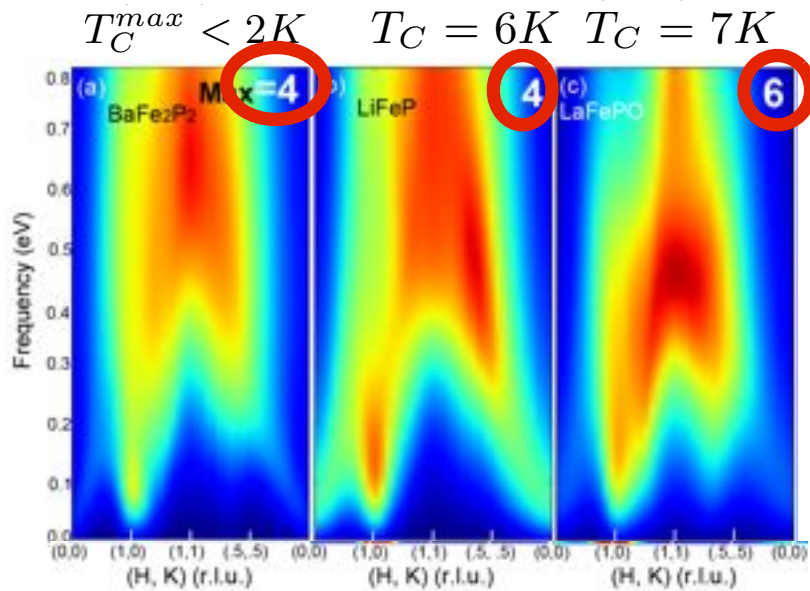
## Low- $T_c$ compounds



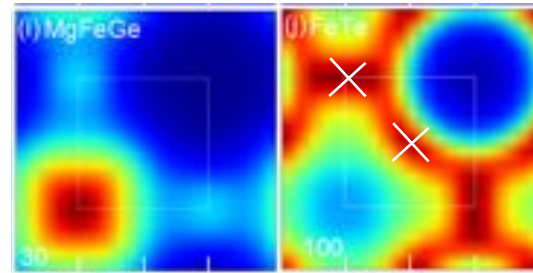
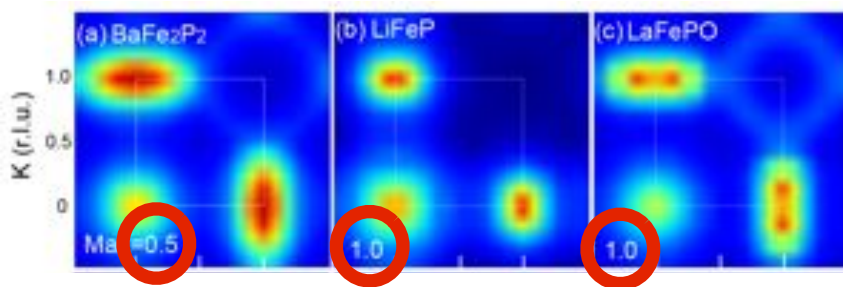
**Maximum intensity  
two orders of magnitude smaller**

# Variation across families

## Low- $T_c$ compounds



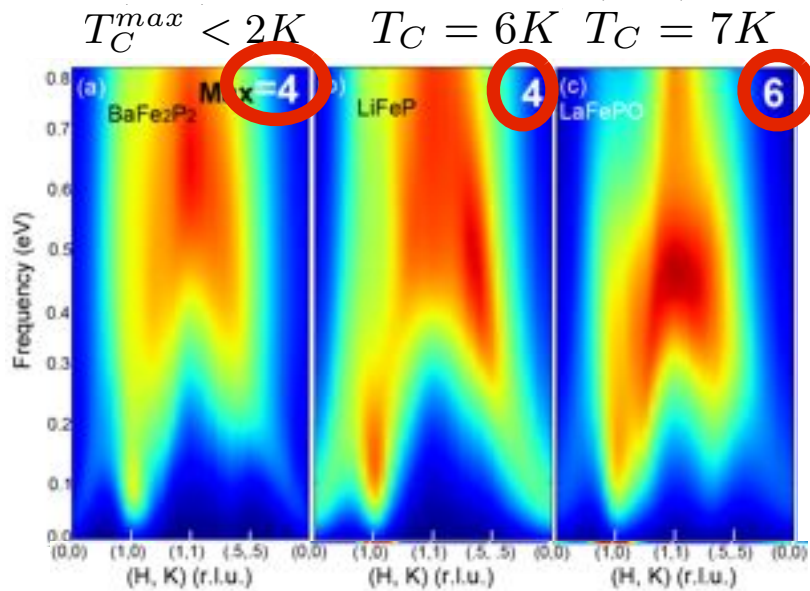
very small low energy intensity  
competing order at (0,0)!



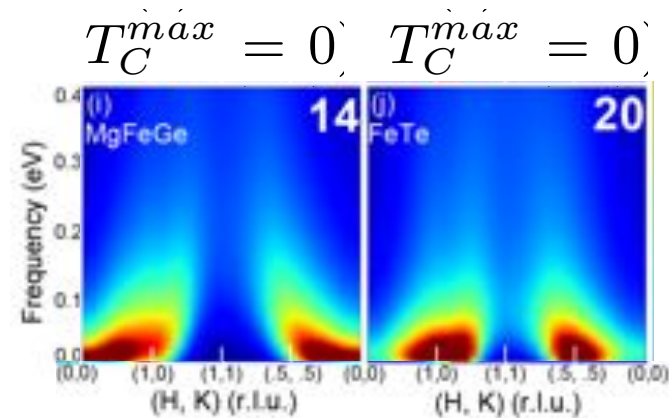
Maximum intensity  
two orders of magnitude smaller

# Variation across families

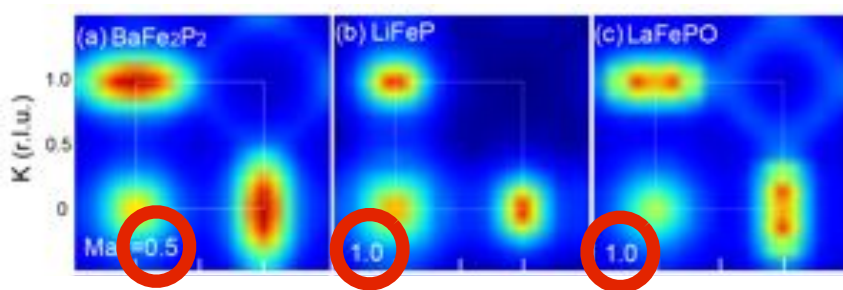
## Low- $T_c$ compounds



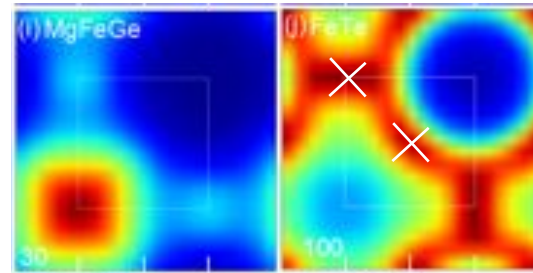
very small low energy intensity  
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broad with  
mostly  
(0,0) peak

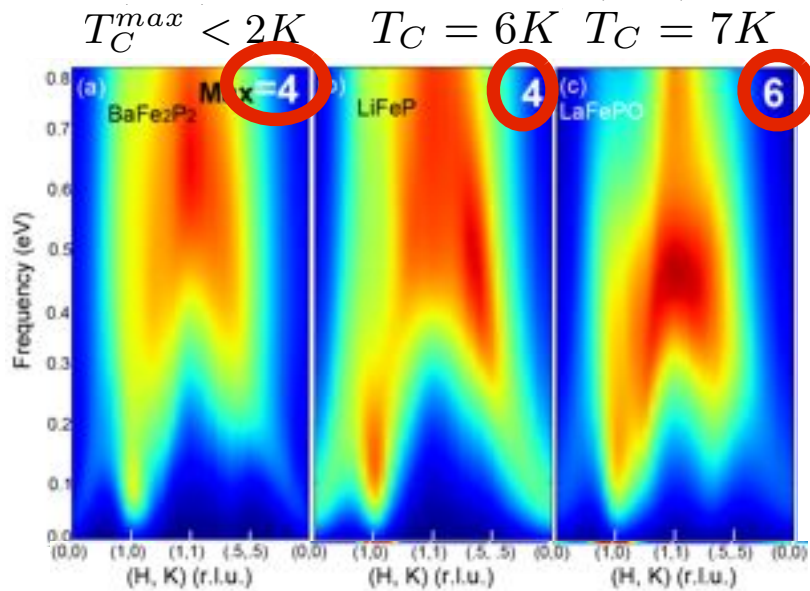


Maximum intensity  
two orders of magnitude smaller

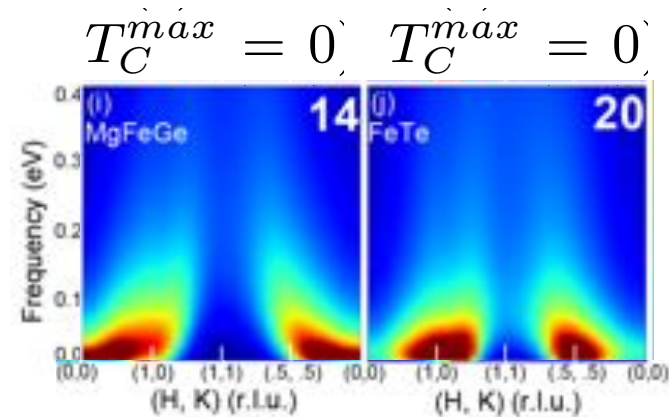


# Variation across families

## Low- $T_c$ compounds

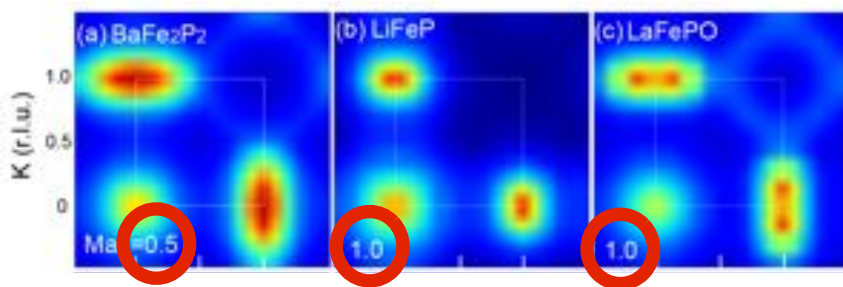


very small low energy intensity  
competing order at (0,0)!

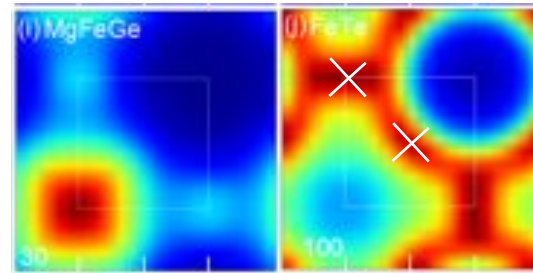


broad with mostly (0,0) peak

two competing orders (1,0)&(1/2,1/2)



Maximum intensity  
two orders of magnitude smaller

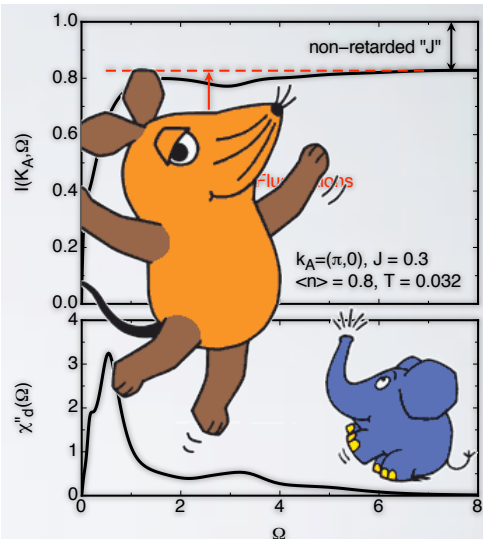


# What do we need for SC?



P.W. Anderson, Science 316, 1705 (2007):  
“We have a mammoth ( $U$ ) and an elephant ( $J$ )  
in our refrigerator -do we care if  
there is also a mouse (*spin fluctuations*)?”

“We have a mammoth and an elephant in our refrigerator—  
do we care much if there is also a mouse?”



D. Scalapino & T. Maier:  
Spin fluctuation theory and weak coupling  
approaches: Only *low energy spin  
fluctuations are important* :  
“mouse is larger than the elephant”

# What do we need for SC?



"We have a mammoth and an elephant in our refrigerator—do we care much if there is also a mouse?"

P.W. Anderson, *Science* 316, 1705 (2007):  
"We have a mammoth ( $U$ ) and an elephant ( $J$ )  
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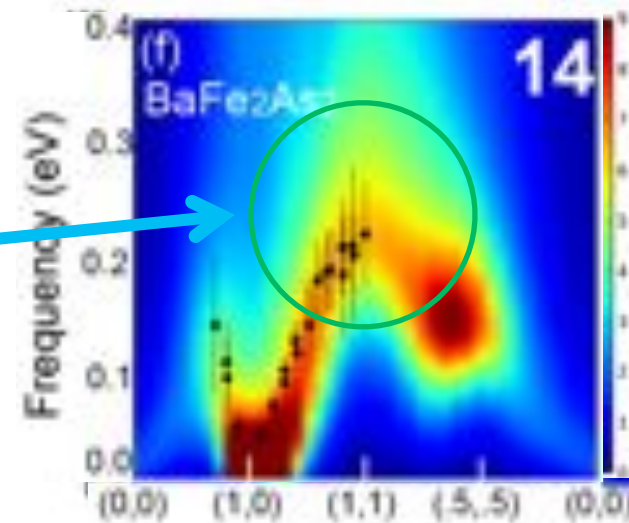


"We have a mammoth and an elephant in our refrigerator—do we care much if there is also a mouse?"

P.W. Anderson, *Science* 316, 1705 (2007):  
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there is also a mouse (spin fluctuations)?"

*Both appear in iron superconductors:*

high-energy magnetic excitations with well-defined dispersion  
(which give large fluctuating moment)





# What do we need for SC?



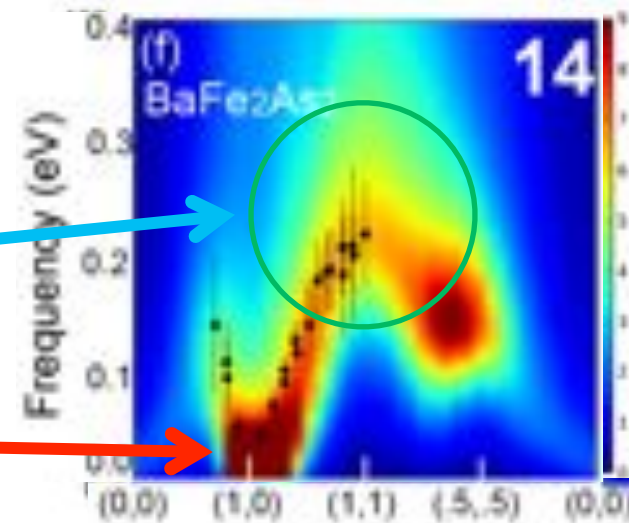
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"We have a mammoth ( $U$ ) and an elephant ( $J$ ) in our refrigerator -do we care if there is also a mouse (spin fluctuations)?"

*Both appear in iron superconductors:*

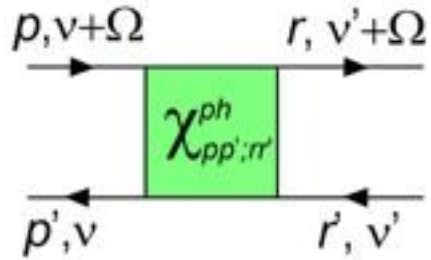
high-energy magnetic excitations with well-defined dispersion (which give large fluctuating moment)

commensurate (1,0) low-energy magnetic excitations (spin fluctuations)

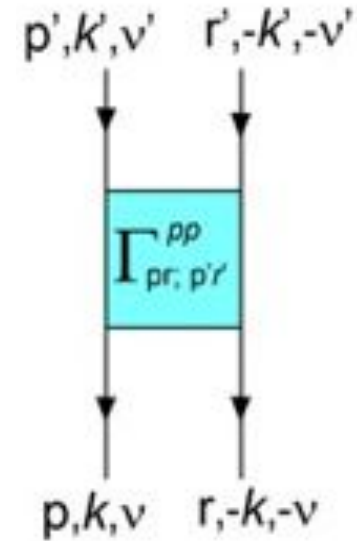


# Particle-particle irreducible vertex

have particle hole

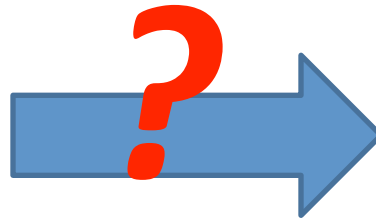
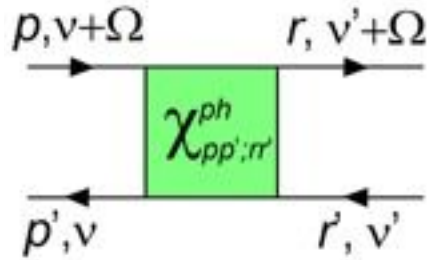


want

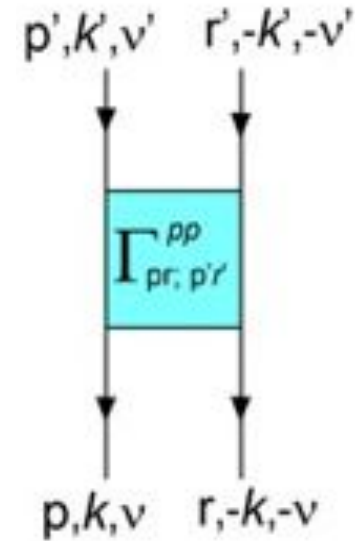


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have particle hole

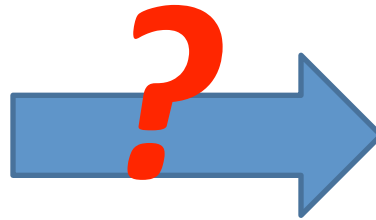
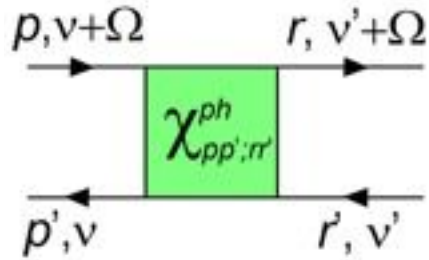


want

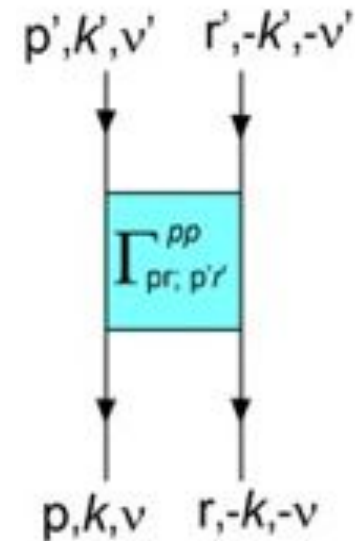


# Particle-particle irreducible vertex

have particle hole



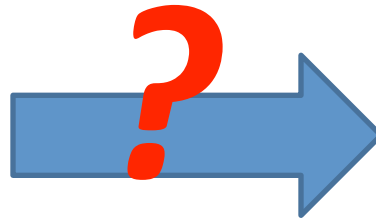
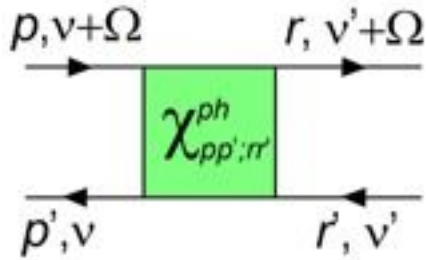
want



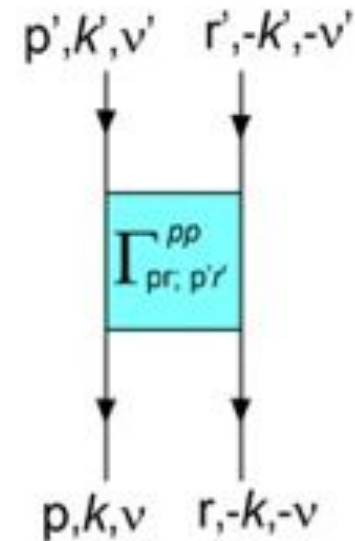
We can compute particle-particle vertex using particle-hole vertex and susceptibility:

# Particle-particle irreducible vertex

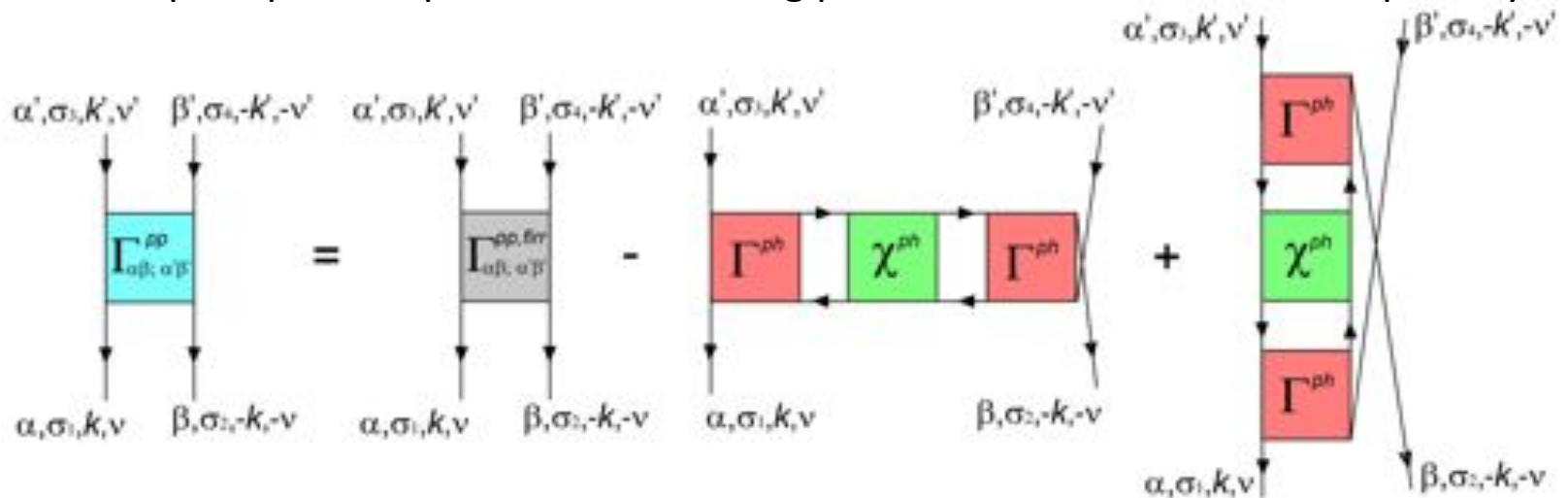
have particle hole

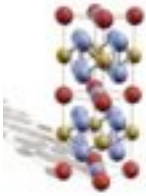


want



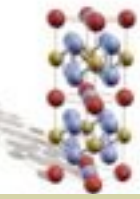
We can compute particle-particle vertex using particle-hole vertex and susceptibility:





# Summary

- Electronic dynamics in Fe superconductors nontrivial because electrons are not well described by localized or itinerant picture: intermediate regime where both the Fermi surface and magnetic exchange play the role. This regime can be described by LDA+DMFT.
- Mass enhancement due to electronic correlations are significant in Fe superconductors ( $> \sim 3$ ), exceed 7 in FeTe.
- Electronic correlations are significant because of Hund's coupling, and not because of Hubbard  $U$ . New physics of Hund's metals as opposed to Mott insulators!
- Correlations give rise to large fluctuating moment at low energy.
- Magnetic spectrum is very sensitive to details (doping), for superconductivity need significant low energy fluctuating moments and large exchange interaction, which can be found at the intermediate correlation strength.
- Three superconducting symmetries are competing,  $s_{+-}$ ,  $d$ , and novel "orbital-antiphase  $s_{+-}$ ", which might be the best candidate in LiFeAs.



THANK YOU!